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SUZUKI TYPE COMMON FIXED POINT THEOREMS AND APPLICATIONS

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Abstract. Common fixed point theorems for Suzuki type conditions for a pair of maps on a metric space are obtained. Existence of a common solution for a class of functional equations arising in dynamic programming is also discussed.
Key Words and Phrases: Fixed point; Banach contraction theorem, functional equations, dynamic programming.
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