

CARISTI'S TYPE MAPPINGS ON COMPLETE PARTIAL METRIC SPACES

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Abstract. We introduce a new type of Caristi's mapping on partial metric spaces and show that a partial metric space is complete if and only if every Caristi mapping has a fixed point. From this result we deduce a characterization of bicomplete weightable quasi-metric spaces. Several illustrative examples are given.

Key Words and Phrases: Fixed point, complete partial metric space, Caristi's type mapping.

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