

A NOTE ON RAKOTCH CONTRACTIONS

SIMEON REICH* AND ALEXANDER J. ZASLAVSKI**

*Department of Mathematics
The Technion-Israel Institute of Technology
32000 Haifa, Israel
E-mail: sreich@tx.technion.ac.il

**Department of Mathematics
The Technion-Israel Institute of Technology
32000 Haifa, Israel
E-mail: ajzasl@tx.technion.ac.il

Abstract. We establish fixed point and convergence theorems for certain mappings of contractive type which take a closed subset of a complete metric space X into X .

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