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ULAM-HYERS STABILITY OF OPERATORIAL INCLUSIONS IN COMPLETE GAUGE SPACES

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Abstract. Using the weakly Picard operator technique, we will present some Ulam-Hyers stability results for operatorial inclusions using the weakly Picard operator technique. We study the Ulam-Hyers stability of some inclusions, where the multivalued operator satisfies some contraction conditions. We also give an application to integral inclusion.
Key Words and Phrases: Ulam-Hyers stability, multivalued operator, weakly Picard operator, c-weakly Picard operator, fixed point, integral inclusion.
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