

## MULTIPLICITY RESULTS FOR A DISCRETE BOUNDARY VALUE PROBLEM VIA CRITICAL POINT THEORY

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**Abstract.** This paper is a survey on some recent multiplicity results, contained in [11], for a discrete boundary value problem involving the  $p$ -Laplacian via critical point theory. An overview on the abstract critical points results used to obtain them it is also given.

**Key Words and Phrases:** Difference equations, critical point theory, nonlinear boundary value problems.

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