

FIXED POINTS OF INFINITELY CONNECTED DOMAIN CONTINUOUS MAPPINGS

ALEXANDER KIRILLOV* AND VICTOR STARKOV**

*Institute of Applied Mathematical Research
Karelian Research Centre
Russian Academy of Sciences
11, Pushkinskaya str., Petrozavodsk
Karelia 185910
Russia
E-mail: kirillov@krc.karelia.ru

** Department of Mathematics
Petrozavodsk State University
33, Lenin str., Petrozavodsk
Karelia 185910
Russia
E-mail: vstar@psu.karelia.ru

Abstract. We consider infinitely connected domain continuous mappings, satisfying the condition of interior boundary components interchange. The fixed point theorem is proved.

Key Words and Phrases: Fixed point, infinitely connected compact, spherical compact, globular compact.

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