EXISTENCE OF SOLUTIONS OF A NONLINEAR THIRD ORDER BOUNDARY VALUE PROBLEM

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Abstract. This paper deals with a third-order three-point boundary value problem. Applying the Banach contraction principle and Leray Schauder nonlinear alternative, we establish the existence of solutions for the considered problem.
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