

## GENERAL ITERATION SCHEME WITH PERTURBED MAPPING FOR COMMON FIXED POINTS OF A FINITE FAMILY OF NONEXPANSIVE MAPPINGS

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**Abstract.** A new general composite implicit random iteration scheme with perturbed mapping is proposed and obtain necessary and sufficient conditions for strong convergence of proposed iteration scheme to random fixed point of a finite family of random nonexpansive mappings are obtained.

**Key Words and Phrases:** General iteration scheme;, nonexpansive random operator, fixed point, perturbed mapping.

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