ITERATES OF BERNSTEIN TYPE OPERATORS ON A SQUARE WITH ONE CURVED SIDE VIA CONTRACTION PRINCIPLE

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Abstract. Given a function defined on a square with one curved side, we consider some Bernstein-type operators as well as their product and Boolean sum. Using the weakly Picard operators technique and the contraction principle, we study the convergence of the iterates of these operators.
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