

ON CERTAIN STABILITY RESULTS OF BARBET AND NACHI

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Abstract. Stability results for a sequence of mappings in a Hausdorff uniform space are proved. The results obtained here are the generalizations of the recent results of Barbet and Nachi.

Key Words and Phrases: Fixed points, stability, Hausdorff, uniform space.

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