

ARONSZAJN TYPE THEOREMS FOR INTEGRAL EQUATIONS ON UNBOUNDED DOMAINS VIA MAXIMAL SOLUTIONS

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Dedicated to Professor Ioan A. Rus on the occasion of his 70th birthday

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Abstract. This paper discusses the topological structure of the solution set of a general Volterra integral equation. Under natural conditions we show that the solution set is an R_δ set.

Key Words and Phrases: Volterra integral equation, solution set, R_δ set.

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