Fixed Point Theory, Volume 9, No. 1, 2008, 351-362
http://www.math.ubbcluj.ro/~nodeacj/sfptcj.html

ITERATION PROCESS WITH ERRORS FOR LOCAL STRONGLY H-ACCRETIVE TYPE MAPPINGS

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Abstract. Some iteration processes of Mann and Ishikawa type with error has been discussed to approximate solution of equation $Tx = f$, where T is locally strongly H - accretive mapping [18] on uniformly smooth Banach space X. This extends an earlier result of Liu [9] on iterative processes with errors. We also extend a result of Weng [20] on iterative processes of dissipative type mappings.

Key Words and Phrases: Mann iteration process, Ishikawa iteration process, strictly pseudo-contractive map, local strongly H-accretive map, accretive map,strongly accretive map.

2000 Mathematics Subject Classification: 47H10, 54H25.

Acknowledgement. The authors are thankful to Prof. S.P. Singh for his valuable suggestions to improve the results.

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Received: November 10, 2007; Accepted: January 21, 2008.