

## THE FIXED POINT PROPERTY FOR SOME GENERALIZED NONEXPANSIVE MAPPINGS IN A NONREFLEXIVE BANACH SPACE

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**Abstract.** The space  $\ell_1$  can be equivalently renormed to enjoy the fixed point property for a large class of generalized nonexpansive mappings.

**Key Words and Phrases:** Fixed point, generalized nonexpansive mappings, nonreflexive Banach space.

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