

P-CONVEXITY AND PROPERTIES IMPLYING THE FIXED POINT PROPERTY

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Abstract. We show that several properties implying the FPP do not follow from P-convexity.

Key Words and Phrases: P-convexity, normal structure, coefficient $MW(X)$, Kadec-Klee property, property (S).

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