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A TOPOLOGICAL PROPERTY OF THE COMMON FIXED POINTS SET OF TWO MULTIVALUED OPERATORS SATISFYING A LATIF-BEG TYPE CONDITION

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Abstract. Let X be a nonempty, closed and convex subset of a Banach space. We prove that the common fixed points set of two lower semicontinuous multivalued operators defined on X with values in the set of all nonempty, closed and convex subsets of X, which satisfy a contraction type condition of Latif-Beg type, is an absolute retract for paracompact spaces. We also present a result regarding the common fixed points set for two multivalued operators satisfying a Latif-Beg type condition, using the notion of selection property.
Key Words and Phrases: multivalued operator, fixed point, common fixed point, absolute retract, selection property.
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