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FIXED POINT THEOREMS ON CARTESIAN PRODUCT

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Abstract. In this paper we study the existence of the fixed point for operators on cartesian product $f : X \times Y \to X \times Y$, $f = (f_1, f_2)$, in terms of the operators $f_1(\cdot, y) : X \to X$ and $f_2(x, \cdot) : Y \to Y$.

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