

THREE EXAMPLES IN METRIC FIXED POINT THEORY

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Dedicated to Professor Ioan A. Rus on the occasion of his 70th birthday

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Abstract. We present three examples concerning the relations between various classes of mappings of contractive type defined on complete metric spaces.

Key Words and Phrases: complete metric space, contractive mapping, fixed point, iteration, nonexpansive mapping, strict contraction.

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