

## MSC2010: Final Public Draft (Nov. 2008)

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This document is the Final Public Working Draft of MSC2010 produced jointly by the editorial staffs of Mathematical Reviews (MR) and Zentralblatt für Mathematik (Zbl) in consultation with the mathematical community. The goals of this revision of the Mathematics Subject Classification (MSC) were set out in the announcement of it and call for comments by the Executive Editor of MR and the Chief Editor of Zbl.

Publication as a Working Draft does not imply endorsement by MR and Zbl, though this is a final draft and, except for small unintended errors which will be corrected, is expected to be adopted. This is a **draft** document and may be updated, replaced or made obsolete by other documents. **It is inappropriate to cite this document as other than a work in progress.**

The deadline for finishing a production version of the MSC2010 has passed. The editors of MR and Zbl preparing this revision therefore ask for feedback and suggestions to help remove any obvious errors in this work, which should be given, preferably, on the Web site at <http://MSC2010.org> or, if the internet is not available, through e-mail to [feedback@MSC2010.org](mailto:feedback@MSC2010.org). They are grateful for the many suggestions that were received previously.

### How to use the Mathematics Subject Classification [MSC]

The main purpose of the classification of items in the mathematical literature using the Mathematics Subject Classification scheme is to help users find the items of present or potential interest to them as readily as possible—in products derived from the Mathematical Reviews Database (MRDB), in Zentralblatt MATH, or anywhere else where this classification scheme is used. An item in the mathematical literature should be classified so as to attract the attention of all those possibly interested in it. The item may be something which falls squarely within one clear area of the MSC, or it may involve several areas. Ideally, the MSC codes attached to an item should represent the subjects to which the item contains a contribution. The classification should serve both those closely concerned with specific subject areas, and those familiar enough with subjects to apply their results and methods elsewhere, inside or outside of mathematics. It will be extremely useful for both users and classifiers to familiarize themselves with the entire classification system and thus to become aware of all the classifications of possible interest to them.

Every item in the MRDB receives precisely one *primary* classification, which is simply the MSC code that describes its principal contribution. When an item contains several principal contributions to different areas, the primary classification should cover the most important among them. A paper or book may be assigned one or several secondary classification numbers to cover any remaining principal contributions, ancillary results, motivation or origin of the matters discussed, intended or potential field of application, or other significant aspects worthy of notice.

The principal contribution is meant to be the one including the most important part of the work actually done in the item. For example, a paper whose main overall content is the solution of a problem in graph theory, which arose in computer science and whose solution is (perhaps) at present only of interest to computer scientists, would have a primary classification in 05C (Graph Theory) with one or more secondary classifications in 68 (Computer Science); conversely, a paper whose overall content lies mainly in computer science should receive a primary

classification in 68, even if it makes heavy use of graph theory and proves several new graph-theoretic results along the way.

There are two types of cross-references given at the end of many of the entries in the MSC. The first type is in braces: “{For A, see X}”; if this appears in section Y, it means that contributions described by A should usually be assigned the classification code X, not Y. The other type of cross-reference merely points out related classifications; it is in brackets: “[See also ...]”, “[See mainly ...]”, etc., and the classification codes listed in the brackets may, but need not, be included in the classification codes of a paper, or they may be used in place of the classification where the cross-reference is given. The classifier must judge which classification is the most appropriate for the paper at hand.

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### **00–XX GENERAL**

- 00–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 00–02 Research exposition (monographs, survey articles)
- 00Axx General and miscellaneous specific topics**
- 00A05 General mathematics
- 00A06 Mathematics for nonmathematicians (engineering, social sciences, etc.)
- 00A07 Problem books
- 00A08 Recreational mathematics [See also 97A20]
- 00A09 Popularization of mathematics
- 00A15 Bibliographies
- 00A17 External book reviews
- 00A20 Dictionaries and other general reference works
- 00A22 Formularies
- 00A30 Philosophy of mathematics [See also 03A05]
- 00A35 Methodology of mathematics, didactics [See also 97Cxx, 97Dxx]
- 00A65 Mathematics and music
- 00A66 Mathematics and visual arts, visualization
- 00A67 Mathematics and architecture
- 00A69 General applied mathematics  $\{\{\}\}$ For physics, see 00A79 and Sections 70 through 86
- 00A71 Theory of mathematical modeling
- 00A72 General methods of simulation
- 00A73 Dimensional analysis
- 00A79 Physics (use more specific entries from Sections 70 through 86 when possible)
- 00A99 Miscellaneous topics
- 00Bxx Conference proceedings and collections of papers**
- 00B05 Collections of abstracts of lectures
- 00B10 Collections of articles of general interest
- 00B15 Collections of articles of miscellaneous specific content
- 00B20 Proceedings of conferences of general interest
- 00B25 Proceedings of conferences of miscellaneous specific interest
- 00B30 Festschriften
- 00B50 Volumes of selected translations
- 00B55 Miscellaneous volumes of translations
- 00B60 Collections of reprinted articles [See also 01A75]
- 00B99 None of the above, but in this section

### **01–XX HISTORY AND BIOGRAPHY [See also the classification number –03 in the other sections]**

- 01–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 01–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 01–02 Research exposition (monographs, survey articles)
- 01–06 Proceedings, conferences, collections, etc.
- 01–08 Computational methods
- 01Axx History of mathematics and mathematicians**
- 01A05 General histories, source books
- 01A07 Ethnomathematics, general
- 01A10 Paleolithic, Neolithic

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- 01A12 Indigenous cultures of the Americas
- 01A13 Other indigenous cultures (non-European)
- 01A15 Indigenous European cultures (pre-Greek, etc.)
- 01A16 Egyptian
- 01A17 Babylonian
- 01A20 Greek, Roman
- 01A25 China
- 01A27 Japan
- 01A29 Southeast Asia
- 01A30 Islam (Medieval)
- 01A32 India
- 01A35 Medieval
- 01A40 15th and 16th centuries, Renaissance
- 01A45 17th century
- 01A50 18th century
- 01A55 19th century
- 01A60 20th century
- 01A61 Twenty-first century
- 01A65 Contemporary
- 01A67 Future prospectives
- 01A70 Biographies, obituaries, personalia, bibliographies
- 01A72 Schools of mathematics
- 01A73 Universities
- 01A74 Other institutions and academies
- 01A75 Collected or selected works; reprintings or translations of classics  
[See also 00B60]
- 01A80 Sociology (and profession) of mathematics
- 01A85 Historiography
- 01A90 Bibliographic studies
- 01A99 Miscellaneous topics
- 03–XX MATHEMATICAL LOGIC AND FOUNDATIONS**
- 03–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 03–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 03–02 Research exposition (monographs, survey articles)
- 03–03 Historical (must also be assigned at least one classification number from Section 01)
- 03–04 Explicit machine computation and programs (not the theory of computation or programming)
- 03–06 Proceedings, conferences, collections, etc.
- 03Axx Philosophical aspects of logic and foundations**
- 03A05 Philosophical and critical  $\{\{\}$ For philosophy of mathematics, see also 00A30
- 03A10 Logic in the philosophy of science
- 03A99 None of the above, but in this section
- 03Bxx General logic**
- 03B05 Classical propositional logic
- 03B10 Classical first-order logic
- 03B15 Higher-order logic and type theory
- 03B20 Subsystems of classical logic (including intuitionistic logic)
- 03B22 Abstract deductive systems

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- 03B25 Decidability of theories and sets of sentences [See also 11U05, 12L05, 20F10]
- 03B30 Foundations of classical theories (including reverse mathematics) [See also 03F35]
- 03B35 Mechanization of proofs and logical operations [See also 68T15]
- 03B40 Combinatory logic and lambda-calculus [See also 68N18]
- 03B42 Logics of knowledge and belief (including belief change)
- 03B44 Temporal logic
- 03B45 Modal logic (including the logic of norms)  $\{\{\}\}$ For knowledge and belief, see 03B42; for temporal logic, see 03B44; for provability logic, see also 03F45
- 03B47 Substructural logics (including relevance, entailment, linear logic, Lambek calculus, BCK and BCI logics)  $\{\{\}\}$ For proof-theoretic aspects see 03F52
- 03B48 Probability and inductive logic [See also 60A05]
- 03B50 Many-valued logic
- 03B52 Fuzzy logic; logic of vagueness [See also 68T27, 68T37, 94D05]
- 03B53 Paraconsistent logics
- 03B55 Intermediate logics
- 03B60 Other nonclassical logic
- 03B62 Combined logics
- 03B65 Logic of natural languages [See also 68T50, 91F20]
- 03B70 Logic in computer science [See also 68-XX]
- 03B80 Other applications of logic
- 03B99 None of the above, but in this section
- 03Cxx Model theory**
- 03C05 Equational classes, universal algebra [See also 08Axx, 08Bxx, 18C05]
- 03C07 Basic properties of first-order languages and structures
- 03C10 Quantifier elimination, model completeness and related topics
- 03C13 Finite structures [See also 68Q15, 68Q19]
- 03C15 Denumerable structures
- 03C20 Ultraproducts and related constructions
- 03C25 Model-theoretic forcing
- 03C30 Other model constructions
- 03C35 Categoricity and completeness of theories
- 03C40 Interpolation, preservation, definability
- 03C45 Classification theory, stability and related concepts [See also 03C48]
- 03C48 Abstract elementary classes and related topics [See also 03C45]
- 03C50 Models with special properties (saturated, rigid, etc.)
- 03C52 Properties of classes of models
- 03C55 Set-theoretic model theory
- 03C57 Effective and recursion-theoretic model theory [See also 03D45]
- 03C60 Model-theoretic algebra [See also 08C10, 12Lxx, 13L05]
- 03C62 Models of arithmetic and set theory [See also 03Hxx]
- 03C64 Model theory of ordered structures; o-minimality
- 03C65 Models of other mathematical theories
- 03C68 Other classical first-order model theory
- 03C70 Logic on admissible sets
- 03C75 Other infinitary logic
- 03C80 Logic with extra quantifiers and operators [See also 03B42, 03B44, 03B45, 03B48]

- 03C85 Second- and higher-order model theory
- 03C90 Nonclassical models (Boolean-valued, sheaf, etc.)
- 03C95 Abstract model theory
- 03C98 Applications of model theory [See also 03C60]
- 03C99 None of the above, but in this section
- 03Dxx Computability and recursion theory**
- 03D03 Thue and Post systems, etc.
- 03D05 Automata and formal grammars in connection with logical questions  
[See also 68Q45, 68Q70, 68R15]
- 03D10 Turing machines and related notions [See also 68Q05]
- 03D15 Complexity of computation (including implicit computational  
complexity) [See also 68Q15, 68Q17]
- 03D20 Recursive functions and relations, subrecursive hierarchies
- 03D25 Recursively (computably) enumerable sets and degrees
- 03D28 Other Turing degree structures
- 03D30 Other degrees and reducibilities
- 03D32 Algorithmic randomness and dimension [See also 68Q30]
- 03D35 Undecidability and degrees of sets of sentences
- 03D40 Word problems, etc. [See also 06B25, 08A50, 20F10, 68R15]
- 03D45 Theory of numerations, effectively presented structures  
[See also 03C57; for intuitionistic and similar approaches see 03F55]
- 03D50 Recursive equivalence types of sets and structures, isols
- 03D55 Hierarchies
- 03D60 Computability and recursion theory on ordinals, admissible sets, etc.
- 03D65 Higher-type and set recursion theory
- 03D70 Inductive definability
- 03D75 Abstract and axiomatic computability and recursion theory
- 03D78 Computation over the reals  $\{\{\}\}$  For constructive aspects, see 03F60
- 03D80 Applications of computability and recursion theory
- 03D99 None of the above, but in this section
- 03Exx Set theory**
- 03E02 Partition relations
- 03E04 Ordered sets and their cofinalities; pcf theory
- 03E05 Other combinatorial set theory
- 03E10 Ordinal and cardinal numbers
- 03E15 Descriptive set theory [See also 28A05, 54H05]
- 03E17 Cardinal characteristics of the continuum
- 03E20 Other classical set theory (including functions, relations, and set  
algebra)
- 03E25 Axiom of choice and related propositions
- 03E30 Axiomatics of classical set theory and its fragments
- 03E35 Consistency and independence results
- 03E40 Other aspects of forcing and Boolean-valued models
- 03E45 Inner models, including constructibility, ordinal definability, and core  
models
- 03E47 Other notions of set-theoretic definability
- 03E50 Continuum hypothesis and Martin's axiom [See also 03E57]
- 03E55 Large cardinals
- 03E57 Generic absoluteness and forcing axioms [See also 03E50]
- 03E60 Determinacy principles
- 03E65 Other hypotheses and axioms

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- 03E70 Nonclassical and second-order set theories
- 03E72 Fuzzy set theory
- 03E75 Applications of set theory
- 03E99 None of the above, but in this section
- 03Fxx Proof theory and constructive mathematics**
- 03F03 Proof theory, general
- 03F05 Cut-elimination and normal-form theorems
- 03F07 Structure of proofs
- 03F10 Functionals in proof theory
- 03F15 Recursive ordinals and ordinal notations
- 03F20 Complexity of proofs
- 03F25 Relative consistency and interpretations
- 03F30 First-order arithmetic and fragments
- 03F35 Second- and higher-order arithmetic and fragments [See also 03B30]
- 03F40 Gödel numberings and issues of incompleteness
- 03F45 Provability logics and related algebras (e.g., diagonalizable algebras) [See also 03B45, 03G25, 06E25]
- 03F50 Metamathematics of constructive systems
- 03F52 Linear logic and other substructural logics [See also 03B47]
- 03F55 Intuitionistic mathematics
- 03F60 Constructive and recursive analysis [See also 03B30, 03D45, 03D78, 26E40, 46S30, 47S30]
- 03F65 Other constructive mathematics [See also 03D45]
- 03F99 None of the above, but in this section
- 03Gxx Algebraic logic**
- 03G05 Boolean algebras [See also 06Exx]
- 03G10 Lattices and related structures [See also 06Bxx]
- 03G12 Quantum logic [See also 06C15, 81P10]
- 03G15 Cylindric and polyadic algebras; relation algebras
- 03G20 Lukasiewicz and Post algebras [See also 06D25, 06D30]
- 03G25 Other algebras related to logic [See also 03F45, 06D20, 06E25, 06F35]
- 03G27 Abstract algebraic logic
- 03G30 Categorical logic, topoi [See also 18B25, 18C05, 18C10]
- 03G99 None of the above, but in this section
- 03Hxx Nonstandard models [See also 03C62]**
- 03H05 Nonstandard models in mathematics [See also 26E35, 28E05, 30G06, 46S20, 47S20, 54J05]
- 03H10 Other applications of nonstandard models (economics, physics, etc.)
- 03H15 Nonstandard models of arithmetic [See also 11U10, 12L15, 13L05]
- 03H99 None of the above, but in this section
- 05–XX COMBINATORICS FOR FINITE FIELDS, SEE 11TXX{}**
- 05–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 05–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 05–02 Research exposition (monographs, survey articles)
- 05–03 Historical (must also be assigned at least one classification number from Section 01)
- 05–04 Explicit machine computation and programs (not the theory of computation or programming)
- 05–06 Proceedings, conferences, collections, etc.

- 05Axx** **Enumerative combinatorics** {For enumeration in graph theory, see **05C30**}
- 05A05 Permutations, words, matrices
- 05A10 Factorials, binomial coefficients, combinatorial functions  
[See also 11B65, 33Cxx]
- 05A15 Exact enumeration problems, generating functions [See also 33Cxx, 33Dxx]
- 05A16 Asymptotic enumeration
- 05A17 Partitions of integers [See also 11P81, 11P82, 11P83]
- 05A18 Partitions of sets
- 05A19 Combinatorial identities, bijective combinatorics
- 05A20 Combinatorial inequalities
- 05A30  $q$ -calculus and related topics [See also 33Dxx]
- 05A40 Umbral calculus
- 05A99 None of the above, but in this section
- 05Bxx** **Designs and configurations** {{{}}For applications of design theory, see **94C30**
- 05B05 Block designs [See also 51E05, 62K10]
- 05B07 Triple systems
- 05B10 Difference sets (number-theoretic, group-theoretic, etc.)  
[See also 11B13]
- 05B15 Orthogonal arrays, Latin squares, Room squares
- 05B20 Matrices (incidence, Hadamard, etc.)
- 05B25 Finite geometries [See also 51D20, 51Exx]
- 05B30 Other designs, configurations [See also 51E30]
- 05B35 Matroids, geometric lattices [See also 52B40, 90C27]
- 05B40 Packing and covering [See also 11H31, 52C15, 52C17]
- 05B45 Tessellation and tiling problems [See also 52C20, 52C22]
- 05B50 Polyominoes
- 05B99 None of the above, but in this section
- 05Cxx** **Graph theory** {{{}}For applications of graphs, see **68R10, 81Q30, 81T15, 82B20, 82C20, 90C35, 92E10, 94C15**
- 05C05 Trees
- 05C07 Vertex degrees [See also 05E30]
- 05C10 Planar graphs; geometric and topological aspects of graph theory  
[See also 57M15, 57M25]
- 05C12 Distance in graphs
- 05C15 Coloring of graphs and hypergraphs
- 05C17 Perfect graphs
- 05C20 Directed graphs (digraphs), tournaments
- 05C21 Flows in graphs
- 05C22 Signed and weighted graphs
- 05C25 Graphs and abstract algebra (groups, rings, fields, etc.)  
[See also 20F65]
- 05C30 Enumeration in graph theory
- 05C31 Graph polynomials
- 05C35 Extremal problems [See also 90C35]
- 05C38 Paths and cycles [See also 90B10]
- 05C40 Connectivity
- 05C42 Density (toughness, etc.)
- 05C45 Eulerian and Hamiltonian graphs

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- 05C50 Graphs and linear algebra (matrices, eigenvalues, etc.)
- 05C51 Graph designs and isomomorphic decomposition [See also 05B30]
- 05C55 Generalized Ramsey theory [See also 05D10]
- 05C57 Games on graphs [See also 91A43, 91A46]
- 05C60 Isomorphism problems (reconstruction conjecture, etc.) and homomorphisms (subgraph embedding, etc.)
- 05C62 Graph representations (geometric and intersection representations, etc.) {For graph drawing, see also 68R10}
- 05C63 Infinite graphs
- 05C65 Hypergraphs
- 05C69 Dominating sets, independent sets, cliques
- 05C70 Factorization, matching, partitioning, covering and packing
- 05C72 Fractional graph theory, fuzzy graph theory
- 05C75 Structural characterization of families of graphs
- 05C76 Graph operations (line graphs, products, etc.)
- 05C78 Graph labelling (graceful graphs, bandwidth, etc.)
- 05C80 Random graphs [See also 60B20]
- 05C81 Random walks on graphs
- 05C82 Small world graphs, complex networks [See also 90Bxx, 91D30]
- 05C83 Graph minors
- 05C85 Graph algorithms [See also 68R10, 68W05]
- 05C90 Applications [See also 68R10, 81Q30, 81T15, 82B20, 82C20, 90C35, 92E10, 94C15]
- 05C99 None of the above, but in this section
- 05Dxx Extremal combinatorics**
- 05D05 Extremal set theory
- 05D10 Ramsey theory [See also 05C55]
- 05D15 Transversal (matching) theory
- 05D40 Probabilistic methods
- 05D99 None of the above, but in this section
- 05Exx Algebraic combinatorics**
- 05E05 Symmetric functions and generalizations
- 05E10 Combinatorial aspects of representation theory [See also 20C30]
- 05E15 Combinatorial aspects of groups and algebras [See also 14Nxx, 22E45, 33C80]
- 05E18 Group actions on combinatorial structures
- 05E30 Association schemes, strongly regular graphs
- 05E40 Combinatorial aspects of commutative algebra
- 05E45 Combinatorial aspects of simplicial complexes
- 05E99 None of the above, but in this section
- 06–XX ORDER, LATTICES, ORDERED ALGEBRAIC STRUCTURES**  
[See also 18B35]
- 06–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 06–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 06–02 Research exposition (monographs, survey articles)
- 06–03 Historical (must also be assigned at least one classification number from Section 01)
- 06–04 Explicit machine computation and programs (not the theory of computation or programming)
- 06–06 Proceedings, conferences, collections, etc.

- 06Axx**    **Ordered sets**
- 06A05    Total order
- 06A06    Partial order, general
- 06A07    Combinatorics of partially ordered sets
- 06A11    Algebraic aspects of posets
- 06A12    Semilattices [See also 20M10; for topological semilattices see 22A26]
- 06A15    Galois correspondences, closure operators
- 06A75    Generalizations of ordered sets
- 06A99    None of the above, but in this section
- 06Bxx**    **Lattices [See also 03G10]**
- 06B05    Structure theory
- 06B10    Ideals, congruence relations
- 06B15    Representation theory
- 06B20    Varieties of lattices
- 06B23    Complete lattices, completions
- 06B25    Free lattices, projective lattices, word problems [See also 03D40, 08A50, 20F10]
- 06B30    Topological lattices, order topologies [See also 06F30, 22A26, 54F05, 54H12]
- 06B35    Continuous lattices and posets, applications [See also 06B30, 06D10, 06F30, 18B35, 22A26, 68Q55]
- 06B75    Generalizations of lattices
- 06B99    None of the above, but in this section
- 06Cxx**    **Modular lattices, complemented lattices**
- 06C05    Modular lattices, Desarguesian lattices
- 06C10    Semimodular lattices, geometric lattices
- 06C15    Complemented lattices, orthocomplemented lattices and posets [See also 03G12, 81P10]
- 06C20    Complemented modular lattices, continuous geometries
- 06C99    None of the above, but in this section
- 06Dxx**    **Distributive lattices**
- 06D05    Structure and representation theory
- 06D10    Complete distributivity
- 06D15    Pseudocomplemented lattices
- 06D20    Heyting algebras [See also 03G25]
- 06D22    Frames, locales  $\{\{\}\}$  For topological questions see 54–XX
- 06D25    Post algebras [See also 03G20]
- 06D30    De Morgan algebras, Łukasiewicz algebras [See also 03G20]
- 06D35    MV-algebras
- 06D50    Lattices and duality
- 06D72    Fuzzy lattices (soft algebras) and related topics
- 06D75    Other generalizations of distributive lattices
- 06D99    None of the above, but in this section
- 06Exx**    **Boolean algebras (Boolean rings) [See also 03G05]**
- 06E05    Structure theory
- 06E10    Chain conditions, complete algebras
- 06E15    Stone spaces (Boolean spaces) and related structures
- 06E20    Ring-theoretic properties [See also 16E50, 16G30]
- 06E25    Boolean algebras with additional operations (diagonalizable algebras, etc.) [See also 03G25, 03F45]
- 06E30    Boolean functions [See also 94C10]

- 06E75 Generalizations of Boolean algebras
- 06E99 None of the above, but in this section
- 06Fxx Ordered structures**
- 06F05 Ordered semigroups and monoids [See also 20Mxx]
- 06F07 Quantales
- 06F10 Noether lattices
- 06F15 Ordered groups [See also 20F60]
- 06F20 Ordered abelian groups, Riesz groups, ordered linear spaces  
[See also 46A40]
- 06F25 Ordered rings, algebras, modules  $\{\{\}\}$  For ordered fields, see 12J15;  
see also 13J25, 16W80
- 06F30 Topological lattices, order topologies [See also 06B30, 22A26, 54F05,  
54H12]
- 06F35 BCK-algebras, BCI-algebras [See also 03G25]
- 06F99 None of the above, but in this section
- 08–XX GENERAL ALGEBRAIC SYSTEMS**
- 08–00 General reference works (handbooks, dictionaries, bibliographies,  
etc.)
- 08–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 08–02 Research exposition (monographs, survey articles)
- 08–03 Historical (must also be assigned at least one classification number  
from Section 01)
- 08–04 Explicit machine computation and programs (not the theory of  
computation or programming)
- 08–06 Proceedings, conferences, collections, etc.
- 08Axx Algebraic structures [See also 03C05]**
- 08A02 Relational systems, laws of composition
- 08A05 Structure theory
- 08A30 Subalgebras, congruence relations
- 08A35 Automorphisms, endomorphisms
- 08A40 Operations, polynomials, primal algebras
- 08A45 Equational compactness
- 08A50 Word problems [See also 03D40, 06B25, 20F10, 68R15]
- 08A55 Partial algebras
- 08A60 Unary algebras
- 08A62 Finitary algebras
- 08A65 Infinitary algebras
- 08A68 Heterogeneous algebras
- 08A70 Applications of universal algebra in computer science
- 08A72 Fuzzy algebraic structures
- 08A99 None of the above, but in this section
- 08Bxx Varieties [See also 03C05]**
- 08B05 Equational logic, Mal'cev (Mal'tsev) conditions
- 08B10 Congruence modularity, congruence distributivity
- 08B15 Lattices of varieties
- 08B20 Free algebras
- 08B25 Products, amalgamated products, and other kinds of limits and  
colimits [See also 18A30]
- 08B26 Subdirect products and subdirect irreducibility
- 08B30 Injectives, projectives
- 08B99 None of the above, but in this section

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- 08Cxx Other classes of algebras**
- 08C05 Categories of algebras [See also 18C05]
- 08C10 Axiomatic model classes [See also 03Cxx, in particular 03C60]
- 08C15 Quasivarieties
- 08C20 Natural dualities for classes of algebras [See also 06E15, 18A40, 22A30]
- 08C99 None of the above, but in this section
- 11–XX NUMBER THEORY**
- 11–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 11–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 11–02 Research exposition (monographs, survey articles)
- 11–03 Historical (must also be assigned at least one classification number from Section 01)
- 11–04 Explicit machine computation and programs (not the theory of computation or programming)
- 11–06 Proceedings, conferences, collections, etc.
- 11Axx Elementary number theory  $\{\{\}\}$ For analogues in number fields, see 11R04**
- 11A05 Multiplicative structure; Euclidean algorithm; greatest common divisors
- 11A07 Congruences; primitive roots; residue systems
- 11A15 Power residues, reciprocity
- 11A25 Arithmetic functions; related numbers; inversion formulas
- 11A41 Primes
- 11A51 Factorization; primality
- 11A55 Continued fractions  $\{\{\}\}$ For approximation results, see 11J70 [See also 11K50, 30B70, 40A15]
- 11A63 Radix representation; digital problems  $\{\{\}\}$ For metric results, see 11K16
- 11A67 Other representations
- 11A99 None of the above, but in this section
- 11Bxx Sequences and sets**
- 11B05 Density, gaps, topology
- 11B13 Additive bases, including sumsets [See also 05B10]
- 11B25 Arithmetic progressions [See also 11N13]
- 11B30 Arithmetic combinatorics; higher degree uniformity
- 11B34 Representation functions
- 11B37 Recurrences  $\{\{\}\}$ For applications to special functions, see 33–XX
- 11B39 Fibonacci and Lucas numbers and polynomials and generalizations
- 11B50 Sequences (mod  $m$ )
- 11B57 Farey sequences; the sequences  $1^k, 2^k, \dots$
- 11B65 Binomial coefficients; factorials;  $q$ -identities [See also 05A10, 05A30]
- 11B68 Bernoulli and Euler numbers and polynomials
- 11B73 Bell and Stirling numbers
- 11B75 Other combinatorial number theory
- 11B83 Special sequences and polynomials
- 11B85 Automata sequences
- 11B99 None of the above, but in this section

- 11Cxx Polynomials and matrices**
- 11C08 Polynomials [See also 13F20]
- 11C20 Matrices, determinants [See also 15B36]
- 11C99 None of the above, but in this section
- 11Dxx Diophantine equations [See also 11Gxx, 14Gxx]**
- 11D04 Linear equations
- 11D07 The Frobenius problem
- 11D09 Quadratic and bilinear equations
- 11D25 Cubic and quartic equations
- 11D41 Higher degree equations; Fermat's equation
- 11D45 Counting solutions of Diophantine equations
- 11D57 Multiplicative and norm form equations
- 11D59 Thue-Mahler equations
- 11D61 Exponential equations
- 11D68 Rational numbers as sums of fractions
- 11D72 Equations in many variables [See also 11P55]
- 11D75 Diophantine inequalities [See also 11J25]
- 11D79 Congruences in many variables
- 11D85 Representation problems [See also 11P55]
- 11D88  $p$ -adic and power series fields
- 11D99 None of the above, but in this section
- 11Exx Forms and linear algebraic groups [See also 19Gxx] {{{}}For quadratic forms in linear algebra, see 15A63**
- 11E04 Quadratic forms over general fields
- 11E08 Quadratic forms over local rings and fields
- 11E10 Forms over real fields
- 11E12 Quadratic forms over global rings and fields
- 11E16 General binary quadratic forms
- 11E20 General ternary and quaternary quadratic forms; forms of more than two variables
- 11E25 Sums of squares and representations by other particular quadratic forms
- 11E39 Bilinear and Hermitian forms
- 11E41 Class numbers of quadratic and Hermitian forms
- 11E45 Analytic theory (Epstein zeta functions; relations with automorphic forms and functions)
- 11E57 Classical groups [See also 14Lxx, 20Gxx]
- 11E70  $K$ -theory of quadratic and Hermitian forms
- 11E72 Galois cohomology of linear algebraic groups [See also 20G10]
- 11E76 Forms of degree higher than two
- 11E81 Algebraic theory of quadratic forms; Witt groups and rings [See also 19G12, 19G24]
- 11E88 Quadratic spaces; Clifford algebras [See also 15A63, 15A66]
- 11E95  $p$ -adic theory
- 11E99 None of the above, but in this section
- 11Fxx Discontinuous groups and automorphic forms [See also 11R39, 11S37, 14Gxx, 14Kxx, 22E50, 22E55, 30F35, 32Nxx] {{{}}For relations with quadratic forms, see 11E45**
- 11F03 Modular and automorphic functions
- 11F06 Structure of modular groups and generalizations; arithmetic groups [See also 20H05, 20H10, 22E40]

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- 11F11 Holomorphic modular forms of integral weight
- 11F12 Automorphic forms, one variable
- 11F20 Dedekind eta function, Dedekind sums
- 11F22 Relationship to Lie algebras and finite simple groups
- 11F23 Relations with algebraic geometry and topology
- 11F25 Hecke-Petersson operators, differential operators (one variable)
- 11F27 Theta series; Weil representation; theta correspondences
- 11F30 Fourier coefficients of automorphic forms
- 11F32 Modular correspondences, etc.
- 11F33 Congruences for modular and  $p$ -adic modular forms [See also 14G20, 22E50]
- 11F37 Forms of half-integer weight; nonholomorphic modular forms
- 11F41 Automorphic forms on  $GL(2)$ ; Hilbert and Hilbert-Siegel modular groups and their modular and automorphic forms; Hilbert modular surfaces [See also 14J20]
- 11F46 Siegel modular groups; Siegel and Hilbert-Siegel modular and automorphic forms
- 11F50 Jacobi forms
- 11F52 Modular forms associated to Drinfel'd modules
- 11F55 Other groups and their modular and automorphic forms (several variables)
- 11F60 Hecke-Petersson operators, differential operators (several variables)
- 11F66 Langlands  $L$ -functions; one variable Dirichlet series and functional equations
- 11F67 Special values of automorphic  $L$ -series, periods of modular forms, cohomology, modular symbols
- 11F68 Dirichlet series in several complex variables associated to automorphic forms; Weyl group multiple Dirichlet series
- 11F70 Representation-theoretic methods; automorphic representations over local and global fields
- 11F72 Spectral theory; Selberg trace formula
- 11F75 Cohomology of arithmetic groups
- 11F80 Galois representations
- 11F85  $p$ -adic theory, local fields [See also 14G20, 22E50]
- 11F99 None of the above, but in this section
- 11Gxx Arithmetic algebraic geometry (Diophantine geometry)**  
[See also 11Dxx, 14Gxx, 14Kxx]
- 11G05 Elliptic curves over global fields [See also 14H52]
- 11G07 Elliptic curves over local fields [See also 14G20, 14H52]
- 11G09 Drinfel'd modules; higher-dimensional motives, etc. [See also 14L05]
- 11G10 Abelian varieties of dimension  $> 1$  [See also 14Kxx]
- 11G15 Complex multiplication and moduli of abelian varieties  
[See also 14K22]
- 11G16 Elliptic and modular units [See also 11R27]
- 11G18 Arithmetic aspects of modular and Shimura varieties [See also 14G35]
- 11G20 Curves over finite and local fields [See also 14H25]
- 11G25 Varieties over finite and local fields [See also 14G15, 14G20]
- 11G30 Curves of arbitrary genus or genus  $\neq 1$  over global fields  
[See also 14H25]
- 11G32 Dessins d'enfants, Belyĭ theory
- 11G35 Varieties over global fields [See also 14G25]

- 11G40 *L*-functions of varieties over global fields; Birch-Swinnerton-Dyer conjecture [See also 14G10]
- 11G42 Arithmetic mirror symmetry [See also 14J33]
- 11G45 Geometric class field theory [See also 11R37, 14C35, 19F05]
- 11G50 Heights [See also 14G40, 37P30]
- 11G55 Polylogarithms and relations with *K*-theory
- 11G99 None of the above, but in this section
- 11Hxx** **Geometry of numbers** **{ }****For applications in coding theory, see 94B75**
- 11H06 Lattices and convex bodies [See also 11P21, 52C05, 52C07]
- 11H16 Nonconvex bodies
- 11H31 Lattice packing and covering [See also 05B40, 52C15, 52C17]
- 11H46 Products of linear forms
- 11H50 Minima of forms
- 11H55 Quadratic forms (reduction theory, extreme forms, etc.)
- 11H56 Automorphism groups of lattices
- 11H60 Mean value and transfer theorems
- 11H71 Relations with coding theory
- 11H99 None of the above, but in this section
- 11Jxx** **Diophantine approximation, transcendental number theory**  
**[See also 11K60]**
- 11J04 Homogeneous approximation to one number
- 11J06 Markov and Lagrange spectra and generalizations
- 11J13 Simultaneous homogeneous approximation, linear forms
- 11J17 Approximation by numbers from a fixed field
- 11J20 Inhomogeneous linear forms
- 11J25 Diophantine inequalities [See also 11D75]
- 11J54 Small fractional parts of polynomials and generalizations
- 11J61 Approximation in non-Archimedean valuations
- 11J68 Approximation to algebraic numbers
- 11J70 Continued fractions and generalizations [See also 11A55, 11K50]
- 11J71 Distribution modulo one [See also 11K06]
- 11J72 Irrationality; linear independence over a field
- 11J81 Transcendence (general theory)
- 11J82 Measures of irrationality and of transcendence
- 11J83 Metric theory
- 11J85 Algebraic independence; Gel'fond's method
- 11J86 Linear forms in logarithms; Baker's method
- 11J87 Schmidt Subspace Theorem and applications
- 11J89 Transcendence theory of elliptic and abelian functions
- 11J91 Transcendence theory of other special functions
- 11J93 Transcendence theory of Drinfel'd and *t*-modules
- 11J95 Results involving abelian varieties
- 11J97 Analogues of methods in Nevanlinna theory (work of Vojta et al.)
- 11J99 None of the above, but in this section
- 11Kxx** **Probabilistic theory: distribution modulo 1; metric theory of algorithms**
- 11K06 General theory of distribution modulo 1 [See also 11J71]
- 11K16 Normal numbers, radix expansions, Pisot numbers, Salem numbers, good lattice points, etc. [See also 11A63]
- 11K31 Special sequences

- 11K36 Well-distributed sequences and other variations
- 11K38 Irregularities of distribution, discrepancy [See also 11Nxx]
- 11K41 Continuous,  $p$ -adic and abstract analogues
- 11K45 Pseudo-random numbers; Monte Carlo methods
- 11K50 Metric theory of continued fractions [See also 11A55, 11J70]
- 11K55 Metric theory of other algorithms and expansions; measure and Hausdorff dimension [See also 11N99, 28Dxx]
- 11K60 Diophantine approximation [See also 11Jxx]
- 11K65 Arithmetic functions [See also 11Nxx]
- 11K70 Harmonic analysis and almost periodicity
- 11K99 None of the above, but in this section
- 11Lxx Exponential sums and character sums  $\{\{\}\}$  For finite fields, see 11Txx**
- 11L03 Trigonometric and exponential sums, general
- 11L05 Gauss and Kloosterman sums; generalizations
- 11L07 Estimates on exponential sums
- 11L10 Jacobsthal and Brewer sums; other complete character sums
- 11L15 Weyl sums
- 11L20 Sums over primes
- 11L26 Sums over arbitrary intervals
- 11L40 Estimates on character sums
- 11L99 None of the above, but in this section
- 11Mxx Zeta and  $L$ -functions: analytic theory**
- 11M06  $\zeta(s)$  and  $L(s, \chi)$
- 11M20 Real zeros of  $L(s, \chi)$ ; results on  $L(1, \chi)$
- 11M26 Nonreal zeros of  $\zeta(s)$  and  $L(s, \chi)$ ; Riemann and other hypotheses
- 11M32 Multiple Dirichlet series and zeta functions and multizeta values
- 11M35 Hurwitz and Lerch zeta functions
- 11M36 Selberg zeta functions and regularized determinants; applications to spectral theory, Dirichlet series, Eisenstein series, etc. Explicit formulas
- 11M38 Zeta and  $L$ -functions in characteristic  $p$
- 11M41 Other Dirichlet series and zeta functions  $\{\{\}\}$  For local and global ground fields, see 11R42, 11R52, 11S40, 11S45; for algebro-geometric methods, see 14G10; see also 11E45, 11F66, 11F70, 11F72
- 11M45 Tauberian theorems [See also 40E05]
- 11M50 Relations with random matrices
- 11M55 Relations with noncommutative geometry
- 11M99 None of the above, but in this section
- 11Nxx Multiplicative number theory**
- 11N05 Distribution of primes
- 11N13 Primes in progressions [See also 11B25]
- 11N25 Distribution of integers with specified multiplicative constraints
- 11N30 Turán theory [See also 30Bxx]
- 11N32 Primes represented by polynomials; other multiplicative structure of polynomial values
- 11N35 Sieves
- 11N36 Applications of sieve methods
- 11N37 Asymptotic results on arithmetic functions
- 11N45 Asymptotic results on counting functions for algebraic and topological structures
- 11N56 Rate of growth of arithmetic functions

- 11N60 Distribution functions associated with additive and positive multiplicative functions
- 11N64 Other results on the distribution of values or the characterization of arithmetic functions
- 11N69 Distribution of integers in special residue classes
- 11N75 Applications of automorphic functions and forms to multiplicative problems [See also 11Fxx]
- 11N80 Generalized primes and integers
- 11N99 None of the above, but in this section
- 11Pxx Additive number theory; partitions**
- 11P05 Waring's problem and variants
- 11P21 Lattice points in specified regions
- 11P32 Goldbach-type theorems; other additive questions involving primes
- 11P55 Applications of the Hardy-Littlewood method [See also 11D85]
- 11P70 Inverse problems of additive number theory, including sumsets
- 11P81 Elementary theory of partitions [See also 05A17]
- 11P82 Analytic theory of partitions
- 11P83 Partitions; congruences and congruential restrictions
- 11P84 Partition identities; identities of Rogers-Ramanujan type
- 11P99 None of the above, but in this section
- 11Rxx Algebraic number theory: global fields  $\{\{\}\}$  For complex multiplication, see 11G15**
- 11R04 Algebraic numbers; rings of algebraic integers
- 11R06 PV-numbers and generalizations; other special algebraic numbers; Mahler measure
- 11R09 Polynomials (irreducibility, etc.)
- 11R11 Quadratic extensions
- 11R16 Cubic and quartic extensions
- 11R18 Cyclotomic extensions
- 11R20 Other abelian and metabelian extensions
- 11R21 Other number fields
- 11R23 Iwasawa theory
- 11R27 Units and factorization
- 11R29 Class numbers, class groups, discriminants
- 11R32 Galois theory
- 11R33 Integral representations related to algebraic numbers; Galois module structure of rings of integers [See also 20C10]
- 11R34 Galois cohomology [See also 12Gxx, 19A31]
- 11R37 Class field theory
- 11R39 Langlands-Weil conjectures, nonabelian class field theory [See also 11Fxx, 22E55]
- 11R42 Zeta functions and  $L$ -functions of number fields [See also 11M41, 19F27]
- 11R44 Distribution of prime ideals [See also 11N05]
- 11R45 Density theorems
- 11R47 Other analytic theory [See also 11Nxx]
- 11R52 Quaternion and other division algebras: arithmetic, zeta functions
- 11R54 Other algebras and orders, and their zeta and  $L$ -functions [See also 11S45, 16Hxx, 16Kxx]
- 11R56 Adèle rings and groups
- 11R58 Arithmetic theory of algebraic function fields [See also 14-XX]

- 11R60 Cyclotomic function fields (class groups, Bernoulli objects, etc.)
- 11R65 Class groups and Picard groups of orders
- 11R70  $K$ -theory of global fields [See also 19Fxx]
- 11R80 Totally real fields [See also 12J15]
- 11R99 None of the above, but in this section
- 11Sxx Algebraic number theory: local and  $p$ -adic fields**
- 11S05 Polynomials
- 11S15 Ramification and extension theory
- 11S20 Galois theory
- 11S23 Integral representations
- 11S25 Galois cohomology [See also 12Gxx, 16H05]
- 11S31 Class field theory;  $p$ -adic formal groups [See also 14L05]
- 11S37 Langlands-Weil conjectures, nonabelian class field theory  
[See also 11Fxx, 22E50]
- 11S40 Zeta functions and  $L$ -functions [See also 11M41, 19F27]
- 11S45 Algebras and orders, and their zeta functions [See also 11R52, 11R54,  
16Hxx, 16Kxx]
- 11S70  $K$ -theory of local fields [See also 19Fxx]
- 11S80 Other analytic theory (analogues of beta and gamma functions,  $p$ -  
adic integration, etc.)
- 11S82 Non-Archimedean dynamical systems [See mainly 37Pxx]
- 11S85 Other nonanalytic theory
- 11S90 Prehomogeneous vector spaces
- 11S99 None of the above, but in this section
- 11Txx Finite fields and commutative rings (number-theoretic aspects)**
- 11T06 Polynomials
- 11T22 Cyclotomy
- 11T23 Exponential sums
- 11T24 Other character sums and Gauss sums
- 11T30 Structure theory
- 11T55 Arithmetic theory of polynomial rings over finite fields
- 11T60 Finite upper half-planes
- 11T71 Algebraic coding theory; cryptography
- 11T99 None of the above, but in this section
- 11Uxx Connections with logic**
- 11U05 Decidability [See also 03B25]
- 11U07 Ultraproducts [See also 03C20]
- 11U09 Model theory [See also 03Cxx]
- 11U10 Nonstandard arithmetic [See also 03H15]
- 11U99 None of the above, but in this section
- 11Yxx Computational number theory [See also 11-04]**
- 11Y05 Factorization
- 11Y11 Primality
- 11Y16 Algorithms; complexity [See also 68Q25]
- 11Y35 Analytic computations
- 11Y40 Algebraic number theory computations
- 11Y50 Computer solution of Diophantine equations
- 11Y55 Calculation of integer sequences
- 11Y60 Evaluation of constants
- 11Y65 Continued fraction calculations
- 11Y70 Values of arithmetic functions; tables
- 11Y99 None of the above, but in this section

- 11Zxx** **Miscellaneous applications of number theory**
- 11Z05 Miscellaneous applications of number theory
- 11Z99 None of the above, but in this section
- 12–XX** **FIELD THEORY AND POLYNOMIALS**
- 12–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 12–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 12–02 Research exposition (monographs, survey articles)
- 12–03 Historical (must also be assigned at least one classification number from Section 01)
- 12–04 Explicit machine computation and programs (not the theory of computation or programming)
- 12–06 Proceedings, conferences, collections, etc.
- 12Dxx** **Real and complex fields**
- 12D05 Polynomials: factorization
- 12D10 Polynomials: location of zeros (algebraic theorems)  $\{\{\}\}$ For the analytic theory, see 26C10, 30C15
- 12D15 Fields related with sums of squares (formally real fields, Pythagorean fields, etc.) [See also 11Exx]
- 12D99 None of the above, but in this section
- 12Exx** **General field theory**
- 12E05 Polynomials (irreducibility, etc.)
- 12E10 Special polynomials
- 12E12 Equations
- 12E15 Skew fields, division rings [See also 11R52, 11R54, 11S45, 16Kxx]
- 12E20 Finite fields (field-theoretic aspects)
- 12E25 Hilbertian fields; Hilbert’s irreducibility theorem
- 12E30 Field arithmetic
- 12E99 None of the above, but in this section
- 12Fxx** **Field extensions**
- 12F05 Algebraic extensions
- 12F10 Separable extensions, Galois theory
- 12F12 Inverse Galois theory
- 12F15 Inseparable extensions
- 12F20 Transcendental extensions
- 12F99 None of the above, but in this section
- 12Gxx** **Homological methods (field theory)**
- 12G05 Galois cohomology [See also 14F22, 16Hxx, 16K50]
- 12G10 Cohomological dimension
- 12G99 None of the above, but in this section
- 12Hxx** **Differential and difference algebra**
- 12H05 Differential algebra [See also 13Nxx]
- 12H10 Difference algebra [See also 39Axx]
- 12H20 Abstract differential equations [See also 34Mxx]
- 12H25  $p$ -adic differential equations [See also 11S80, 14G20]
- 12H99 None of the above, but in this section
- 12Jxx** **Topological fields**
- 12J05 Normed fields
- 12J10 Valued fields
- 12J12 Formally  $p$ -adic fields
- 12J15 Ordered fields

- 12J17 Topological semifields
- 12J20 General valuation theory [See also 13A18]
- 12J25 Non-Archimedean valued fields [See also 30G06, 32P05, 46S10, 47S10]
- 12J27 Krasner-Tate algebras [See mainly 32P05; see also 46S10, 47S10]
- 12J99 None of the above, but in this section
- 12Kxx Generalizations of fields**
- 12K05 Near-fields [See also 16Y30]
- 12K10 Semifields [See also 16Y60]
- 12K99 None of the above, but in this section
- 12Lxx Connections with logic**
- 12L05 Decidability [See also 03B25]
- 12L10 Ultraproducts [See also 03C20]
- 12L12 Model theory [See also 03C60]
- 12L15 Nonstandard arithmetic [See also 03H15]
- 12L99 None of the above, but in this section
- 12Yxx Computational aspects of field theory and polynomials**
- 12Y05 Computational aspects of field theory and polynomials
- 12Y99 None of the above, but in this section
- 13–XX COMMUTATIVE RINGS AND ALGEBRAS**
- 13–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 13–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 13–02 Research exposition (monographs, survey articles)
- 13–03 Historical (must also be assigned at least one classification number from Section 01)
- 13–04 Explicit machine computation and programs (not the theory of computation or programming)
- 13–06 Proceedings, conferences, collections, etc.
- 13Axx General commutative ring theory**
- 13A02 Graded rings [See also 16W50]
- 13A05 Divisibility; factorizations [See also 13F15]
- 13A15 Ideals; multiplicative ideal theory
- 13A18 Valuations and their generalizations [See also 12J20]
- 13A30 Associated graded rings of ideals (Rees ring, form ring), analytic spread and related topics
- 13A35 Characteristic  $p$  methods (Frobenius endomorphism) and reduction to characteristic  $p$ ; tight closure [See also 13B22]
- 13A50 Actions of groups on commutative rings; invariant theory [See also 14L24]
- 13A99 None of the above, but in this section
- 13Bxx Ring extensions and related topics**
- 13B02 Extension theory
- 13B05 Galois theory
- 13B10 Morphisms
- 13B21 Integral dependence; going up, going down
- 13B22 Integral closure of rings and ideals [See also 13A35]; integrally closed rings, related rings (Japanese, etc.)
- 13B25 Polynomials over commutative rings [See also 11C08, 11T06, 13F20, 13M10]
- 13B30 Rings of fractions and localization [See also 16S85]
- 13B35 Completion [See also 13J10]

- 13B40 Étale and flat extensions; Henselization; Artin approximation  
[See also 13J15, 14B12, 14B25]
- 13B99 None of the above, but in this section
- 13Cxx Theory of modules and ideals**
- 13C05 Structure, classification theorems
- 13C10 Projective and free modules and ideals [See also 19A13]
- 13C11 Injective and flat modules and ideals
- 13C12 Torsion modules and ideals
- 13C13 Other special types
- 13C14 Cohen-Macaulay modules [See also 13H10]
- 13C15 Dimension theory, depth, related rings (catenary, etc.)
- 13C20 Class groups [See also 11R29]
- 13C40 Linkage, complete intersections and determinantal ideals  
[See also 14M06, 14M10, 14M12]
- 13C60 Module categories
- 13C99 None of the above, but in this section
- 13Dxx Homological methods  $\{\{\}\}$  For noncommutative rings, see 16Exx; for general categories, see 18Gxx**
- 13D02 Syzygies, resolutions, complexes
- 13D03 (Co)homology of commutative rings and algebras (e.g., Hochschild, André-Quillen, cyclic, dihedral, etc.)
- 13D05 Homological dimension
- 13D07 Homological functors on modules (Tor, Ext, etc.)
- 13D09 Derived categories
- 13D10 Deformations and infinitesimal methods [See also 14B10, 14B12, 14D15, 32Gxx]
- 13D15 Grothendieck groups,  $K$ -theory [See also 14C35, 18F30, 19Axx, 19D50]
- 13D22 Homological conjectures (intersection theorems)
- 13D30 Torsion theory [See also 13C12, 18E40]
- 13D40 Hilbert-Samuel and Hilbert-Kunz functions; Poincaré series
- 13D45 Local cohomology [See also 14B15]
- 13D99 None of the above, but in this section
- 13Exx Chain conditions, finiteness conditions**
- 13E05 Noetherian rings and modules
- 13E10 Artinian rings and modules, finite-dimensional algebras
- 13E15 Rings and modules of finite generation or presentation; number of generators
- 13E99 None of the above, but in this section
- 13Fxx Arithmetic rings and other special rings**
- 13F05 Dedekind, Prüfer, Krull and Mori rings and their generalizations
- 13F07 Euclidean rings and generalizations
- 13F10 Principal ideal rings
- 13F15 Rings defined by factorization properties (e.g., atomic, factorial, half-factorial) [See also 13A05, 14M05]
- 13F20 Polynomial rings and ideals; rings of integer-valued polynomials  
[See also 11C08, 13B25]
- 13F25 Formal power series rings [See also 13J05]
- 13F30 Valuation rings [See also 13A18]
- 13F35 Witt vectors and related rings
- 13F40 Excellent rings

- 13F45 Seminormal rings
- 13F50 Rings with straightening laws, Hodge algebras
- 13F55 Stanley-Reisner face rings; simplicial complexes [See also 55U10]
- 13F60 Cluster algebras
- 13F99 None of the above, but in this section
- 13Gxx Integral domains**
- 13G05 Integral domains
- 13G99 None of the above, but in this section
- 13Hxx Local rings and semilocal rings**
- 13H05 Regular local rings
- 13H10 Special types (Cohen-Macaulay, Gorenstein, Buchsbaum, etc.)  
[See also 14M05]
- 13H15 Multiplicity theory and related topics [See also 14C17]
- 13H99 None of the above, but in this section
- 13Jxx Topological rings and modules [See also 16W60, 16W80]**
- 13J05 Power series rings [See also 13F25]
- 13J07 Analytical algebras and rings [See also 32B05]
- 13J10 Complete rings, completion [See also 13B35]
- 13J15 Henselian rings [See also 13B40]
- 13J20 Global topological rings
- 13J25 Ordered rings [See also 06F25]
- 13J30 Real algebra [See also 12D15, 14Pxx]
- 13J99 None of the above, but in this section
- 13Lxx Applications of logic to commutative algebra [See also 03Cxx, 03Hxx]**
- 13L05 Applications of logic to commutative algebra [See also 03Cxx, 03Hxx]
- 13L99 None of the above, but in this section
- 13Mxx Finite commutative rings  $\{\{\}\}$  For number-theoretic aspects, see 11Txx**
- 13M05 Structure
- 13M10 Polynomials
- 13M99 None of the above, but in this section
- 13Nxx Differential algebra [See also 12H05, 14F10]**
- 13N05 Modules of differentials
- 13N10 Rings of differential operators and their modules [See also 16S32, 32C38]
- 13N15 Derivations
- 13N99 None of the above, but in this section
- 13Pxx Computational aspects and applications [See also 14Qxx, 68W30]**
- 13P05 Polynomials, factorization [See also 12Y05]
- 13P10 Gröbner bases; other bases for ideals and modules (e.g., Janet and border bases)
- 13P15 Solving polynomial systems; resultants
- 13P20 Computational homological algebra [See also 13Dxx]
- 13P25 Applications of commutative algebra (e.g., to statistics, control theory, optimization, etc.)
- 13P99 None of the above, but in this section
- 14–XX ALGEBRAIC GEOMETRY**
- 14–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 14–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 14–02 Research exposition (monographs, survey articles)

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- 14–03 Historical (must also be assigned at least one classification number from Section 01)
- 14–04 Explicit machine computation and programs (not the theory of computation or programming)
- 14–06 Proceedings, conferences, collections, etc.
- 14Axx Foundations**
- 14A05 Relevant commutative algebra [See also 13–XX]
- 14A10 Varieties and morphisms
- 14A15 Schemes and morphisms
- 14A20 Generalizations (algebraic spaces, stacks)
- 14A22 Noncommutative algebraic geometry [See also 16S38]
- 14A25 Elementary questions
- 14A99 None of the above, but in this section
- 14Bxx Local theory**
- 14B05 Singularities [See also 14E15, 14H20, 14J17, 32Sxx, 58Kxx]
- 14B07 Deformations of singularities [See also 14D15, 32S30]
- 14B10 Infinitesimal methods [See also 13D10]
- 14B12 Local deformation theory, Artin approximation, etc. [See also 13B40, 13D10]
- 14B15 Local cohomology [See also 13D45, 32C36]
- 14B20 Formal neighborhoods
- 14B25 Local structure of morphisms: étale, flat, etc. [See also 13B40]
- 14B99 None of the above, but in this section
- 14Cxx Cycles and subschemes**
- 14C05 Parametrization (Chow and Hilbert schemes)
- 14C15 (Equivariant) Chow groups and rings; motives
- 14C17 Intersection theory, characteristic classes, intersection multiplicities [See also 13H15]
- 14C20 Divisors, linear systems, invertible sheaves
- 14C21 Pencils, nets, webs [See also 53A60]
- 14C22 Picard groups
- 14C25 Algebraic cycles
- 14C30 Transcendental methods, Hodge theory [See also 14D07, 32G20, 32J25, 32S35], Hodge conjecture
- 14C34 Torelli problem [See also 32G20]
- 14C35 Applications of methods of algebraic  $K$ -theory [See also 19Exx]
- 14C40 Riemann-Roch theorems [See also 19E20, 19L10]
- 14C99 None of the above, but in this section
- 14Dxx Families, fibrations**
- 14D05 Structure of families (Picard-Lefschetz, monodromy, etc.)
- 14D06 Fibrations, degenerations
- 14D07 Variation of Hodge structures [See also 32G20]
- 14D10 Arithmetic ground fields (finite, local, global)
- 14D15 Formal methods; deformations [See also 13D10, 14B07, 32Gxx]
- 14D20 Algebraic moduli problems, moduli of vector bundles  $\{\{\}\}$ For analytic moduli problems, see 32G13
- 14D21 Applications of vector bundles and moduli spaces in mathematical physics (twistor theory, instantons, quantum field theory)
- 14D22 Fine and coarse moduli spaces
- 14D23 Stacks and moduli problems
- 14D24 Geometric Langlands program: algebro-geometric aspects [See also 22E57]

- 14D99 None of the above, but in this section
- 14Exx Birational geometry**
- 14E05 Rational and birational maps
- 14E07 Birational automorphisms, Cremona group and generalizations
- 14E08 Rationality questions [See also 14M20]
- 14E15 Global theory and resolution of singularities [See also 14B05, 32S20, 32S45]
- 14E16 McKay correspondence
- 14E18 Arcs and motivic integration
- 14E20 Coverings [See also 14H30]
- 14E22 Ramification problems [See also 11S15]
- 14E25 Embeddings
- 14E30 Minimal model program (Mori theory, extremal rays)
- 14E99 None of the above, but in this section
- 14Fxx (Co)homology theory [See also 13Dxx]**
- 14F05 Sheaves, derived categories of sheaves and related constructions [See also 14H60, 14J60, 18F20, 32Lxx, 46M20]
- 14F10 Differentials and other special sheaves; D-modules; Bernstein-Sato ideals and polynomials [See also 13Nxx, 32C38]
- 14F17 Vanishing theorems [See also 32L20]
- 14F18 Multiplier ideals
- 14F20 Étale and other Grothendieck topologies and cohomologies
- 14F22 Brauer groups of schemes [See also 12G05, 16K50]
- 14F25 Classical real and complex cohomology
- 14F30  $p$ -adic cohomology, crystalline cohomology
- 14F35 Homotopy theory; fundamental groups [See also 14H30]
- 14F40 de Rham cohomology [See also 14C30, 32C35, 32L10]
- 14F42 Motivic cohomology; motivic homotopy theory
- 14F43 Other algebro-geometric (co)homologies (e.g., intersection, equivariant, Lawson, Deligne (co)homologies)
- 14F45 Topological properties
- 14F99 None of the above, but in this section
- 14Gxx Arithmetic problems. Diophantine geometry [See also 11Dxx, 11Gxx]**
- 14G05 Rational points
- 14G10 Zeta-functions and related questions [See also 11G40] (Birch-Swinnerton-Dyer conjecture)
- 14G15 Finite ground fields
- 14G17 Positive characteristic ground fields
- 14G20 Local ground fields
- 14G22 Rigid analytic geometry
- 14G25 Global ground fields
- 14G27 Other nonalgebraically closed ground fields
- 14G32 Universal profinite groups (relationship to moduli spaces, projective and moduli towers, Galois theory)
- 14G35 Modular and Shimura varieties [See also 11F41, 11F46, 11G18]
- 14G40 Arithmetic varieties and schemes; Arakelov theory; heights [See also 11G50, 37P30]
- 14G50 Applications to coding theory and cryptography [See also 94A60, 94B27, 94B40]
- 14G99 None of the above, but in this section

- 14Hxx Curves**
- 14H05 Algebraic functions; function fields [See also 11R58]
  - 14H10 Families, moduli (algebraic)
  - 14H15 Families, moduli (analytic) [See also 30F10, 32Gxx]
  - 14H20 Singularities, local rings [See also 13Hxx, 14B05]
  - 14H25 Arithmetic ground fields [See also 11Dxx, 11G05, 14Gxx]
  - 14H30 Coverings, fundamental group [See also 14E20, 14F35]
  - 14H37 Automorphisms
  - 14H40 Jacobians, Prym varieties [See also 32G20]
  - 14H42 Theta functions; Schottky problem [See also 14K25, 32G20]
  - 14H45 Special curves and curves of low genus
  - 14H50 Plane and space curves
  - 14H51 Special divisors (gonality, Brill-Noether theory)
  - 14H52 Elliptic curves [See also 11G05, 11G07, 14Kxx]
  - 14H55 Riemann surfaces; Weierstrass points; gap sequences [See also 30Fxx]
  - 14H57 Dessins d'enfants theory  $\{\{\}\}$ For arithmetic aspects, see 11G32
  - 14H60 Vector bundles on curves and their moduli [See also 14D20, 14F05]
  - 14H70 Relationships with integrable systems
  - 14H81 Relationships with physics
  - 14H99 None of the above, but in this section
  - 14Jxx Surfaces and higher-dimensional varieties  $\{\{\}\}$ For analytic theory, see 32Jxx**
  - 14J10 Families, moduli, classification: algebraic theory
  - 14J15 Moduli, classification: analytic theory; relations with modular forms [See also 32G13]
  - 14J17 Singularities [See also 14B05, 14E15]
  - 14J20 Arithmetic ground fields [See also 11Dxx, 11G25, 11G35, 14Gxx]
  - 14J25 Special surfaces  $\{\{\}\}$ For Hilbert modular surfaces, see 14G35
  - 14J26 Rational and ruled surfaces
  - 14J27 Elliptic surfaces
  - 14J28  $K3$  surfaces and Enriques surfaces
  - 14J29 Surfaces of general type
  - 14J30 3-folds [See also 32Q25]
  - 14J32 Calabi-Yau manifolds
  - 14J33 Mirror symmetry [See also 11G42, 53D37]
  - 14J35 4-folds
  - 14J40  $n$ -folds ( $n > 4$ )
  - 14J45 Fano varieties
  - 14J50 Automorphisms of surfaces and higher-dimensional varieties
  - 14J60 Vector bundles on surfaces and higher-dimensional varieties, and their moduli [See also 14D20, 14F05, 32Lxx]
  - 14J70 Hypersurfaces
  - 14J80 Topology of surfaces (Donaldson polynomials, Seiberg-Witten invariants)
  - 14J81 Relationships with physics
  - 14J99 None of the above, but in this section
  - 14Kxx Abelian varieties and schemes**
  - 14K02 Isogeny
  - 14K05 Algebraic theory
  - 14K10 Algebraic moduli, classification [See also 11G15]
  - 14K12 Subvarieties

- 14K15 Arithmetic ground fields [See also 11Dxx, 11Fxx, 11Gxx, 14Gxx]
- 14K20 Analytic theory; abelian integrals and differentials
- 14K22 Complex multiplication [See also 11G15]
- 14K25 Theta functions [See also 14H42]
- 14K30 Picard schemes, higher Jacobians [See also 14H40, 32G20]
- 14K99 None of the above, but in this section
- 14Lxx Algebraic groups  $\{\}$  For linear algebraic groups, see 20Gxx; for Lie algebras, see 17B45**
- 14L05 Formal groups,  $p$ -divisible groups [See also 55N22]
- 14L10 Group varieties
- 14L15 Group schemes
- 14L17 Affine algebraic groups, hyperalgebra constructions [See also 17B45, 18D35]
- 14L24 Geometric invariant theory [See also 13A50]
- 14L30 Group actions on varieties or schemes (quotients) [See also 13A50, 14L24]
- 14L35 Classical groups (geometric aspects) [See also 20Gxx, 51N30]
- 14L40 Other algebraic groups (geometric aspects)
- 14L99 None of the above, but in this section
- 14Mxx Special varieties**
- 14M05 Varieties defined by ring conditions (factorial, Cohen-Macaulay, seminormal) [See also 13F45, 13H10]
- 14M06 Linkage [See also 13C40]
- 14M07 Low codimension problems
- 14M10 Complete intersections [See also 13C40]
- 14M12 Determinantal varieties [See also 13C40]
- 14M15 Grassmannians, Schubert varieties, flag manifolds [See also 32M10, 51M35]
- 14M17 Homogeneous spaces and generalizations [See also 32M10, 53C30, 57T15]
- 14M20 Rational and unirational varieties [See also 14E08]
- 14M22 Rationally connected varieties
- 14M25 Toric varieties, Newton polyhedra [See also 52B20]
- 14M27 Compactifications; symmetric and spherical varieties
- 14M30 Supervarities [See also 32C11, 58A50]
- 14M99 None of the above, but in this section
- 14Nxx Projective and enumerative geometry [See also 51–XX]**
- 14N05 Projective techniques [See also 51N35]
- 14N10 Enumerative problems (combinatorial problems)
- 14N15 Classical problems, Schubert calculus
- 14N20 Configurations and arrangements of linear subspaces
- 14N25 Varieties of low degree
- 14N30 Adjunction problems
- 14N35 Gromov-Witten invariants, quantum cohomology, Gopakumar-Vafa invariants, Donaldson-Thomas invariants [See also 53D45]
- 14N99 None of the above, but in this section
- 14Pxx Real algebraic and real analytic geometry**
- 14P05 Real algebraic sets [See also 12Dxx]
- 14P10 Semialgebraic sets and related spaces
- 14P15 Real analytic and semianalytic sets [See also 32B20, 32C05]
- 14P20 Nash functions and manifolds [See also 32C07, 58A07]

- 14P25 Topology of real algebraic varieties
- 14P99 None of the above, but in this section
- 14Qxx Computational aspects in algebraic geometry [See also 12Y05, 13Pxx, 68W30]**
- 14Q05 Curves
- 14Q10 Surfaces, hypersurfaces
- 14Q15 Higher-dimensional varieties
- 14Q20 Effectivity, complexity
- 14Q99 None of the above, but in this section
- 14Rxx Affine geometry**
- 14R05 Classification of affine varieties
- 14R10 Affine spaces (automorphisms, embeddings, exotic structures, cancellation problem)
- 14R15 Jacobian problem
- 14R20 Group actions on affine varieties [See also 13A50, 14L30]
- 14R25 Affine fibrations [See also 14D06]
- 14R99 None of the above, but in this section
- 14Txx Tropical geometry [See also 12K10, 14M25, 14N10, 52B20]**
- 14T05 Tropical geometry [See also 12K10, 14M25, 14N10, 52B20]
- 14T99 None of the above, but in this section
- 15–XX LINEAR AND MULTILINEAR ALGEBRA; MATRIX THEORY**
- 15–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 15–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 15–02 Research exposition (monographs, survey articles)
- 15–03 Historical (must also be assigned at least one classification number from Section 01)
- 15–04 Explicit machine computation and programs (not the theory of computation or programming)
- 15–06 Proceedings, conferences, collections, etc.
- 15Axx Basic linear algebra**
- 15A03 Vector spaces, linear dependence, rank
- 15A04 Linear transformations, semilinear transformations
- 15A06 Linear equations
- 15A09 Matrix inversion, generalized inverses
- 15A12 Conditioning of matrices [See also 65F35]
- 15A15 Determinants, permanents, other special matrix functions [See also 19B10, 19B14]
- 15A16 Matrix exponential and similar functions of matrices
- 15A18 Eigenvalues, singular values, and eigenvectors
- 15A21 Canonical forms, reductions, classification
- 15A22 Matrix pencils [See also 47A56]
- 15A23 Factorization of matrices
- 15A24 Matrix equations and identities
- 15A27 Commutativity
- 15A29 Inverse problems
- 15A30 Algebraic systems of matrices [See also 16S50, 20Gxx, 20Hxx]
- 15A33 Matrices over special rings (quaternions, finite fields, etc.)
- 15A39 Linear inequalities
- 15A42 Inequalities involving eigenvalues and eigenvectors
- 15A45 Miscellaneous inequalities involving matrices

- 15A54 Matrices over function rings in one or more variables
- 15A60 Norms of matrices, numerical range, applications of functional analysis to matrix theory [See also 65F35, 65J05]
- 15A63 Quadratic and bilinear forms, inner products [See mainly 11Exx]
- 15A66 Clifford algebras, spinors
- 15A69 Multilinear algebra, tensor products
- 15A72 Vector and tensor algebra, theory of invariants [See also 13A50, 14L24]
- 15A75 Exterior algebra, Grassmann algebras
- 15A78 Other algebras built from modules
- 15A80 Max-plus and related algebras
- 15A83 Matrix completion problems
- 15A86 Linear preserver problems
- 15A99 Miscellaneous topics
- 15Bxx Special matrices**
- 15B05 Toeplitz, Cauchy, and related matrices
- 15B10 Orthogonal matrices
- 15B15 Fuzzy matrices
- 15B33 Matrices over special rings (quaternions, finite fields, etc.)
- 15B34 Boolean and Hadamard matrices
- 15B35 Sign pattern matrices
- 15B36 Matrices of integers [See also 11C20]
- 15B48 Positive matrices and their generalizations; cones of matrices
- 15B51 Stochastic matrices
- 15B52 Random matrices
- 15B57 Hermitian, skew-Hermitian, and related matrices
- 15B99 None of the above, but in this section
- 16–XX ASSOCIATIVE RINGS AND ALGEBRAS FOR THE COMMUTATIVE CASE, SEE 13–XX{}**
- 16–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 16–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 16–02 Research exposition (monographs, survey articles)
- 16–03 Historical (must also be assigned at least one classification number from Section 01)
- 16–04 Explicit machine computation and programs (not the theory of computation or programming)
- 16–06 Proceedings, conferences, collections, etc.
- 16Bxx General and miscellaneous**
- 16B50 Category-theoretic methods and results (except as in 16D90) [See also 18–XX]
- 16B70 Applications of logic [See also 03Cxx]
- 16B99 None of the above, but in this section
- 16Dxx Modules, bimodules and ideals**
- 16D10 General module theory
- 16D20 Bimodules
- 16D25 Ideals
- 16D30 Infinite-dimensional simple rings (except as in 16Kxx)
- 16D40 Free, projective, and flat modules and ideals [See also 19A13]
- 16D50 Injective modules, self-injective rings [See also 16L60]
- 16D60 Simple and semisimple modules, primitive rings and ideals

- 16D70 Structure and classification (except as in 16Gxx), direct sum decomposition, cancellation
- 16D80 Other classes of modules and ideals [See also 16G50]
- 16D90 Module categories [See also 16Gxx, 16S90]; module theory in a category-theoretic context; Morita equivalence and duality
- 16D99 None of the above, but in this section
- 16Exx Homological methods  $\{\{\}\}$  For commutative rings, see 13Dxx; for general categories, see 18Gxx**
- 16E05 Syzygies, resolutions, complexes
- 16E10 Homological dimension
- 16E20 Grothendieck groups,  $K$ -theory, etc. [See also 18F30, 19Axx, 19D50]
- 16E30 Homological functors on modules (Tor, Ext, etc.)
- 16E35 Derived categories
- 16E40 (Co)homology of rings and algebras (e.g. Hochschild, cyclic, dihedral, etc.)
- 16E45 Differential graded algebras and applications
- 16E50 von Neumann regular rings and generalizations
- 16E60 Semihereditary and hereditary rings, free ideal rings, Sylvester rings, etc.
- 16E65 Homological conditions on rings (generalizations of regular, Gorenstein, Cohen-Macaulay rings, etc.)
- 16E99 None of the above, but in this section
- 16Gxx Representation theory of rings and algebras**
- 16G10 Representations of Artinian rings
- 16G20 Representations of quivers and partially ordered sets
- 16G30 Representations of orders, lattices, algebras over commutative rings [See also 16Hxx]
- 16G50 Cohen-Macaulay modules
- 16G60 Representation type (finite, tame, wild, etc.)
- 16G70 Auslander-Reiten sequences (almost split sequences) and Auslander-Reiten quivers
- 16G99 None of the above, but in this section
- 16Hxx Algebras and orders  $\{\{\}\}$  For arithmetic aspects, see 11R52, 11R54, 11S45**
- 16H05 Separable algebras (e.g., quaternion algebras, Azumaya algebras, etc.)
- 16H10 Orders in separable algebras
- 16H15 Commutative orders
- 16H20 Lattices over orders
- 16H99 None of the above, but in this section
- 16Kxx Division rings and semisimple Artin rings [See also 12E15, 15A30]**
- 16K20 Finite-dimensional  $\{\{\}\}$  For crossed products, see 16S35
- 16K40 Infinite-dimensional and general
- 16K50 Brauer groups [See also 12G05, 14F22]
- 16K99 None of the above, but in this section
- 16Lxx Local rings and generalizations**
- 16L30 Noncommutative local and semilocal rings, perfect rings
- 16L60 Quasi-Frobenius rings [See also 16D50]
- 16L99 None of the above, but in this section
- 16Nxx Radicals and radical properties of rings**
- 16N20 Jacobson radical, quasimultiplication
- 16N40 Nil and nilpotent radicals, sets, ideals, rings

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- 16N60 Prime and semiprime rings [See also 16D60, 16U10]
- 16N80 General radicals and rings  $\{\{\}\}$ For radicals in module categories, see 16S90
- 16N99 None of the above, but in this section
- 16Pxx Chain conditions, growth conditions, and other forms of finiteness**
- 16P10 Finite rings and finite-dimensional algebras  $\{\{\}\}$ For semisimple, see 16K20; for commutative, see 11Txx, 13Mxx
- 16P20 Artinian rings and modules
- 16P40 Noetherian rings and modules
- 16P50 Localization and Noetherian rings [See also 16U20]
- 16P60 Chain conditions on annihilators and summands: Goldie-type conditions [See also 16U20], Krull dimension
- 16P70 Chain conditions on other classes of submodules, ideals, subrings, etc.; coherence
- 16P90 Growth rate, Gelfand-Kirillov dimension
- 16P99 None of the above, but in this section
- 16Rxx Rings with polynomial identity**
- 16R10  $T$ -ideals, identities, varieties of rings and algebras
- 16R20 Semiprime p.i. rings, rings embeddable in matrices over commutative rings
- 16R30 Trace rings and invariant theory
- 16R40 Identities other than those of matrices over commutative rings
- 16R50 Other kinds of identities (generalized polynomial, rational, involution)
- 16R60 Functional identities
- 16R99 None of the above, but in this section
- 16Sxx Rings and algebras arising under various constructions**
- 16S10 Rings determined by universal properties (free algebras, coproducts, adjunction of inverses, etc.)
- 16S15 Finite generation, finite presentability, normal forms (diamond lemma, term-rewriting)
- 16S20 Centralizing and normalizing extensions
- 16S30 Universal enveloping algebras of Lie algebras [See mainly 17B35]
- 16S32 Rings of differential operators [See also 13N10, 32C38]
- 16S34 Group rings [See also 20C05, 20C07], Laurent polynomial rings
- 16S35 Twisted and skew group rings, crossed products
- 16S36 Ordinary and skew polynomial rings and semigroup rings [See also 20M25]
- 16S37 Quadratic and Koszul algebras
- 16S38 Rings arising from non-commutative algebraic geometry [See also 14A22]
- 16S40 Smash products of general Hopf actions [See also 16T05]
- 16S50 Endomorphism rings; matrix rings [See also 15-XX]
- 16S60 Rings of functions, subdirect products, sheaves of rings
- 16S70 Extensions of rings by ideals
- 16S80 Deformations of rings [See also 13D10, 14D15]
- 16S85 Rings of fractions and localizations [See also 13B30]
- 16S90 Torsion theories; radicals on module categories [See also 13D30, 18E40]  $\{\{\}\}$ For radicals of rings, see 16Nxx
- 16S99 None of the above, but in this section

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- 16Txx**    **Hopf algebras, quantum groups and related topics**
- 16T05    Hopf algebras and their applications [See also 16S40, 57T05]
- 16T10    Bialgebras
- 16T15    Coalgebras and comodules; corings
- 16T20    Ring-theoretic aspects of quantum groups [See also 17B37, 20G42, 81R50]
- 16T25    Yang-Baxter equations
- 16T30    Connections with combinatorics
- 16T99    None of the above, but in this section
- 16Uxx**    **Conditions on elements**
- 16U10    Integral domains
- 16U20    Ore rings, multiplicative sets, Ore localization
- 16U30    Divisibility, noncommutative UFDs
- 16U60    Units, groups of units
- 16U70    Center, normalizer (invariant elements)
- 16U80    Generalizations of commutativity
- 16U99    None of the above, but in this section
- 16Wxx**    **Rings and algebras with additional structure**
- 16W10    Rings with involution; Lie, Jordan and other nonassociative structures [See also 17B60, 17C50, 46Kxx]
- 16W20    Automorphisms and endomorphisms
- 16W22    Actions of groups and semigroups; invariant theory
- 16W25    Derivations, actions of Lie algebras
- 16W50    Graded rings and modules
- 16W55    “Super” (or “skew”) structure [See also 17A70, 17Bxx, 17C70]   
    {{{}}For exterior algebras, see 15A75; for Clifford algebras, see 11E88, 15A66
- 16W60    Valuations, completions, formal power series and related constructions [See also 13Jxx]
- 16W70    Filtered rings; filtrational and graded techniques
- 16W80    Topological and ordered rings and modules [See also 06F25, 13Jxx]
- 16W99    None of the above, but in this section
- 16Yxx**    **Generalizations {{{}}For nonassociative rings, see 17-XX**
- 16Y30    Near-rings [See also 12K05]
- 16Y60    Semirings [See also 12K10]
- 16Y99    None of the above, but in this section
- 16Zxx**    **Computational aspects of associative rings**
- 16Z05    Computational aspects of associative rings [See also 68W30]
- 16Z99    None of the above, but in this section
- 17-XX**    **NONASSOCIATIVE RINGS AND ALGEBRAS**
- 17-00    General reference works (handbooks, dictionaries, bibliographies, etc.)
- 17-01    Instructional exposition (textbooks, tutorial papers, etc.)
- 17-02    Research exposition (monographs, survey articles)
- 17-03    Historical (must also be assigned at least one classification number from Section 01)
- 17-04    Explicit machine computation and programs (not the theory of computation or programming)
- 17-06    Proceedings, conferences, collections, etc.
- 17-08    Computational methods

- 17Axx**    **General nonassociative rings**
- 17A01    General theory
- 17A05    Power-associative rings
- 17A15    Noncommutative Jordan algebras
- 17A20    Flexible algebras
- 17A30    Algebras satisfying other identities
- 17A32    Leibniz algebras
- 17A35    Division algebras
- 17A36    Automorphisms, derivations, other operators
- 17A40    Ternary compositions
- 17A42    Other  $n$ -ary compositions ( $n \geq 3$ )
- 17A45    Quadratic algebras (but not quadratic Jordan algebras)
- 17A50    Free algebras
- 17A60    Structure theory
- 17A65    Radical theory
- 17A70    Superalgebras
- 17A75    Composition algebras
- 17A80    Valued algebras
- 17A99    None of the above, but in this section
- 17Bxx**    **Lie algebras and Lie superalgebras  $\{\{\}\}$  For Lie groups, see 22Exx**
- 17B01    Identities, free Lie (super)algebras
- 17B05    Structure theory
- 17B08    Coadjoint orbits; nilpotent varieties
- 17B10    Representations, algebraic theory (weights)
- 17B15    Representations, analytic theory
- 17B20    Simple, semisimple, reductive (super)algebras
- 17B22    Root systems
- 17B25    Exceptional (super)algebras
- 17B30    Solvable, nilpotent (super)algebras
- 17B35    Universal enveloping (super)algebras [See also 16S30]
- 17B37    Quantum groups (quantized enveloping algebras) and related deformations [See also 16T20, 20G42, 81R50, 82B23]
- 17B40    Automorphisms, derivations, other operators
- 17B45    Lie algebras of linear algebraic groups [See also 14Lxx and 20Gxx]
- 17B50    Modular Lie (super)algebras
- 17B55    Homological methods in Lie (super)algebras
- 17B56    Cohomology of Lie (super)algebras
- 17B60    Lie (super)algebras associated with other structures (associative, Jordan, etc.) [See also 16W10, 17C40, 17C50]
- 17B62    Lie bialgebras; Lie coalgebras
- 17B63    Poisson algebras
- 17B65    Infinite-dimensional Lie (super)algebras [See also 22E65]
- 17B66    Lie algebras of vector fields and related (super) algebras
- 17B67    Kac-Moody (super)algebras; extended affine Lie algebras; toroidal Lie algebras
- 17B68    Virasoro and related algebras
- 17B69    Vertex operators; vertex operator algebras and related structures
- 17B70    Graded Lie (super)algebras
- 17B75    Color Lie (super)algebras
- 17B80    Applications to integrable systems
- 17B81    Applications to physics
- 17B99    None of the above, but in this section

- 17Cxx** **Jordan algebras (algebras, triples and pairs)**
- 17C05 Identities and free Jordan structures
- 17C10 Structure theory
- 17C17 Radicals
- 17C20 Simple, semisimple algebras
- 17C27 Idempotents, Peirce decompositions
- 17C30 Associated groups, automorphisms
- 17C36 Associated manifolds
- 17C37 Associated geometries
- 17C40 Exceptional Jordan structures
- 17C50 Jordan structures associated with other structures [See also 16W10]
- 17C55 Finite-dimensional structures
- 17C60 Division algebras
- 17C65 Jordan structures on Banach spaces and algebras [See also 46H70, 46L70]
- 17C70 Super structures
- 17C90 Applications to physics
- 17C99 None of the above, but in this section
- 17Dxx** **Other nonassociative rings and algebras**
- 17D05 Alternative rings
- 17D10 Mal'cev (Mal'tsev) rings and algebras
- 17D15 Right alternative rings
- 17D20  $(\gamma, \delta)$ -rings, including  $(1, -1)$ -rings
- 17D25 Lie-admissible algebras
- 17D92 Genetic algebras
- 17D99 None of the above, but in this section
- 18–XX** **CATEGORY THEORY; HOMOLOGICAL ALGEBRA FOR COMMUTATIVE RINGS SEE 13DXX, FOR ASSOCIATIVE RINGS 16EXX, FOR GROUPS 20JXX, FOR TOPOLOGICAL GROUPS AND RELATED STRUCTURES 57TXX; SEE ALSO 55NXX AND 55UXX FOR ALGEBRAIC TOPOLOGY{}**
- 18–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 18–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 18–02 Research exposition (monographs, survey articles)
- 18–03 Historical (must also be assigned at least one classification number from Section 01)
- 18–04 Explicit machine computation and programs (not the theory of computation or programming)
- 18–06 Proceedings, conferences, collections, etc.
- 18Axx** **General theory of categories and functors**
- 18A05 Definitions, generalizations
- 18A10 Graphs, diagram schemes, precategories [See especially 20L05]
- 18A15 Foundations, relations to logic and deductive systems [See also 03–XX]
- 18A20 Epimorphisms, monomorphisms, special classes of morphisms, null morphisms
- 18A22 Special properties of functors (faithful, full, etc.)
- 18A23 Natural morphisms, dinatural morphisms
- 18A25 Functor categories, comma categories

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- 18A30 Limits and colimits (products, sums, directed limits, pushouts, fiber products, equalizers, kernels, ends and coends, etc.)
- 18A32 Factorization of morphisms, substructures, quotient structures, congruences, amalgams
- 18A35 Categories admitting limits (complete categories), functors preserving limits, completions
- 18A40 Adjoint functors (universal constructions, reflective subcategories, Kan extensions, etc.)
- 18A99 None of the above, but in this section
- 18Bxx Special categories**
- 18B05 Category of sets, characterizations [See also 03–XX]
- 18B10 Category of relations, additive relations
- 18B15 Embedding theorems, universal categories [See also 18E20]
- 18B20 Categories of machines, automata, operative categories [See also 03D05, 68Qxx]
- 18B25 Topoi [See also 03G30]
- 18B30 Categories of topological spaces and continuous mappings [See also 54–XX]
- 18B35 Preorders, orders and lattices (viewed as categories) [See also 06–XX]
- 18B40 Groupoids, semigroupoids, semigroups, groups (viewed as categories) [See also 20Axx, 20L05, 20Mxx]
- 18B99 None of the above, but in this section
- 18Cxx Categories and theories**
- 18C05 Equational categories [See also 03C05, 08C05]
- 18C10 Theories (e.g. algebraic theories), structure, and semantics [See also 03G30]
- 18C15 Triples (= standard construction, monad or triad), algebras for a triple, homology and derived functors for triples [See also 18Gxx]
- 18C20 Algebras and Kleisli categories associated with monads
- 18C30 Sketches and generalizations
- 18C35 Accessible and locally presentable categories
- 18C50 Categorical semantics of formal languages [See also 68Q55, 68Q65]
- 18C99 None of the above, but in this section
- 18Dxx Categories with structure**
- 18D05 Double categories, 2-categories, bicategories and generalizations
- 18D10 Monoidal categories (= multiplicative categories), symmetric monoidal categories, braided categories [See also 19D23]
- 18D15 Closed categories (closed monoidal and Cartesian closed categories, etc.)
- 18D20 Enriched categories (over closed or monoidal categories)
- 18D25 Strong functors, strong adjunctions
- 18D30 Fibered categories
- 18D35 Structured objects in a category (group objects, etc.)
- 18D50 Operads [See also 55P48]
- 18D99 None of the above, but in this section
- 18Exx Abelian categories**
- 18E05 Preadditive, additive categories
- 18E10 Exact categories, abelian categories
- 18E15 Grothendieck categories
- 18E20 Embedding theorems [See also 18B15]
- 18E25 Derived functors and satellites

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- 18E30 Derived categories, triangulated categories
- 18E35 Localization of categories
- 18E40 Torsion theories, radicals [See also 13D30, 16S90]
- 18E99 None of the above, but in this section
- 18Fxx Categories and geometry**
- 18F05 Local categories and functors
- 18F10 Grothendieck topologies [See also 14F20]
- 18F15 Abstract manifolds and fiber bundles [See also 55Rxx, 57Pxx]
- 18F20 Presheaves and sheaves [See also 14F05, 32C35, 32L10, 54B40, 55N30]
- 18F25 Algebraic  $K$ -theory and  $L$ -theory [See also 11Exx, 11R70, 11S70, 12–XX, 13D15, 14Cxx, 16E20, 19–XX, 46L80, 57R65, 57R67]
- 18F30 Grothendieck groups [See also 13D15, 16E20, 19Axx]
- 18F99 None of the above, but in this section
- 18Gxx Homological algebra** [See also 13Dxx, 16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx]
- 18G05 Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50]
- 18G10 Resolutions; derived functors [See also 13D02, 16E05, 18E25]
- 18G15 Ext and Tor, generalizations, Künneth formula [See also 55U25]
- 18G20 Homological dimension [See also 13D05, 16E10]
- 18G25 Relative homological algebra, projective classes
- 18G30 Simplicial sets, simplicial objects (in a category) [See also 55U10]
- 18G35 Chain complexes [See also 18E30, 55U15]
- 18G40 Spectral sequences, hypercohomology [See also 55Txx]
- 18G50 Nonabelian homological algebra
- 18G55 Homotopical algebra
- 18G60 Other (co)homology theories [See also 19D55, 46L80, 58J20, 58J22]
- 18G99 None of the above, but in this section
- 19–XX  $K$ -THEORY** [See also 16E20, 18F25]
- 19–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 19–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 19–02 Research exposition (monographs, survey articles)
- 19–03 Historical (must also be assigned at least one classification number from Section 01)
- 19–04 Explicit machine computation and programs (not the theory of computation or programming)
- 19–06 Proceedings, conferences, collections, etc.
- 19Axx Grothendieck groups and  $K_0$**  [See also 13D15, 18F30]
- 19A13 Stability for projective modules [See also 13C10]
- 19A15 Efficient generation
- 19A22 Frobenius induction, Burnside and representation rings
- 19A31  $K_0$  of group rings and orders
- 19A49  $K_0$  of other rings
- 19A99 None of the above, but in this section
- 19Bxx Whitehead groups and  $K_1$**
- 19B10 Stable range conditions
- 19B14 Stability for linear groups
- 19B28  $K_1$  of group rings and orders [See also 57Q10]
- 19B37 Congruence subgroup problems [See also 20H05]
- 19B99 None of the above, but in this section

- 19Cxx**    **Steinberg groups and  $K_2$**
- 19C09    Central extensions and Schur multipliers
- 19C20    Symbols, presentations and stability of  $K_2$
- 19C30     $K_2$  and the Brauer group
- 19C40    Excision for  $K_2$
- 19C99    None of the above, but in this section
- 19Dxx**    **Higher algebraic  $K$ -theory**
- 19D06     $Q$ - and plus-constructions
- 19D10    Algebraic  $K$ -theory of spaces
- 19D23    Symmetric monoidal categories [See also 18D10]
- 19D25    Karoubi-Villamayor-Gersten  $K$ -theory
- 19D35    Negative  $K$ -theory, NK and Nil
- 19D45    Higher symbols, Milnor  $K$ -theory
- 19D50    Computations of higher  $K$ -theory of rings [See also 13D15, 16E20]
- 19D55     $K$ -theory and homology; cyclic homology and cohomology  
[See also 18G60]
- 19D99    None of the above, but in this section
- 19Exx**     **$K$ -theory in geometry**
- 19E08     $K$ -theory of schemes [See also 14C35]
- 19E15    Algebraic cycles and motivic cohomology [See also 14C25, 14C35]
- 19E20    Relations with cohomology theories [See also 14Fxx]
- 19E99    None of the above, but in this section
- 19Fxx**     **$K$ -theory in number theory [See also 11R70, 11S70]**
- 19F05    Generalized class field theory [See also 11G45]
- 19F15    Symbols and arithmetic [See also 11R37]
- 19F27    Étale cohomology, higher regulators, zeta and  $L$ -functions  
[See also 11G40, 11R42, 11S40, 14F20, 14G10]
- 19F99    None of the above, but in this section
- 19Gxx**     **$K$ -theory of forms [See also 11Exx]**
- 19G05    Stability for quadratic modules
- 19G12    Witt groups of rings [See also 11E81]
- 19G24     $L$ -theory of group rings [See also 11E81]
- 19G38    Hermitian  $K$ -theory, relations with  $K$ -theory of rings
- 19G99    None of the above, but in this section
- 19Jxx**    **Obstructions from topology**
- 19J05    Finiteness and other obstructions in  $K_0$
- 19J10    Whitehead (and related) torsion
- 19J25    Surgery obstructions [See also 57R67]
- 19J35    Obstructions to group actions
- 19J99    None of the above, but in this section
- 19Kxx**     **$K$ -theory and operator algebras [See mainly 46L80, and also 46M20]**
- 19K14     $K_0$  as an ordered group, traces
- 19K33    EXT and  $K$ -homology [See also 55N22]
- 19K35    Kasparov theory ( $KK$ -theory) [See also 58J22]
- 19K56    Index theory [See also 58J20, 58J22]
- 19K99    None of the above, but in this section
- 19Lxx**    **Topological  $K$ -theory [See also 55N15, 55R50, 55S25]**
- 19L10    Riemann-Roch theorems, Chern characters
- 19L20     $J$ -homomorphism, Adams operations [See also 55Q50]
- 19L41    Connective  $K$ -theory, cobordism [See also 55N22]
- 19L47    Equivariant  $K$ -theory [See also 55N91, 55P91, 55Q91, 55R91, 55S91]

- 19L50 Twisted  $K$ -theory; differential  $K$ -theory
- 19L64 Computations, geometric applications
- 19L99 None of the above, but in this section
- 19Mxx** **Miscellaneous applications of  $K$ -theory**
- 19M05 Miscellaneous applications of  $K$ -theory
- 19M99 None of the above, but in this section
- 20–XX** **GROUP THEORY AND GENERALIZATIONS**
- 20–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 20–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 20–02 Research exposition (monographs, survey articles)
- 20–03 Historical (must also be assigned at least one classification number from Section 01)
- 20–04 Explicit machine computation and programs (not the theory of computation or programming)
- 20–06 Proceedings, conferences, collections, etc.
- 20Axx** **Foundations**
- 20A05 Axiomatics and elementary properties
- 20A10 Metamathematical considerations  $\{\{\}\}$ For word problems, see 20F10
- 20A15 Applications of logic to group theory
- 20A99 None of the above, but in this section
- 20Bxx** **Permutation groups**
- 20B05 General theory for finite groups
- 20B07 General theory for infinite groups
- 20B10 Characterization theorems
- 20B15 Primitive groups
- 20B20 Multiply transitive finite groups
- 20B22 Multiply transitive infinite groups
- 20B25 Finite automorphism groups of algebraic, geometric, or combinatorial structures [See also 05Bxx, 12F10, 20G40, 20H30, 51–XX]
- 20B27 Infinite automorphism groups [See also 12F10]
- 20B30 Symmetric groups
- 20B35 Subgroups of symmetric groups
- 20B40 Computational methods
- 20B99 None of the above, but in this section
- 20Cxx** **Representation theory of groups [See also 19A22 (for representation rings and Burnside rings)]**
- 20C05 Group rings of finite groups and their modules [See also 16S34]
- 20C07 Group rings of infinite groups and their modules [See also 16S34]
- 20C08 Hecke algebras and their representations
- 20C10 Integral representations of finite groups
- 20C11  $p$ -adic representations of finite groups
- 20C12 Integral representations of infinite groups
- 20C15 Ordinary representations and characters
- 20C20 Modular representations and characters
- 20C25 Projective representations and multipliers
- 20C30 Representations of finite symmetric groups
- 20C32 Representations of infinite symmetric groups
- 20C33 Representations of finite groups of Lie type
- 20C34 Representations of sporadic groups
- 20C35 Applications of group representations to physics

- 20C40 Computational methods
- 20C99 None of the above, but in this section
- 20Dxx Abstract finite groups**
- 20D05 Finite simple groups and their classification
- 20D06 Simple groups: alternating groups and groups of Lie type  
[See also 20Gxx]
- 20D08 Simple groups: sporadic groups
- 20D10 Solvable groups, theory of formations, Schunck classes, Fitting classes,  $\pi$ -length, ranks [See also 20F17]
- 20D15 Nilpotent groups,  $p$ -groups
- 20D20 Sylow subgroups, Sylow properties,  $\pi$ -groups,  $\pi$ -structure
- 20D25 Special subgroups (Frattini, Fitting, etc.)
- 20D30 Series and lattices of subgroups
- 20D35 Subnormal subgroups
- 20D40 Products of subgroups
- 20D45 Automorphisms
- 20D60 Arithmetic and combinatorial problems
- 20D99 None of the above, but in this section
- 20Exx Structure and classification of infinite or finite groups**
- 20E05 Free nonabelian groups
- 20E06 Free products, free products with amalgamation, Higman-Neumann-Neumann extensions, and generalizations
- 20E07 Subgroup theorems; subgroup growth
- 20E08 Groups acting on trees [See also 20F65]
- 20E10 Quasivarieties and varieties of groups
- 20E15 Chains and lattices of subgroups, subnormal subgroups  
[See also 20F22]
- 20E18 Limits, profinite groups
- 20E22 Extensions, wreath products, and other compositions [See also 20J05]
- 20E25 Local properties
- 20E26 Residual properties and generalizations; residually finite groups
- 20E28 Maximal subgroups
- 20E32 Simple groups [See also 20D05]
- 20E34 General structure theorems
- 20E36 Automorphisms of infinite groups [For automorphisms of finite groups, see 20D45]
- 20E42 Groups with a  $BN$ -pair; buildings [See also 51E24]
- 20E45 Conjugacy classes
- 20E99 None of the above, but in this section
- 20Fxx Special aspects of infinite or finite groups**
- 20F05 Generators, relations, and presentations
- 20F06 Cancellation theory; application of van Kampen diagrams  
[See also 57M05]
- 20F10 Word problems, other decision problems, connections with logic and automata [See also 03B25, 03D05, 03D40, 06B25, 08A50, 68Q70]
- 20F11 Groups of finite Morley rank [See also 03C45, 03C60]
- 20F12 Commutator calculus
- 20F14 Derived series, central series, and generalizations
- 20F16 Solvable groups, supersolvable groups [See also 20D10]
- 20F17 Formations of groups, Fitting classes [See also 20D10]
- 20F18 Nilpotent groups [See also 20D15]

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- 20F19 Generalizations of solvable and nilpotent groups
- 20F22 Other classes of groups defined by subgroup chains
- 20F24 FC-groups and their generalizations
- 20F28 Automorphism groups of groups [See also 20E36]
- 20F29 Representations of groups as automorphism groups of algebraic systems
- 20F34 Fundamental groups and their automorphisms [See also 57M05, 57Sxx]
- 20F36 Braid groups; Artin groups
- 20F38 Other groups related to topology or analysis
- 20F40 Associated Lie structures
- 20F45 Engel conditions
- 20F50 Periodic groups; locally finite groups
- 20F55 Reflection and Coxeter groups [See also 22E40, 51F15]
- 20F60 Ordered groups [See mainly 06F15]
- 20F65 Geometric group theory [See also 05C25, 20E08, 57Mxx]
- 20F67 Hyperbolic groups and nonpositively curved groups
- 20F69 Asymptotic properties of groups
- 20F70 Algebraic geometry over groups; equations over groups
- 20F99 None of the above, but in this section
- 20Gxx** **Linear algebraic groups and related topics**  $\{\{\}\}$  **For arithmetic theory, see 11E57, 11H56; for geometric theory, see 14Lxx, 22Exx; for other methods in representation theory, see 15A30, 22E45, 22E46, 22E47, 22E50, 22E55**
- 20G05 Representation theory
- 20G07 Structure theory
- 20G10 Cohomology theory
- 20G15 Linear algebraic groups over arbitrary fields
- 20G20 Linear algebraic groups over the reals, the complexes, the quaternions
- 20G25 Linear algebraic groups over local fields and their integers
- 20G30 Linear algebraic groups over global fields and their integers
- 20G35 Linear algebraic groups over adèles and other rings and schemes
- 20G40 Linear algebraic groups over finite fields
- 20G41 Exceptional groups
- 20G42 Quantum groups (quantized function algebras) and their representations [See also 16T20, 17B37, 81R50]
- 20G43 Schur and  $q$ -Schur algebras
- 20G44 Kac-Moody groups
- 20G45 Applications to physics
- 20G99 None of the above, but in this section
- 20Hxx** **Other groups of matrices** [See also 15A30]
- 20H05 Unimodular groups, congruence subgroups [See also 11F06, 19B37, 22E40, 51F20]
- 20H10 Fuchsian groups and their generalizations [See also 11F06, 22E40, 30F35, 32Nxx]
- 20H15 Other geometric groups, including crystallographic groups [See also 51-XX, especially 51F15, and 82D25]
- 20H20 Other matrix groups over fields
- 20H25 Other matrix groups over rings
- 20H30 Other matrix groups over finite fields
- 20H99 None of the above, but in this section

- 20Jxx** **Connections with homological algebra and category theory**
- 20J05 Homological methods in group theory
- 20J06 Cohomology of groups
- 20J15 Category of groups
- 20J99 None of the above, but in this section
- 20Kxx** **Abelian groups**
- 20K01 Finite abelian groups [For sumsets, see 11B13 and 11P70]
- 20K10 Torsion groups, primary groups and generalized primary groups
- 20K15 Torsion-free groups, finite rank
- 20K20 Torsion-free groups, infinite rank
- 20K21 Mixed groups
- 20K25 Direct sums, direct products, etc.
- 20K27 Subgroups
- 20K30 Automorphisms, homomorphisms, endomorphisms, etc.
- 20K35 Extensions
- 20K40 Homological and categorical methods
- 20K45 Topological methods [See also 22A05, 22B05]
- 20K99 None of the above, but in this section
- 20Lxx** **Groupoids (i.e. small categories in which all morphisms are isomorphisms)  $\{\{\}\}$ For sets with a single binary operation, see 20N02; for topological groupoids, see 22A22, 58H05**
- 20L05 Groupoids (i.e. small categories in which all morphisms are isomorphisms)  $\{\{\}\}$ For sets with a single binary operation, see 20N02; for topological groupoids, see 22A22, 58H05
- 20L99 None of the above, but in this section
- 20Mxx** **Semigroups**
- 20M05 Free semigroups, generators and relations, word problems
- 20M07 Varieties and pseudovarieties of semigroups
- 20M10 General structure theory
- 20M11 Radical theory
- 20M12 Ideal theory
- 20M13 Arithmetic theory of monoids
- 20M14 Commutative semigroups
- 20M15 Mappings of semigroups
- 20M17 Regular semigroups
- 20M18 Inverse semigroups
- 20M19 Orthodox semigroups
- 20M20 Semigroups of transformations, etc. [See also 47D03, 47H20, 54H15]
- 20M25 Semigroup rings, multiplicative semigroups of rings [See also 16S36, 16Y60]
- 20M30 Representation of semigroups; actions of semigroups on sets
- 20M32 Algebraic monoids
- 20M35 Semigroups in automata theory, linguistics, etc. [See also 03D05, 68Q70, 68T50]
- 20M50 Connections of semigroups with homological algebra and category theory
- 20M99 None of the above, but in this section
- 20Nxx** **Other generalizations of groups**
- 20N02 Sets with a single binary operation (groupoids)
- 20N05 Loops, quasigroups [See also 05Bxx]
- 20N10 Ternary systems (heaps, semiheaps, heapoids, etc.)

- 20N15  $n$ -ary systems ( $n \geq 3$ )
- 20N20 Hypergroups
- 20N25 Fuzzy groups [See also 03E72]
- 20N99 None of the above, but in this section
- 20Pxx Probabilistic methods in group theory [See also 60Bxx]**
- 20P05 Probabilistic methods in group theory [See also 60Bxx]
- 20P99 None of the above, but in this section
- 22–XX TOPOLOGICAL GROUPS, LIE GROUPS FOR TRANSFORMATION GROUPS, SEE 54H15, 57SXX, 58–XX. FOR ABSTRACT HARMONIC ANALYSIS, SEE 43–XX{}**
- 22–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 22–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 22–02 Research exposition (monographs, survey articles)
- 22–03 Historical (must also be assigned at least one classification number from Section 01)
- 22–04 Explicit machine computation and programs (not the theory of computation or programming)
- 22–06 Proceedings, conferences, collections, etc.
- 22Axx Topological and differentiable algebraic systems {{{}}For topological rings and fields, see 12Jxx, 13Jxx, 16W80**
- 22A05 Structure of general topological groups
- 22A10 Analysis on general topological groups
- 22A15 Structure of topological semigroups
- 22A20 Analysis on topological semigroups
- 22A22 Topological groupoids (including differentiable and Lie groupoids) [See also 58H05]
- 22A25 Representations of general topological groups and semigroups
- 22A26 Topological semilattices, lattices and applications [See also 06B30, 06B35, 06F30]
- 22A30 Other topological algebraic systems and their representations
- 22A99 None of the above, but in this section
- 22Bxx Locally compact abelian groups (LCA groups)**
- 22B05 General properties and structure of LCA groups
- 22B10 Structure of group algebras of LCA groups
- 22B99 None of the above, but in this section
- 22Cxx Compact groups**
- 22C05 Compact groups
- 22C99 None of the above, but in this section
- 22Dxx Locally compact groups and their algebras**
- 22D05 General properties and structure of locally compact groups
- 22D10 Unitary representations of locally compact groups
- 22D12 Other representations of locally compact groups
- 22D15 Group algebras of locally compact groups
- 22D20 Representations of group algebras
- 22D25  $C^*$ -algebras and  $W^*$ -algebras in relation to group representations [See also 46Lxx]
- 22D30 Induced representations
- 22D35 Duality theorems
- 22D40 Ergodic theory on groups [See also 28Dxx]
- 22D45 Automorphism groups of locally compact groups

- 22D99 None of the above, but in this section
- 22Exx Lie groups  $\{\{\}\}$ For the topology of Lie groups and homogeneous spaces, see 57Sxx, 57Txx; for analysis thereon, see 43A80, 43A85, 43A90**
- 22E05 Local Lie groups [See also 34–XX, 35–XX, 58H05]
- 22E10 General properties and structure of complex Lie groups  
[See also 32M05]
- 22E15 General properties and structure of real Lie groups
- 22E20 General properties and structure of other Lie groups
- 22E25 Nilpotent and solvable Lie groups
- 22E27 Representations of nilpotent and solvable Lie groups (special orbital integrals, non-type I representations, etc.)
- 22E30 Analysis on real and complex Lie groups [See also 33C80, 43–XX]
- 22E35 Analysis on  $p$ -adic Lie groups
- 22E40 Discrete subgroups of Lie groups [See also 20Hxx, 32Nxx]
- 22E41 Continuous cohomology [See also 57R32, 57Txx, 58H10]
- 22E43 Structure and representation of the Lorentz group
- 22E45 Representations of Lie and linear algebraic groups over real fields: analytic methods  $\{\{\}\}$ For the purely algebraic theory, see 20G05
- 22E46 Semisimple Lie groups and their representations
- 22E47 Representations of Lie and real algebraic groups: algebraic methods (Verma modules, etc.) [See also 17B10]
- 22E50 Representations of Lie and linear algebraic groups over local fields  
[See also 20G05]
- 22E55 Representations of Lie and linear algebraic groups over global fields and adèle rings [See also 20G05]
- 22E57 Geometric Langlands program: representation-theoretic aspects  
[See also 14D24]
- 22E60 Lie algebras of Lie groups  $\{\{\}\}$ For the algebraic theory of Lie algebras, see 17Bxx
- 22E65 Infinite-dimensional Lie groups and their Lie algebras: general properties [See also 17B65, 58B25, 58H05]
- 22E66 Analysis on and representations of infinite-dimensional Lie groups
- 22E67 Loop groups and related constructions, group-theoretic treatment  
[See also 58D05]
- 22E70 Applications of Lie groups to physics; explicit representations  
[See also 81R05, 81R10]
- 22E99 None of the above, but in this section
- 22Fxx Noncompact transformation groups**
- 22F05 General theory of group and pseudogroup actions  $\{\{\}\}$ For topological properties of spaces with an action, see 57S20
- 22F10 Measurable group actions [See also 22D40, 28Dxx, 37Axx]
- 22F30 Homogeneous spaces  $\{\{\}\}$ For general actions on manifolds or preserving geometrical structures, see 57M60, 57Sxx; for discrete subgroups of Lie groups, see especially 22E40
- 22F50 Groups as automorphisms of other structures
- 22F99 None of the above, but in this section
- 26–XX REAL FUNCTIONS [See also 54C30]**
- 26–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 26–01 Instructional exposition (textbooks, tutorial papers, etc.)

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- 26–02 Research exposition (monographs, survey articles)
- 26–03 Historical (must also be assigned at least one classification number from Section 01)
- 26–04 Explicit machine computation and programs (not the theory of computation or programming)
- 26–06 Proceedings, conferences, collections, etc.
- 26Axx Functions of one variable**
- 26A03 Foundations: limits and generalizations, elementary topology of the line
- 26A06 One-variable calculus
- 26A09 Elementary functions
- 26A12 Rate of growth of functions, orders of infinity, slowly varying functions [See also 26A48]
- 26A15 Continuity and related questions (modulus of continuity, semicontinuity, discontinuities, etc.)  $\{\{\}\}$ For properties determined by Fourier coefficients, see 42A16; for those determined by approximation properties, see 41A25, 41A27
- 26A16 Lipschitz (Hölder) classes
- 26A18 Iteration [See also 37Bxx, 37Cxx, 37Exx, 39B12, 47H10, 54H25]
- 26A21 Classification of real functions; Baire classification of sets and functions [See also 03E15, 28A05, 54C50]
- 26A24 Differentiation (functions of one variable): general theory, generalized derivatives, mean-value theorems [See also 28A15]
- 26A27 Nondifferentiability (nondifferentiable functions, points of nondifferentiability), discontinuous derivatives
- 26A30 Singular functions, Cantor functions, functions with other special properties
- 26A33 Fractional derivatives and integrals
- 26A36 Antidifferentiation
- 26A39 Denjoy and Perron integrals, other special integrals
- 26A42 Integrals of Riemann, Stieltjes and Lebesgue type [See also 28–XX]
- 26A45 Functions of bounded variation, generalizations
- 26A46 Absolutely continuous functions
- 26A48 Monotonic functions, generalizations
- 26A51 Convexity, generalizations
- 26A99 None of the above, but in this section
- 26Bxx Functions of several variables**
- 26B05 Continuity and differentiation questions
- 26B10 Implicit function theorems, Jacobians, transformations with several variables
- 26B12 Calculus of vector functions
- 26B15 Integration: length, area, volume [See also 28A75, 51M25]
- 26B20 Integral formulas (Stokes, Gauss, Green, etc.)
- 26B25 Convexity, generalizations
- 26B30 Absolutely continuous functions, functions of bounded variation
- 26B35 Special properties of functions of several variables, Hölder conditions, etc.
- 26B40 Representation and superposition of functions
- 26B99 None of the above, but in this section
- 26Cxx Polynomials, rational functions**
- 26C05 Polynomials: analytic properties, etc. [See also 12Dxx, 12Exx]

- 26C10 Polynomials: location of zeros [See also 12D10, 30C15, 65H05]
- 26C15 Rational functions [See also 14Pxx]
- 26C99 None of the above, but in this section
- 26Dxx Inequalities** {{{}}For maximal function inequalities, see **42B25**; for functional inequalities, see **39B72**; for probabilistic inequalities, see **60E15**
- 26D05 Inequalities for trigonometric functions and polynomials
- 26D07 Inequalities involving other types of functions
- 26D10 Inequalities involving derivatives and differential and integral operators
- 26D15 Inequalities for sums, series and integrals
- 26D20 Other analytical inequalities
- 26D99 None of the above, but in this section
- 26Exx Miscellaneous topics** [See also **58Cxx**]
- 26E05 Real-analytic functions [See also 32B05, 32C05]
- 26E10  $C^\infty$ -functions, quasi-analytic functions [See also 58C25]
- 26E15 Calculus of functions on infinite-dimensional spaces [See also 46G05, 58Cxx]
- 26E20 Calculus of functions taking values in infinite-dimensional spaces [See also 46E40, 46G10, 58Cxx]
- 26E25 Set-valued functions [See also 28B20, 54C60] {{{}}For nonsmooth analysis, see 49J52, 58Cxx, 90Cxx
- 26E30 Non-Archimedean analysis [See also 12J25]
- 26E35 Nonstandard analysis [See also 03H05, 28E05, 54J05]
- 26E40 Constructive real analysis [See also 03F60]
- 26E50 Fuzzy real analysis [See also 03E72, 28E10]
- 26E60 Means [See also 47A64]
- 26E70 Real analysis on time scales or measure chains {{{}}For dynamic equations on time scales or measure chains see 34N05
- 26E99 None of the above, but in this section
- 28–XX MEASURE AND INTEGRATION FOR ANALYSIS ON MANIFOLDS, SEE 58–XX**{}
  - 28–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
  - 28–01 Instructional exposition (textbooks, tutorial papers, etc.)
  - 28–02 Research exposition (monographs, survey articles)
  - 28–03 Historical (must also be assigned at least one classification number from Section 01)
  - 28–04 Explicit machine computation and programs (not the theory of computation or programming)
  - 28–06 Proceedings, conferences, collections, etc.
  - 28Axx Classical measure theory**
  - 28A05 Classes of sets (Borel fields,  $\sigma$ -rings, etc.), measurable sets, Suslin sets, analytic sets [See also 03E15, 26A21, 54H05]
  - 28A10 Real- or complex-valued set functions
  - 28A12 Contents, measures, outer measures, capacities
  - 28A15 Abstract differentiation theory, differentiation of set functions [See also 26A24]
  - 28A20 Measurable and nonmeasurable functions, sequences of measurable functions, modes of convergence
  - 28A25 Integration with respect to measures and other set functions

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- 28A33 Spaces of measures, convergence of measures [See also 46E27, 60Bxx]
- 28A35 Measures and integrals in product spaces
- 28A50 Integration and disintegration of measures
- 28A51 Lifting theory [See also 46G15]
- 28A60 Measures on Boolean rings, measure algebras [See also 54H10]
- 28A75 Length, area, volume, other geometric measure theory  
[See also 26B15, 49Q15]
- 28A78 Hausdorff and packing measures
- 28A80 Fractals [See also 37Fxx]
- 28A99 None of the above, but in this section
- 28Bxx Set functions, measures and integrals with values in abstract spaces**
- 28B05 Vector-valued set functions, measures and integrals [See also 46G10]
- 28B10 Group- or semigroup-valued set functions, measures and integrals
- 28B15 Set functions, measures and integrals with values in ordered spaces
- 28B20 Set-valued set functions and measures; integration of set-valued  
functions; measurable selections [See also 26E25, 54C60, 54C65,  
91B14]
- 28B99 None of the above, but in this section
- 28Cxx Set functions and measures on spaces with additional structure**  
**[See also 46G12, 58C35, 58D20]**
- 28C05 Integration theory via linear functionals (Radon measures, Daniell  
integrals, etc.), representing set functions and measures
- 28C10 Set functions and measures on topological groups or semigroups,  
Haar measures, invariant measures [See also 22Axx, 43A05]
- 28C15 Set functions and measures on topological spaces (regularity of  
measures, etc.)
- 28C20 Set functions and measures and integrals in infinite-dimensional  
spaces (Wiener measure, Gaussian measure, etc.) [See also 46G12,  
58C35, 58D20, 60B11]
- 28C99 None of the above, but in this section
- 28Dxx Measure-theoretic ergodic theory [See also 11K50, 11K55, 22D40,**  
**37Axx, 47A35, 54H20, 60Fxx, 60G10]**
- 28D05 Measure-preserving transformations
- 28D10 One-parameter continuous families of measure-preserving  
transformations
- 28D15 General groups of measure-preserving transformations
- 28D20 Entropy and other invariants
- 28D99 None of the above, but in this section
- 28Exx Miscellaneous topics in measure theory**
- 28E05 Nonstandard measure theory [See also 03H05, 26E35]
- 28E10 Fuzzy measure theory [See also 03E72, 26E50, 94D05]
- 28E15 Other connections with logic and set theory
- 28E99 None of the above, but in this section
- 30–XX FUNCTIONS OF A COMPLEX VARIABLE FOR ANALYSIS ON**  
**MANIFOLDS, SEE 58–XX{}**
- 30–00 General reference works (handbooks, dictionaries, bibliographies,  
etc.)
- 30–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 30–02 Research exposition (monographs, survey articles)
- 30–03 Historical (must also be assigned at least one classification number  
from Section 01)

- 30–04 Explicit machine computation and programs (not the theory of computation or programming)
- 30–06 Proceedings, conferences, collections, etc.
- 30Axx General properties**
- 30A05 Monogenic properties of complex functions (including polygenic and areolar monogenic functions)
- 30A10 Inequalities in the complex domain
- 30A99 None of the above, but in this section
- 30Bxx Series expansions**
- 30B10 Power series (including lacunary series)
- 30B20 Random power series
- 30B30 Boundary behavior of power series, over-convergence
- 30B40 Analytic continuation
- 30B50 Dirichlet series and other series expansions, exponential series  
[See also 11M41, 42–XX]
- 30B60 Completeness problems, closure of a system of functions
- 30B70 Continued fractions [See also 11A55, 40A15]
- 30B99 None of the above, but in this section
- 30Cxx Geometric function theory**
- 30C10 Polynomials
- 30C15 Zeros of polynomials, rational functions, and other analytic functions (e.g. zeros of functions with bounded Dirichlet integral)  $\{\{\}\}$ For algebraic theory, see 12D10; for real methods, see 26C10
- 30C20 Conformal mappings of special domains
- 30C25 Covering theorems in conformal mapping theory
- 30C30 Numerical methods in conformal mapping theory [See also 65E05]
- 30C35 General theory of conformal mappings
- 30C40 Kernel functions and applications
- 30C45 Special classes of univalent and multivalent functions (starlike, convex, bounded rotation, etc.)
- 30C50 Coefficient problems for univalent and multivalent functions
- 30C55 General theory of univalent and multivalent functions
- 30C62 Quasiconformal mappings in the plane
- 30C65 Quasiconformal mappings in  $\mathbf{R}^n$ , other generalizations
- 30C70 Extremal problems for conformal and quasiconformal mappings, variational methods
- 30C75 Extremal problems for conformal and quasiconformal mappings, other methods
- 30C80 Maximum principle; Schwarz’s lemma, Lindelöf principle, analogues and generalizations; subordination
- 30C85 Capacity and harmonic measure in the complex plane  
[See also 31A15]
- 30C99 None of the above, but in this section
- 30Dxx Entire and meromorphic functions, and related topics**
- 30D05 Functional equations in the complex domain, iteration and composition of analytic functions [See also 34Mxx, 37Fxx, 39–XX]
- 30D10 Representations of entire functions by series and integrals
- 30D15 Special classes of entire functions and growth estimates
- 30D20 Entire functions, general theory
- 30D30 Meromorphic functions, general theory
- 30D35 Distribution of values, Nevanlinna theory

- 30D40 Cluster sets, prime ends, boundary behavior
- 30D45 Bloch functions, normal functions, normal families
- 30D60 Quasi-analytic and other classes of functions
- 30D99 None of the above, but in this section
- 30Exx Miscellaneous topics of analysis in the complex domain**
- 30E05 Moment problems, interpolation problems
- 30E10 Approximation in the complex domain
- 30E15 Asymptotic representations in the complex domain
- 30E20 Integration, integrals of Cauchy type, integral representations of analytic functions [See also 45Exx]
- 30E25 Boundary value problems [See also 45Exx]
- 30E99 None of the above, but in this section
- 30Fxx Riemann surfaces**
- 30F10 Compact Riemann surfaces and uniformization [See also 14H15, 32G15]
- 30F15 Harmonic functions on Riemann surfaces
- 30F20 Classification theory of Riemann surfaces
- 30F25 Ideal boundary theory
- 30F30 Differentials on Riemann surfaces
- 30F35 Fuchsian groups and automorphic functions [See also 11Fxx, 20H10, 22E40, 32Gxx, 32Nxx]
- 30F40 Kleinian groups [See also 20H10]
- 30F45 Conformal metrics (hyperbolic, Poincaré, distance functions)
- 30F50 Klein surfaces
- 30F60 Teichmüller theory [See also 32G15]
- 30F99 None of the above, but in this section
- 30Gxx Generalized function theory**
- 30G06 Non-Archimedean function theory [See also 12J25]; nonstandard function theory [See also 03H05]
- 30G12 Finely holomorphic functions and topological function theory
- 30G20 Generalizations of Bers or Vekua type (pseudoanalytic,  $p$ -analytic, etc.)
- 30G25 Discrete analytic functions
- 30G30 Other generalizations of analytic functions (including abstract-valued functions)
- 30G35 Functions of hypercomplex variables and generalized variables
- 30G99 None of the above, but in this section
- 30Hxx Spaces and algebras of analytic functions**
- 30H05 Bounded analytic functions
- 30H10 Hardy spaces
- 30H15 Nevanlinna class and Smirnov class
- 30H20 Bergman spaces, Fock spaces
- 30H25 Besov spaces and  $Q_p$ -spaces
- 30H30 Bloch spaces
- 30H35 BMO-spaces
- 30H50 Algebras of analytic functions
- 30H80 Corona theorems
- 30H99 None of the above, but in this section
- 30Jxx Function theory on the disc**
- 30J05 Inner functions
- 30J10 Blaschke products

- 30J15 Singular inner functions
- 30J99 None of the above, but in this section
- 30Kxx Universal holomorphic functions**
- 30K05 Universal Taylor series
- 30K10 Universal Dirichlet series
- 30K15 Bounded universal functions
- 30K20 Compositional universality
- 30K99 None of the above, but in this section
- 30Lxx Analysis on metric spaces**
- 30L05 Geometric embeddings of metric spaces
- 30L10 Quasiconformal mappings in metric spaces
- 30L99 None of the above, but in this section
- 31–XX POTENTIAL THEORY FOR PROBABILISTIC POTENTIAL THEORY, SEE 60J45{}**
- 31–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 31–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 31–02 Research exposition (monographs, survey articles)
- 31–03 Historical (must also be assigned at least one classification number from Section 01)
- 31–04 Explicit machine computation and programs (not the theory of computation or programming)
- 31–06 Proceedings, conferences, collections, etc.
- 31Axx Two-dimensional theory**
- 31A05 Harmonic, subharmonic, superharmonic functions
- 31A10 Integral representations, integral operators, integral equations methods
- 31A15 Potentials and capacity, harmonic measure, extremal length [See also 30C85]
- 31A20 Boundary behavior (theorems of Fatou type, etc.)
- 31A25 Boundary value and inverse problems
- 31A30 Biharmonic, polyharmonic functions and equations, Poisson's equation
- 31A35 Connections with differential equations
- 31A99 None of the above, but in this section
- 31Bxx Higher-dimensional theory**
- 31B05 Harmonic, subharmonic, superharmonic functions
- 31B10 Integral representations, integral operators, integral equations methods
- 31B15 Potentials and capacities, extremal length
- 31B20 Boundary value and inverse problems
- 31B25 Boundary behavior
- 31B30 Biharmonic and polyharmonic equations and functions
- 31B35 Connections with differential equations
- 31B99 None of the above, but in this section
- 31Cxx Other generalizations**
- 31C05 Harmonic, subharmonic, superharmonic functions
- 31C10 Pluriharmonic and plurisubharmonic functions [See also 32U05]
- 31C12 Potential theory on Riemannian manifolds [See also 53C20; for Hodge theory, see 58A14]
- 31C15 Potentials and capacities

- 31C20 Discrete potential theory and numerical methods
- 31C25 Dirichlet spaces
- 31C35 Martin boundary theory [See also 60J50]
- 31C40 Fine potential theory
- 31C45 Other generalizations (nonlinear potential theory, etc.)
- 31C99 None of the above, but in this section
- 31Dxx Axiomatic potential theory**
- 31D05 Axiomatic potential theory
- 31D99 None of the above, but in this section
- 31Exx Potential theory on metric spaces**
- 31E05 Potential theory on metric spaces
- 31E99 None of the above, but in this section
- 32–XX SEVERAL COMPLEX VARIABLES AND ANALYTIC SPACES FOR INFINITE-DIMENSIONAL HOLOMORPHY, SEE 46G20, 58B12{}**
- 32–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 32–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 32–02 Research exposition (monographs, survey articles)
- 32–03 Historical (must also be assigned at least one classification number from Section 01)
- 32–04 Explicit machine computation and programs (not the theory of computation or programming)
- 32–06 Proceedings, conferences, collections, etc.
- 32Axx Holomorphic functions of several complex variables**
- 32A05 Power series, series of functions
- 32A07 Special domains (Reinhardt, Hartogs, circular, tube)
- 32A10 Holomorphic functions
- 32A12 Multifunctions
- 32A15 Entire functions
- 32A17 Special families of functions
- 32A18 Bloch functions, normal functions
- 32A19 Normal families of functions, mappings
- 32A20 Meromorphic functions
- 32A22 Nevanlinna theory (local); growth estimates; other inequalities  
 {{{}}For geometric theory, see 32H25, 32H30
- 32A25 Integral representations; canonical kernels (Szegő, Bergman, etc.)
- 32A26 Integral representations, constructed kernels (e.g. Cauchy, Fantappiè-type kernels)
- 32A27 Local theory of residues [See also 32C30]
- 32A30 Other generalizations of function theory of one complex variable (should also be assigned at least one classification number from Section 30) {{{}}For functions of several hypercomplex variables, see 30G35
- 32A35  $H^p$ -spaces, Nevanlinna spaces [See also 32M15, 42B30, 43A85, 46J15]
- 32A36 Bergman spaces
- 32A37 Other spaces of holomorphic functions (e.g. bounded mean oscillation (BMOA), vanishing mean oscillation (VMOA)) [See also 46Exx]
- 32A38 Algebras of holomorphic functions [See also 30H05, 46J10, 46J15]
- 32A40 Boundary behavior of holomorphic functions
- 32A45 Hyperfunctions [See also 46F15]

- 32A50 Harmonic analysis of several complex variables [See mainly 43–XX]
- 32A55 Singular integrals
- 32A60 Zero sets of holomorphic functions
- 32A65 Banach algebra techniques [See mainly 46Jxx]
- 32A70 Functional analysis techniques [See mainly 46Exx]
- 32A99 None of the above, but in this section
- 32Bxx Local analytic geometry [See also 13–XX and 14–XX]**
- 32B05 Analytic algebras and generalizations, preparation theorems
- 32B10 Germs of analytic sets, local parametrization
- 32B15 Analytic subsets of affine space
- 32B20 Semi-analytic sets and subanalytic sets [See also 14P15]
- 32B25 Triangulation and related questions
- 32B99 None of the above, but in this section
- 32Cxx Analytic spaces**
- 32C05 Real-analytic manifolds, real-analytic spaces [See also 14Pxx, 58A07]
- 32C07 Real-analytic sets, complex Nash functions [See also 14P15, 14P20]
- 32C09 Embedding of real analytic manifolds
- 32C11 Complex supergeometry [See also 14A22, 14M30, 58A50]
- 32C15 Complex spaces
- 32C18 Topology of analytic spaces
- 32C20 Normal analytic spaces
- 32C22 Embedding of analytic spaces
- 32C25 Analytic subsets and submanifolds
- 32C30 Integration on analytic sets and spaces, currents  $\{\{\}\}$ For local theory, see 32A25 or 32A27
- 32C35 Analytic sheaves and cohomology groups [See also 14Fxx, 18F20, 55N30]
- 32C36 Local cohomology of analytic spaces
- 32C37 Duality theorems
- 32C38 Sheaves of differential operators and their modules,  $D$ -modules [See also 14F10, 16S32, 35A27, 58J15]
- 32C55 The Levi problem in complex spaces; generalizations
- 32C81 Applications to physics
- 32C99 None of the above, but in this section
- 32Dxx Analytic continuation**
- 32D05 Domains of holomorphy
- 32D10 Envelopes of holomorphy
- 32D15 Continuation of analytic objects
- 32D20 Removable singularities
- 32D26 Riemann domains
- 32D99 None of the above, but in this section
- 32Exx Holomorphic convexity**
- 32E05 Holomorphically convex complex spaces, reduction theory
- 32E10 Stein spaces, Stein manifolds
- 32E20 Polynomial convexity
- 32E30 Holomorphic and polynomial approximation, Runge pairs, interpolation
- 32E35 Global boundary behavior of holomorphic functions
- 32E40 The Levi problem
- 32E99 None of the above, but in this section

- 32Fxx Geometric convexity**
- 32F10 *q*-convexity, *q*-concavity
- 32F17 Other notions of convexity
- 32F18 Finite-type conditions
- 32F27 Topological consequences of geometric convexity
- 32F32 Analytical consequences of geometric convexity (vanishing theorems, etc.)
- 32F45 Invariant metrics and pseudodistances
- 32F99 None of the above, but in this section
- 32Gxx Deformations of analytic structures**
- 32G05 Deformations of complex structures [See also 13D10, 16S80, 58H10, 58H15]
- 32G07 Deformations of special (e.g. CR) structures
- 32G08 Deformations of fiber bundles
- 32G10 Deformations of submanifolds and subspaces
- 32G13 Analytic moduli problems  $\{\{\}\}$ For algebraic moduli problems, see 14D20, 14D22, 14H10, 14J10 [See also 14H15, 14J15]
- 32G15 Moduli of Riemann surfaces, Teichmüller theory [See also 14H15, 30Fxx]
- 32G20 Period matrices, variation of Hodge structure; degenerations [See also 14D05, 14D07, 14K30]
- 32G34 Moduli and deformations for ordinary differential equations (e.g. Knizhnik-Zamolodchikov equation) [See also 34Mxx]
- 32G81 Applications to physics
- 32G99 None of the above, but in this section
- 32Hxx Holomorphic mappings and correspondences**
- 32H02 Holomorphic mappings, (holomorphic) embeddings and related questions
- 32H04 Meromorphic mappings
- 32H12 Boundary uniqueness of mappings
- 32H25 Picard-type theorems and generalizations  $\{\{\}\}$ For function-theoretic properties, see 32A22
- 32H30 Value distribution theory in higher dimensions  $\{\{\}\}$ For function-theoretic properties, see 32A22
- 32H35 Proper mappings, finiteness theorems
- 32H40 Boundary regularity of mappings
- 32H50 Iteration problems
- 32H99 None of the above, but in this section
- 32Jxx Compact analytic spaces  $\{\{\}\}$ For Riemann surfaces, see 14Hxx, 30Fxx; for algebraic theory, see 14Jxx**
- 32J05 Compactification of analytic spaces
- 32J10 Algebraic dependence theorems
- 32J15 Compact surfaces
- 32J17 Compact 3-folds
- 32J18 Compact *n*-folds
- 32J25 Transcendental methods of algebraic geometry [See also 14C30]
- 32J27 Compact Kähler manifolds: generalizations, classification
- 32J81 Applications to physics
- 32J99 None of the above, but in this section

- 32Kxx**    **Generalizations of analytic spaces (should also be assigned at least one other classification number from Section 32 describing the type of problem)**
- 32K05    Banach analytic spaces [See also 58Bxx]
- 32K07    Formal and graded complex spaces [See also 58C50]
- 32K15    Differentiable functions on analytic spaces, differentiable spaces [See also 58C25]
- 32K99    None of the above, but in this section
- 32Lxx**    **Holomorphic fiber spaces [See also 55Rxx]**
- 32L05    Holomorphic bundles and generalizations
- 32L10    Sheaves and cohomology of sections of holomorphic vector bundles, general results [See also 14F05, 18F20, 55N30]
- 32L15    Bundle convexity [See also 32F10]
- 32L20    Vanishing theorems
- 32L25    Twistor theory, double fibrations [See also 53C28]
- 32L81    Applications to physics
- 32L99    None of the above, but in this section
- 32Mxx**    **Complex spaces with a group of automorphisms**
- 32M05    Complex Lie groups, automorphism groups acting on complex spaces [See also 22E10]
- 32M10    Homogeneous complex manifolds [See also 14M17, 57T15]
- 32M12    Almost homogeneous manifolds and spaces [See also 14M17]
- 32M15    Hermitian symmetric spaces, bounded symmetric domains, Jordan algebras [See also 22E10, 22E40, 53C35, 57T15]
- 32M17    Automorphism groups of  $\mathbf{C}^n$  and affine manifolds
- 32M25    Complex vector fields
- 32M99    None of the above, but in this section
- 32Nxx**    **Automorphic functions [See also 11Fxx, 20H10, 22E40, 30F35]**
- 32N05    General theory of automorphic functions of several complex variables
- 32N10    Automorphic forms
- 32N15    Automorphic functions in symmetric domains
- 32N99    None of the above, but in this section
- 32Pxx**    **Non-Archimedean analysis (should also be assigned at least one other classification number from Section 32 describing the type of problem)**
- 32P05    Non-Archimedean analysis (should also be assigned at least one other classification number from Section 32 describing the type of problem)
- 32P99    None of the above, but in this section
- 32Qxx**    **Complex manifolds**
- 32Q05    Negative curvature manifolds
- 32Q10    Positive curvature manifolds
- 32Q15    Kähler manifolds
- 32Q20    Kähler-Einstein manifolds [See also 53Cxx]
- 32Q25    Calabi-Yau theory [See also 14J30]
- 32Q26    Notions of stability
- 32Q28    Stein manifolds
- 32Q30    Uniformization
- 32Q35    Complex manifolds as subdomains of Euclidean space
- 32Q40    Embedding theorems
- 32Q45    Hyperbolic and Kobayashi hyperbolic manifolds
- 32Q55    Topological aspects of complex manifolds

- 32Q57 Classification theorems
- 32Q60 Almost complex manifolds
- 32Q65 Pseudoholomorphic curves
- 32Q99 None of the above, but in this section
- 32Sxx Singularities [See also 58Kxx]**
- 32S05 Local singularities [See also 14J17]
- 32S10 Invariants of analytic local rings
- 32S15 Equisingularity (topological and analytic) [See also 14E15]
- 32S20 Global theory of singularities; cohomological properties  
[See also 14E15]
- 32S22 Relations with arrangements of hyperplanes [See also 52C35]
- 32S25 Surface and hypersurface singularities [See also 14J17]
- 32S30 Deformations of singularities; vanishing cycles [See also 14B07]
- 32S35 Mixed Hodge theory of singular varieties [See also 14C30, 14D07]
- 32S40 Monodromy; relations with differential equations and  $D$ -modules
- 32S45 Modifications; resolution of singularities [See also 14E15]
- 32S50 Topological aspects: Lefschetz theorems, topological classification,  
invariants
- 32S55 Milnor fibration; relations with knot theory [See also 57M25, 57Q45]
- 32S60 Stratifications; constructible sheaves; intersection cohomology  
[See also 58Kxx]
- 32S65 Singularities of holomorphic vector fields and foliations
- 32S70 Other operations on singularities
- 32S99 None of the above, but in this section
- 32Txx Pseudoconvex domains**
- 32T05 Domains of holomorphy
- 32T15 Strongly pseudoconvex domains
- 32T20 Worm domains
- 32T25 Finite type domains
- 32T27 Geometric and analytic invariants on weakly pseudoconvex  
boundaries
- 32T35 Exhaustion functions
- 32T40 Peak functions
- 32T99 None of the above, but in this section
- 32Uxx Pluripotential theory**
- 32U05 Plurisubharmonic functions and generalizations [See also 31C10]
- 32U10 Plurisubharmonic exhaustion functions
- 32U15 General pluripotential theory
- 32U20 Capacity theory and generalizations
- 32U25 Lelong numbers
- 32U30 Removable sets
- 32U35 Pluricomplex Green functions
- 32U40 Currents
- 32U99 None of the above, but in this section
- 32Vxx CR manifolds**
- 32V05 CR structures, CR operators, and generalizations
- 32V10 CR functions
- 32V15 CR manifolds as boundaries of domains
- 32V20 Analysis on CR manifolds
- 32V25 Extension of functions and other analytic objects from CR manifolds
- 32V30 Embeddings of CR manifolds

- 32V35 Finite type conditions on CR manifolds
- 32V40 Real submanifolds in complex manifolds
- 32V99 None of the above, but in this section
- 32Wxx Differential operators in several variables**
- 32W05  $\bar{\partial}$  and  $\bar{\partial}$ -Neumann operators
- 32W10  $\bar{\partial}_b$  and  $\bar{\partial}_b$ -Neumann operators
- 32W20 Complex Monge-Ampère operators
- 32W25 Pseudodifferential operators in several complex variables
- 32W30 Heat kernels in several complex variables
- 32W50 Other partial differential equations of complex analysis
- 32W99 None of the above, but in this section
- 33–XX SPECIAL FUNCTIONS (33–XX DEALS WITH THE PROPERTIES OF FUNCTIONS AS FUNCTIONS) FOR ORTHOGONAL FUNCTIONS, SEE 42CXX; FOR ASPECTS OF COMBINATORICS SEE 05AXX; FOR NUMBER-THEORETIC ASPECTS SEE 11–XX; FOR REPRESENTATION THEORY SEE 22EXX{}**
- 33–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 33–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 33–02 Research exposition (monographs, survey articles)
- 33–03 Historical (must also be assigned at least one classification number from Section 01)
- 33–04 Explicit machine computation and programs (not the theory of computation or programming)
- 33–06 Proceedings, conferences, collections, etc.
- 33Bxx Elementary classical functions**
- 33B10 Exponential and trigonometric functions
- 33B15 Gamma, beta and polygamma functions
- 33B20 Incomplete beta and gamma functions (error functions, probability integral, Fresnel integrals)
- 33B30 Higher logarithm functions
- 33B99 None of the above, but in this section
- 33Cxx Hypergeometric functions**
- 33C05 Classical hypergeometric functions,  ${}_2F_1$
- 33C10 Bessel and Airy functions, cylinder functions,  ${}_0F_1$
- 33C15 Confluent hypergeometric functions, Whittaker functions,  ${}_1F_1$
- 33C20 Generalized hypergeometric series,  ${}_pF_q$
- 33C45 Orthogonal polynomials and functions of hypergeometric type (Jacobi, Laguerre, Hermite, Askey scheme, etc.) [See also 42C05 for general orthogonal polynomials and functions]
- 33C47 Other special orthogonal polynomials and functions
- 33C50 Orthogonal polynomials and functions in several variables expressible in terms of special functions in one variable
- 33C52 Orthogonal polynomials and functions associated with root systems
- 33C55 Spherical harmonics
- 33C60 Hypergeometric integrals and functions defined by them ( $E$ ,  $G$ ,  $H$  and  $I$  functions)
- 33C65 Appell, Horn and Lauricella functions
- 33C67 Hypergeometric functions associated with root systems
- 33C70 Other hypergeometric functions and integrals in several variables

- 33C75 Elliptic integrals as hypergeometric functions
- 33C80 Connections with groups and algebras, and related topics
- 33C90 Applications
- 33C99 None of the above, but in this section
- 33Dxx Basic hypergeometric functions**
- 33D05  $q$ -gamma functions,  $q$ -beta functions and integrals
- 33D15 Basic hypergeometric functions in one variable,  ${}_r\varphi_s$
- 33D45 Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.)
- 33D50 Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable
- 33D52 Basic orthogonal polynomials and functions associated with root systems (Macdonald polynomials, etc.)
- 33D60 Basic hypergeometric integrals and functions defined by them
- 33D65 Bibasic functions and multiple bases
- 33D67 Basic hypergeometric functions associated with root systems
- 33D70 Other basic hypergeometric functions and integrals in several variables
- 33D80 Connections with quantum groups, Chevalley groups,  $p$ -adic groups, Hecke algebras, and related topics
- 33D90 Applications
- 33D99 None of the above, but in this section
- 33Exx Other special functions**
- 33E05 Elliptic functions and integrals
- 33E10 Lamé, Mathieu, and spheroidal wave functions
- 33E12 Mittag-Leffler functions and generalizations
- 33E15 Other wave functions
- 33E17 Painlevé-type functions
- 33E20 Other functions defined by series and integrals
- 33E30 Other functions coming from differential, difference and integral equations
- 33E50 Special functions in characteristic  $p$  (gamma functions, etc.)
- 33E99 None of the above, but in this section
- 33Fxx Computational aspects**
- 33F05 Numerical approximation and evaluation [See also 65D20]
- 33F10 Symbolic computation (Gosper and Zeilberger algorithms, etc.) [See also 68W30]
- 33F99 None of the above, but in this section
- 34–XX ORDINARY DIFFERENTIAL EQUATIONS**
- 34–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 34–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 34–02 Research exposition (monographs, survey articles)
- 34–03 Historical (must also be assigned at least one classification number from Section 01)
- 34–04 Explicit machine computation and programs (not the theory of computation or programming)
- 34–06 Proceedings, conferences, collections, etc.
- 34Axx General theory**
- 34A05 Explicit solutions and reductions
- 34A07 Fuzzy differential equations

- 34A08 Fractional differential equations
- 34A09 Implicit equations, differential-algebraic equations [See also 65L80]
- 34A12 Initial value problems, existence, uniqueness, continuous dependence and continuation of solutions
- 34A25 Analytical theory: series, transformations, transforms, operational calculus, etc. [See also 44–XX]
- 34A26 Geometric methods in differential equations
- 34A30 Linear equations and systems, general
- 34A33 Lattice differential equations
- 34A34 Nonlinear equations and systems, general
- 34A35 Differential equations of infinite order
- 34A36 Discontinuous equations
- 34A37 Differential equations with impulses
- 34A38 Hybrid systems
- 34A40 Differential inequalities [See also 26D20]
- 34A45 Theoretical approximation of solutions  $\{\{\}\}$ For numerical analysis, see 65Lxx
- 34A55 Inverse problems
- 34A60 Differential inclusions [See also 49J21, 49K21]
- 34A99 None of the above, but in this section
- 34Bxx** **Boundary value problems  $\{\{\}\}$ For ordinary differential operators, see 34Lxx**
- 34B05 Linear boundary value problems
- 34B07 Linear boundary value problems with nonlinear dependence on the spectral parameter
- 34B08 Parameter dependent boundary value problems
- 34B09 Boundary eigenvalue problems
- 34B10 Nonlocal and multipoint boundary value problems
- 34B15 Nonlinear boundary value problems
- 34B16 Singular nonlinear boundary value problems
- 34B18 Positive solutions of nonlinear boundary value problems
- 34B20 Weyl theory and its generalizations
- 34B24 Sturm-Liouville theory [See also 34Lxx]
- 34B27 Green functions
- 34B30 Special equations (Mathieu, Hill, Bessel, etc.)
- 34B37 Boundary value problems with impulses
- 34B40 Boundary value problems on infinite intervals
- 34B45 Boundary value problems on graphs and networks
- 34B60 Applications
- 34B99 None of the above, but in this section
- 34Cxx** **Qualitative theory [See also 37–XX]**
- 34C05 Location of integral curves, singular points, limit cycles
- 34C07 Theory of limit cycles of polynomial and analytic vector fields (existence, uniqueness, bounds, Hilbert’s 16th problem and ramifications)
- 34C08 Connections with real algebraic geometry (fewnomials, desingularization, zeros of Abelian integrals, etc.)
- 34C10 Oscillation theory, zeros, disconjugacy and comparison theory
- 34C11 Growth, boundedness
- 34C12 Monotone systems
- 34C14 Symmetries, invariants

- 34C15 Nonlinear oscillations, coupled oscillators
- 34C20 Transformation and reduction of equations and systems, normal forms
- 34C23 Bifurcation [See also 37Gxx]
- 34C25 Periodic solutions
- 34C26 Relaxation oscillations
- 34C27 Almost and pseudo-almost periodic solutions
- 34C28 Complex behavior, chaotic systems [See also 37Dxx]
- 34C29 Averaging method
- 34C37 Homoclinic and heteroclinic solutions
- 34C40 Equations and systems on manifolds
- 34C41 Equivalence, asymptotic equivalence
- 34C45 Invariant manifolds
- 34C46 Multifrequency systems
- 34C55 Hysteresis
- 34C60 Qualitative investigation and simulation of models
- 34C99 None of the above, but in this section
- 34Dxx Stability theory [See also 37C75, 93Dxx]**
- 34D05 Asymptotic properties
- 34D06 Synchronization
- 34D08 Characteristic and Lyapunov exponents
- 34D09 Dichotomy, trichotomy
- 34D10 Perturbations
- 34D15 Singular perturbations
- 34D20 Stability
- 34D23 Global stability
- 34D30 Structural stability and analogous concepts [See also 37C20]
- 34D35 Stability of manifolds of solutions
- 34D45 Attractors [See also 37C70, 37D45]
- 34D99 None of the above, but in this section
- 34Exx Asymptotic theory**
- 34E05 Asymptotic expansions
- 34E10 Perturbations, asymptotics
- 34E13 Multiple scale methods
- 34E15 Singular perturbations, general theory
- 34E17 Canard solutions
- 34E18 Methods of nonstandard analysis
- 34E20 Singular perturbations, turning point theory, WKB methods
- 34E99 None of the above, but in this section
- 34Fxx Equations and systems with randomness [See also 34K50, 60H10, 93E03]**
- 34F05 Equations and systems with randomness [See also 34K50, 60H10, 93E03]
- 34F10 Bifurcation
- 34F15 Resonance phenomena
- 34F99 None of the above, but in this section
- 34Gxx Differential equations in abstract spaces [See also 34Lxx, 37Kxx, 47Dxx, 47Hxx, 47Jxx, 58D25]**
- 34G10 Linear equations [See also 47D06, 47D09]
- 34G20 Nonlinear equations [See also 47Hxx, 47Jxx]
- 34G25 Evolution inclusions
- 34G99 None of the above, but in this section

- 34Hxx** **Control problems** [See also 49J15, 49K15, 93C15]
- 34H05 Control problems [See also 49J15, 49K15, 93C15]
- 34H10 Chaos control
- 34H15 Stabilization
- 34H20 Bifurcation control
- 34H99 None of the above, but in this section
- 34Kxx** **Functional-differential and differential-difference equations**  
[See also 37–XX]
- 34K05 General theory
- 34K06 Linear functional-differential equations
- 34K07 Theoretical approximation of solutions
- 34K08 Spectral theory of functional-differential operators
- 34K09 Functional-differential inclusions
- 34K10 Boundary value problems
- 34K11 Oscillation theory
- 34K12 Growth, boundedness, comparison of solutions
- 34K13 Periodic solutions
- 34K14 Almost and pseudo-periodic solutions
- 34K17 Transformation and reduction of equations and systems, normal forms
- 34K18 Bifurcation theory
- 34K19 Invariant manifolds
- 34K20 Stability theory
- 34K21 Stationary solutions
- 34K23 Complex (chaotic) behavior of solutions
- 34K25 Asymptotic theory
- 34K26 Singular perturbations
- 34K27 Perturbations
- 34K28 Numerical approximation of solutions
- 34K29 Inverse problems
- 34K30 Equations in abstract spaces [See also 34Gxx, 35R09, 35R10, 47Jxx]
- 34K31 Lattice functional-differential equations
- 34K32 Implicit equations
- 34K33 Averaging
- 34K34 Hybrid systems
- 34K35 Control problems [See also 49J21, 49K21, 93C23]
- 34K36 Fuzzy functional-differential equations
- 34K37 Functional-differential equations with fractional derivatives
- 34K38 Functional-differential inequalities
- 34K40 Neutral equations
- 34K45 Equations with impulses
- 34K50 Stochastic functional-differential equations [See also , 60Hxx]
- 34K60 Qualitative investigation and simulation of models
- 34K99 None of the above, but in this section
- 34Lxx** **Ordinary differential operators** [See also 47E05]
- 34L05 General spectral theory
- 34L10 Eigenfunctions, eigenfunction expansions, completeness of eigenfunctions
- 34L15 Eigenvalues, estimation of eigenvalues, upper and lower bounds
- 34L16 Numerical approximation of eigenvalues and of other parts of the spectrum

- 34L20 Asymptotic distribution of eigenvalues, asymptotic theory of eigenfunctions
- 34L25 Scattering theory, inverse scattering
- 34L30 Nonlinear ordinary differential operators
- 34L40 Particular operators (Dirac, one-dimensional Schrödinger, etc.)
- 34L99 None of the above, but in this section
- 34Mxx Differential equations in the complex domain [See also 30Dxx, 32G34]**
- 34M03 Linear equations and systems
- 34M05 Entire and meromorphic solutions
- 34M10 Oscillation, growth of solutions
- 34M15 Algebraic aspects (differential-algebraic, hypertranscendence, group-theoretical)
- 34M25 Formal solutions, transform techniques
- 34M30 Asymptotics, summation methods
- 34M35 Singularities, monodromy, local behavior of solutions, normal forms
- 34M40 Stokes phenomena and connection problems (linear and nonlinear)
- 34M45 Differential equations on complex manifolds
- 34M50 Inverse problems (Riemann-Hilbert, inverse differential Galois, etc.)
- 34M55 Painlevé and other special equations; classification, hierarchies;
- 34M56 Isomonodromic deformations
- 34M60 Singular perturbation problems in the complex domain (complex WKB, turning points, steepest descent) [See also 34E20]
- 34M99 None of the above, but in this section
- 34Nxx Dynamic equations on time scales or measure chains  $\{\{\}\}$  For real analysis on time scales see 26E60**
- 34N05 Dynamic equations on time scales or measure chains  $\{\{\}\}$  For real analysis on time scales or measure chains, see 26E70
- 34N99 None of the above, but in this section
- 35–XX PARTIAL DIFFERENTIAL EQUATIONS**
- 35–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 35–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 35–02 Research exposition (monographs, survey articles)
- 35–03 Historical (must also be assigned at least one classification number from Section 01)
- 35–04 Explicit machine computation and programs (not the theory of computation or programming)
- 35–06 Proceedings, conferences, collections, etc.
- 35Axx General topics**
- 35A01 Existence problems: global existence, local existence, non-existence
- 35A02 Uniqueness problems: global uniqueness, local uniqueness, non-uniqueness
- 35A08 Fundamental solutions
- 35A09 Classical solutions
- 35A10 Cauchy-Kovalevskaya theorems
- 35A15 Variational methods
- 35A16 Topological and monotonicity methods
- 35A17 Parametrices
- 35A18 Wave front sets
- 35A20 Analytic methods, singularities

- 35A21 Propagation of singularities
- 35A22 Transform methods (e.g. integral transforms)
- 35A23 Inequalities involving derivatives and differential and integral operators, inequalities for integrals
- 35A24 Methods of ordinary differential equations
- 35A25 Other special methods
- 35A27 Microlocal methods; methods of sheaf theory and homological algebra in PDE [See also 32C38, 58J15]
- 35A30 Geometric theory, characteristics, transformations [See also 58J70, 58J72]
- 35A35 Theoretical approximation to solutions  $\{\{\}\}$  For numerical analysis, see 65Mxx, 65Nxx
- 35A99 None of the above, but in this section
- 35Bxx Qualitative properties of solutions**
- 35B05 Oscillation, zeros of solutions, mean value theorems, etc.
- 35B06 Symmetries, invariants, etc.
- 35B07 Axially symmetric solutions
- 35B08 Entire solutions
- 35B09 Positive solutions
- 35B10 Periodic solutions
- 35B15 Almost and pseudo-almost periodic solutions
- 35B20 Perturbations
- 35B25 Singular perturbations
- 35B27 Homogenization; equations in media with periodic structure [See also 74Qxx, 76M50]
- 35B30 Dependence of solutions on initial and boundary data, parameters [See also 37Cxx]
- 35B32 Bifurcation [See also 37Gxx, 37K50]
- 35B33 Critical exponents
- 35B34 Resonances
- 35B35 Stability
- 35B36 Pattern formation
- 35B38 Critical points
- 35B40 Asymptotic behavior of solutions
- 35B41 Attractors
- 35B42 Inertial manifolds
- 35B44 Blow-up
- 35B45 A priori estimates
- 35B50 Maximum principles
- 35B51 Comparison principles
- 35B53 Liouville theorems, Phragmén-Lindelöf theorems
- 35B60 Continuation and prolongation of solutions [See also 58A15, 58A17, 58Hxx]
- 35B65 Smoothness and regularity of solutions
- 35B99 None of the above, but in this section
- 35Cxx Representations of solutions**
- 35C05 Solutions in closed form
- 35C06 Self-similar solutions
- 35C07 Traveling wave solutions
- 35C08 Soliton solutions
- 35C09 Trigonometric solutions

35C10	Series solutions
35C11	Polynomial solutions
35C15	Integral representations of solutions
35C20	Asymptotic expansions
35C99	None of the above, but in this section
<b>35Dxx</b>	<b>Generalized solutions</b>
35D30	Weak solutions
35D35	Strong solutions
35D40	Viscosity solutions
35D99	None of the above, but in this section
<b>35Exx</b>	<b>Equations and systems with constant coefficients [See also 35N05]</b>
35E05	Fundamental solutions
35E10	Convexity properties
35E15	Initial value problems
35E20	General theory
35E99	None of the above, but in this section
<b>35Fxx</b>	<b>General first-order equations and systems</b>
35F05	Linear first-order equations
35F10	Initial value problems for linear first-order equations
35F15	Boundary value problems for linear first-order equations
35F16	Initial-boundary value problems for linear first-order equations
35F20	Nonlinear first-order equations
35F21	Hamilton-Jacobi equations
35F25	Initial value problems for nonlinear first-order equations
35F30	Boundary value problems for nonlinear first-order equations
35F31	Initial-boundary value problems for nonlinear first-order equations
35F35	Linear first-order systems
35F40	Initial value problems for linear first-order systems
35F45	Boundary value problems for linear first-order systems
35F46	Initial-boundary value problems for linear first-order systems
35F50	Nonlinear first-order systems
35F55	Initial value problems for nonlinear first-order systems
35F60	Boundary value problems for nonlinear first-order systems
35F61	Initial-boundary value problems for nonlinear first-order systems
35F99	None of the above, but in this section
<b>35Gxx</b>	<b>General higher-order equations and systems</b>
35G05	Linear higher-order equations
35G10	Initial value problems for linear higher-order equations
35G15	Boundary value problems for linear higher-order equations
35G16	Initial-boundary value problems for linear higher-order equations
35G20	Nonlinear higher-order equations
35G25	Initial value problems for nonlinear higher-order equations
35G30	Boundary value problems for nonlinear higher-order equations
35G31	Initial-boundary value problems for nonlinear higher-order equations
35G35	Linear higher-order systems
35G40	Initial value problems for linear higher-order systems
35G45	Boundary value problems for linear higher-order systems
35G46	Initial-boundary value problems for linear higher-order systems
35G50	Nonlinear higher-order systems
35G55	Initial value problems for nonlinear higher-order systems
35G60	Boundary value problems for nonlinear higher-order systems

- 35G61 Initial-boundary value problems for nonlinear higher-order systems
- 35G99 None of the above, but in this section
- 35Hxx Close-to-elliptic equations and systems**
- 35H10 Hypoelliptic equations
- 35H20 Subelliptic equations
- 35H30 Quasi-elliptic equations
- 35H99 None of the above, but in this section
- 35Jxx Elliptic equations and systems [See also 58J10, 58J20]**
- 35J05 Laplacian operator, reduced wave equation (Helmholtz equation), Poisson equation [See also 31Axx, 31Bxx]
- 35J08 Green's functions
- 35J10 Schrödinger operator [See also 35Pxx]
- 35J15 Second-order elliptic equations
- 35J20 Variational methods for second-order elliptic equations
- 35J25 Boundary value problems for second-order elliptic equations
- 35J30 Higher-order elliptic equations [See also 31A30, 31B30]
- 35J35 Variational methods for higher-order elliptic equations
- 35J40 Boundary value problems for higher-order elliptic equations
- 35J46 First-order elliptic systems
- 35J47 Second-order elliptic systems
- 35J48 Higher-order elliptic systems
- 35J50 Variational methods for elliptic systems
- 35J56 Boundary value problems for first-order elliptic systems
- 35J57 Boundary value problems for second-order elliptic systems
- 35J58 Boundary value problems for higher-order elliptic systems
- 35J60 Nonlinear elliptic equations
- 35J61 Semilinear elliptic equations
- 35J62 Quasilinear elliptic equations
- 35J65 Nonlinear boundary value problems for linear elliptic equations
- 35J66 Nonlinear boundary value problems for nonlinear elliptic equations
- 35J67 Boundary values of solutions to elliptic equations
- 35J70 Degenerate elliptic equations
- 35J75 Singular elliptic equations
- 35J86 Linear elliptic unilateral problems and linear elliptic variational inequalities [See also 35R35, 49J40]
- 35J87 Nonlinear elliptic unilateral problems and nonlinear elliptic variational inequalities [See also 35R35, 49J40]
- 35J88 Systems of elliptic variational inequalities [See also 35R35, 49J40]
- 35J91 Semilinear elliptic equations with Laplacian, bi-Laplacian or poly-Laplacian
- 35J92 Quasilinear elliptic equations with  $p$ -Laplacian
- 35J93 Quasilinear elliptic equations with mean curvature operator
- 35J96 Elliptic Monge-Ampère equations
- 35J99 None of the above, but in this section
- 35Kxx Parabolic equations and systems [See also 35Bxx, 35Dxx, 35R30, 35R35, 58J35]**
- 35K05 Heat equation
- 35K08 Heat kernel
- 35K10 Second-order parabolic equations
- 35K15 Initial value problems for second-order parabolic equations
- 35K20 Initial-boundary value problems for second-order parabolic equations

- 35K25 Higher-order parabolic equations
- 35K30 Initial value problems for higher-order parabolic equations
- 35K35 Initial-boundary value problems for higher-order parabolic equations
- 35K40 Second-order parabolic systems
- 35K41 Higher-order parabolic systems
- 35K45 Initial value problems for second-order parabolic systems
- 35K46 Initial value problems for higher-order parabolic systems
- 35K51 Initial-boundary value problems for second-order parabolic systems
- 35K52 Initial-boundary value problems for higher-order parabolic systems
- 35K55 Nonlinear parabolic equations
- 35K57 Reaction-diffusion equations
- 35K58 Semilinear parabolic equations
- 35K59 Quasilinear parabolic equations
- 35K60 Nonlinear initial value problems for linear parabolic equations
- 35K61 Nonlinear initial-boundary value problems for nonlinear parabolic equations
- 35K65 Degenerate parabolic equations
- 35K67 Singular parabolic equations
- 35K70 Ultraparabolic equations, pseudoparabolic equations, etc.
- 35K85 Linear parabolic unilateral problems and linear parabolic variational inequalities [See also 35R35, 49J40]
- 35K86 Nonlinear parabolic unilateral problems and nonlinear parabolic variational inequalities [See also 35R35, 49J40]
- 35K87 Systems of parabolic variational inequalities [See also 35R35, 49J40]
- 35K90 Abstract parabolic equations
- 35K91 Semilinear parabolic equations with Laplacian, bi-Laplacian or poly-Laplacian
- 35K92 Quasilinear parabolic equations with  $p$ -Laplacian
- 35K93 Quasilinear parabolic equations with mean curvature operator
- 35K96 Parabolic Monge-Ampère equations
- 35K99 None of the above, but in this section
- 35Lxx Hyperbolic equations and systems [See also 58J45]**
- 35L02 First-order hyperbolic equations
- 35L03 Initial value problems for first-order hyperbolic equations
- 35L04 Initial-boundary value problems for first-order hyperbolic equations
- 35L05 Wave equation
- 35L10 Second-order hyperbolic equations
- 35L15 Initial value problems for second-order hyperbolic equations
- 35L20 Initial-boundary value problems for second-order hyperbolic equations
- 35L25 Higher-order hyperbolic equations
- 35L30 Initial value problems for higher-order hyperbolic equations
- 35L35 Initial-boundary value problems for higher-order hyperbolic equations
- 35L40 First-order hyperbolic systems
- 35L45 Initial value problems for first-order hyperbolic systems
- 35L50 Initial-boundary value problems for first-order hyperbolic systems
- 35L51 Second-order hyperbolic systems
- 35L52 Initial value problems for second-order hyperbolic systems
- 35L53 Initial-boundary value problems for second-order hyperbolic systems
- 35L55 Higher-order hyperbolic systems
- 35L56 Initial value problems for higher-order hyperbolic systems

- 35L57 Initial-boundary value problems for higher-order hyperbolic systems
- 35L60 Nonlinear first-order hyperbolic equations
- 35L65 Conservation laws
- 35L67 Shocks and singularities [See also 58Kxx, 76L05]
- 35L70 Nonlinear second-order hyperbolic equations
- 35L71 Semilinear second-order hyperbolic equations
- 35L72 Quasilinear second-order hyperbolic equations
- 35L75 Nonlinear higher-order hyperbolic equations
- 35L76 Semilinear higher-order hyperbolic equations
- 35L77 Quasilinear higher-order hyperbolic equations
- 35L80 Degenerate hyperbolic equations
- 35L81 Singular hyperbolic equations
- 35L82 Pseudohyperbolic equations
- 35L85 Linear hyperbolic unilateral problems and linear hyperbolic variational inequalities [See also 35R35, 49J40]
- 35L86 Nonlinear hyperbolic unilateral problems and nonlinear hyperbolic variational inequalities [See also 35R35, 49J40]
- 35L87 Unilateral problems and variational inequalities for hyperbolic systems [See also 35R35, 49J40]
- 35L90 Abstract hyperbolic equations
- 35L99 None of the above, but in this section
- 35Mxx Equations and systems of special type (mixed, composite, etc.)**
- 35M10 Equations of mixed type
- 35M11 Initial value problems for equations of mixed type
- 35M12 Boundary value problems for equations of mixed type
- 35M13 Initial-boundary value problems for equations of mixed type
- 35M30 Systems of mixed type
- 35M31 Initial value problems for systems of mixed type
- 35M32 Boundary value problems for systems of mixed type
- 35M33 Initial-boundary value problems for systems of mixed type
- 35M85 Linear unilateral problems and variational inequalities of mixed type [See also 35R35, 49J40]
- 35M86 Nonlinear unilateral problems and nonlinear variational inequalities of mixed type [See also 35R35, 49J40]
- 35M87 Systems of variational inequalities of mixed type [See also 35R35, 49J40]
- 35M99 None of the above, but in this section
- 35Nxx Overdetermined systems [See also 58Hxx, 58J10, 58J15]**
- 35N05 Overdetermined systems with constant coefficients
- 35N10 Overdetermined systems with variable coefficients
- 35N15  $\bar{\partial}$ -Neumann problem and generalizations; formal complexes [See also 32W05, 32W10, 58J10]
- 35N20 Overdetermined initial value problems
- 35N25 Overdetermined boundary value problems
- 35N30 Overdetermined initial-boundary value problems
- 35N99 None of the above, but in this section
- 35Pxx Spectral theory and eigenvalue problems [See also 47Axx, 47Bxx, 47F05]**
- 35P05 General topics in linear spectral theory
- 35P10 Completeness of eigenfunctions, eigenfunction expansions
- 35P15 Estimation of eigenvalues, upper and lower bounds

- 35P20 Asymptotic distribution of eigenvalues and eigenfunctions
- 35P25 Scattering theory [See also 47A40]
- 35P30 Nonlinear eigenvalue problems, nonlinear spectral theory
- 35P99 None of the above, but in this section
- 35Qxx Some special equations of mathematical physics [See also 35J05, 35J10, 35K05, 35L05]**
- 35Q05 Euler-Poisson-Darboux equations
- 35Q15 Riemann-Hilbert problems [See also 30E25, 31A25, 31B20]
- 35Q30 Navier-Stokes equations [See also 76D05, 76D07, 76N10]
- 35Q31 Euler equations [See also 76D05, 76D07, 76N10]
- 35Q41 Boltzmann equations
- 35Q45 Vlasov-like equations
- 35Q47 Fokker-Planck equations
- 35Q53 KdV-like equations (Korteweg-de Vries, Burgers, sine-Gordon, sinh-Gordon, etc.) [See also 37K10]
- 35Q55 NLS-like (nonlinear Schrödinger) equations [See also 37K10]
- 35Q56 Ginzburg-Landau equations
- 35Q60 Maxwell equations
- 35Q75 Einstein equations
- 35Q81 Time-dependent Schrödinger equations, Dirac equations
- 35Q99 None of the above, but in this section
- 35Rxx Miscellaneous topics {{{}}}For equations on manifolds, see 58Jxx; for manifolds of solutions, see 58Bxx; for stochastic PDE, see also 60H15**
- 35R01 Partial differential equations on manifolds [See also 32Wxx, 53Cxx, 58Jxx]
- 35R02 Partial differential equations on graphs and networks (ramified or polygonal spaces)
- 35R03 Partial differential equations on Heisenberg groups, Lie groups, Carnot groups, etc.
- 35R05 Partial differential equations with discontinuous coefficients or data
- 35R06 Partial differential equations with measure
- 35R09 Integro-partial differential equations [See also 45Kxx]
- 35R10 Partial functional-differential equations
- 35R11 Fractional partial differential equations
- 35R12 Impulsive partial differential equations
- 35R13 Fuzzy partial differential equations
- 35R15 Partial differential equations on infinite-dimensional (e.g. function) spaces (= PDE in infinitely many variables) [See also 46Gxx, 58D25]
- 35R20 Partial operator-differential equations (i.e., PDE on finite-dimensional spaces for abstract space valued functions) [See also 34Gxx, 47A50, 47D03, 47D06, 47D09, 47H20, 47Jxx]
- 35R25 Improperly posed problems
- 35R30 Inverse problems
- 35R35 Free boundary problems
- 35R37 Moving boundary problems
- 35R45 Partial differential inequalities
- 35R50 Partial differential equations of infinite order
- 35R60 Partial differential equations with randomness, stochastic partial differential equations [See also 60H15]
- 35R70 Partial differential equations with multivalued right-hand sides
- 35R99 None of the above, but in this section

- 35Sxx Pseudodifferential operators and other generalizations of partial differential operators [See also 47G30, 58J40]**
- 35S05 Pseudodifferential operators
- 35S10 Initial value problems for pseudodifferential operators
- 35S11 Initial-boundary value problems for pseudodifferential operators
- 35S15 Boundary value problems for pseudodifferential operators
- 35S30 Fourier integral operators
- 35S35 Topological aspects: intersection cohomology, stratified sets, etc. [See also 32C38, 32S40, 32S60, 58J15]
- 35S50 Paradifferential operators
- 35S99 None of the above, but in this section
- 37–XX DYNAMICAL SYSTEMS AND ERGODIC THEORY [See also 26A18, 28Dxx, 34Cxx, 34Dxx, 35Bxx, 46Lxx, 58Jxx, 70–XX]**
- 37–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 37–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 37–02 Research exposition (monographs, survey articles)
- 37–03 Historical (must also be assigned at least one classification number from Section 01)
- 37–04 Explicit machine computation and programs (not the theory of computation or programming)
- 37–06 Proceedings, conferences, collections, etc.
- 37Axx Ergodic theory [See also 28Dxx]**
- 37A05 Measure-preserving transformations
- 37A10 One-parameter continuous families of measure-preserving transformations
- 37A15 General groups of measure-preserving transformations [See mainly 22Fxx]
- 37A17 Homogeneous flows [See also 22Fxx]
- 37A20 Orbit equivalence, cocycles, ergodic equivalence relations
- 37A25 Ergodicity, mixing, rates of mixing
- 37A30 Ergodic theorems, spectral theory, Markov operators  $\{\}$ For operator ergodic theory, see mainly 47A35
- 37A35 Entropy and other invariants, isomorphism, classification
- 37A40 Nonsingular (and infinite-measure preserving) transformations
- 37A45 Relations with number theory and harmonic analysis [See also 11Kxx]
- 37A50 Relations with probability theory and stochastic processes [See also 60Fxx and 60G10]
- 37A55 Relations with the theory of  $C^*$ -algebras [See mainly 46L55]
- 37A60 Dynamical systems in statistical mechanics [See also 82Cxx]
- 37A99 None of the above, but in this section
- 37Bxx Topological dynamics [See also 54H20]**
- 37B05 Transformations and group actions with special properties (minimality, distality, proximality, etc.)
- 37B10 Symbolic dynamics [See also 37Cxx, 37Dxx]
- 37B15 Cellular automata [See also 68Q80]
- 37B20 Notions of recurrence
- 37B25 Lyapunov functions and stability; attractors, repellers
- 37B30 Index theory, Morse-Conley indices

- 37B35 Gradient-like and recurrent behavior; isolated (locally maximal) invariant sets
- 37B40 Topological entropy
- 37B45 Continua theory in dynamics
- 37B50 Multi-dimensional shifts of finite type, tiling dynamics
- 37B55 Nonautonomous dynamical systems
- 37B99 None of the above, but in this section
- 37Cxx Smooth dynamical systems: general theory [See also 34Cxx, 34Dxx]**
- 37C05 Smooth mappings and diffeomorphisms
- 37C10 Vector fields, flows, ordinary differential equations
- 37C15 Topological and differentiable equivalence, conjugacy, invariants, moduli, classification
- 37C20 Generic properties, structural stability
- 37C25 Fixed points, periodic points, fixed-point index theory
- 37C27 Periodic orbits of vector fields and flows
- 37C29 Homoclinic and heteroclinic orbits
- 37C30 Zeta functions, (Ruelle-Frobenius) transfer operators, and other functional analytic techniques in dynamical systems
- 37C35 Orbit growth
- 37C40 Smooth ergodic theory, invariant measures [See also 37Dxx]
- 37C45 Dimension theory of dynamical systems
- 37C50 Approximate trajectories (pseudotrajectories, shadowing, etc.)
- 37C55 Periodic and quasiperiodic flows and diffeomorphisms
- 37C60 Nonautonomous smooth dynamical systems [See also 37B55]
- 37C65 Monotone flows
- 37C70 Attractors and repellers, topological structure
- 37C75 Stability theory
- 37C80 Symmetries, equivariant dynamical systems
- 37C85 Dynamics of group actions other than  $\mathbf{Z}$  and  $\mathbf{R}$ , and foliations [See mainly 22Fxx, and also 57R30, 57Sxx]
- 37C99 None of the above, but in this section
- 37Dxx Dynamical systems with hyperbolic behavior**
- 37D05 Hyperbolic orbits and sets
- 37D10 Invariant manifold theory
- 37D15 Morse-Smale systems
- 37D20 Uniformly hyperbolic systems (expanding, Anosov, Axiom A, etc.)
- 37D25 Nonuniformly hyperbolic systems (Lyapunov exponents, Pesin theory, etc.)
- 37D30 Partially hyperbolic systems and dominated splittings
- 37D35 Thermodynamic formalism, variational principles, equilibrium states
- 37D40 Dynamical systems of geometric origin and hyperbolicity (geodesic and horocycle flows, etc.)
- 37D45 Strange attractors, chaotic dynamics
- 37D50 Hyperbolic systems with singularities (billiards, etc.)
- 37D99 None of the above, but in this section
- 37Exx Low-dimensional dynamical systems**
- 37E05 Maps of the interval (piecewise continuous, continuous, smooth)
- 37E10 Maps of the circle
- 37E15 Combinatorial dynamics (types of periodic orbits)
- 37E20 Universality, renormalization [See also 37F25]
- 37E25 Maps of trees and graphs

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- 37E30 Homeomorphisms and diffeomorphisms of planes and surfaces
- 37E35 Flows on surfaces
- 37E40 Twist maps
- 37E45 Rotation numbers and vectors
- 37E99 None of the above, but in this section
- 37Fxx Complex dynamical systems [See also 30D05, 32H50]**
- 37F05 Relations and correspondences
- 37F10 Polynomials; rational maps; entire and meromorphic functions  
[See also 32A10, 32A20, 32H02, 32H04]
- 37F15 Expanding maps; hyperbolicity; structural stability
- 37F20 Combinatorics and topology
- 37F25 Renormalization
- 37F30 Quasiconformal methods and Teichmüller theory; Fuchsian and  
Kleinian groups as dynamical systems
- 37F35 Conformal densities and Hausdorff dimension
- 37F40 Geometric limits
- 37F45 Holomorphic families of dynamical systems; the Mandelbrot set;  
bifurcations
- 37F50 Small divisors, rotation domains and linearization; Fatou and Julia  
sets
- 37F75 Holomorphic foliations and vector fields [See also 32M25, 32S65,  
34Mxx]
- 37F99 None of the above, but in this section
- 37Gxx Local and nonlocal bifurcation theory [See also 34C23, 34K18]**
- 37G05 Normal forms
- 37G10 Bifurcations of singular points
- 37G15 Bifurcations of limit cycles and periodic orbits
- 37G20 Hyperbolic singular points with homoclinic trajectories
- 37G25 Bifurcations connected with nontransversal intersection
- 37G30 Infinite nonwandering sets arising in bifurcations
- 37G35 Attractors and their bifurcations
- 37G40 Symmetries, equivariant bifurcation theory
- 37G99 None of the above, but in this section
- 37Hxx Random dynamical systems [See also 15B52, 34D08, 34F05, 47B80,  
70L05, 82C05, 93Exx]**
- 37H05 Foundations, general theory of cocycles, algebraic ergodic theory  
[See also 37Axx]
- 37H10 Generation, random and stochastic difference and differential  
equations [See also 34F05, 34K50, 60H10, 60H15]
- 37H15 Multiplicative ergodic theory, Lyapunov exponents [See also 34D08,  
37Axx, 37Cxx, 37Dxx]
- 37H20 Bifurcation theory [See also 37Gxx]
- 37H99 None of the above, but in this section
- 37Jxx Finite-dimensional Hamiltonian, Lagrangian, contact, and  
nonholonomic systems [See also 53Dxx, 70Fxx, 70Hxx]**
- 37J05 General theory, relations with symplectic geometry and topology
- 37J10 Symplectic mappings, fixed points
- 37J15 Symmetries, invariants, invariant manifolds, momentum maps,  
reduction [See also 53D20]
- 37J20 Bifurcation problems
- 37J25 Stability problems

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- 37J30 Obstructions to integrability (nonintegrability criteria)
- 37J35 Completely integrable systems, topological structure of phase space, integration methods
- 37J40 Perturbations, normal forms, small divisors, KAM theory, Arnol'd diffusion
- 37J45 Periodic, homoclinic and heteroclinic orbits; variational methods, degree-theoretic methods
- 37J50 Action-minimizing orbits and measures
- 37J55 Contact systems [See also 53D10]
- 37J60 Nonholonomic dynamical systems [See also 70F25]
- 37J99 None of the above, but in this section
- 37Kxx Infinite-dimensional Hamiltonian systems [See also 35Axx, 35Qxx]**
- 37K05 Hamiltonian structures, symmetries, variational principles, conservation laws
- 37K10 Completely integrable systems, integrability tests, bi-Hamiltonian structures, hierarchies (KdV, KP, Toda, etc.)
- 37K15 Integration of completely integrable systems by inverse spectral and scattering methods
- 37K20 Relations with algebraic geometry, complex analysis, special functions [See also 14H70]
- 37K25 Relations with differential geometry
- 37K30 Relations with infinite-dimensional Lie algebras and other algebraic structures
- 37K35 Lie-Bäcklund and other transformations
- 37K40 Soliton theory, asymptotic behavior of solutions
- 37K45 Stability problems
- 37K50 Bifurcation problems
- 37K55 Perturbations, KAM for infinite-dimensional systems
- 37K60 Lattice dynamics [See also 37L60]
- 37K65 Hamiltonian systems on groups of diffeomorphisms and on manifolds of mappings and metrics
- 37K99 None of the above, but in this section
- 37Lxx Infinite-dimensional dissipative dynamical systems [See also 35Bxx, 35Qxx]**
- 37L05 General theory, nonlinear semigroups, evolution equations
- 37L10 Normal forms, center manifold theory, bifurcation theory
- 37L15 Stability problems
- 37L20 Symmetries
- 37L25 Inertial manifolds and other invariant attracting sets
- 37L30 Attractors and their dimensions, Lyapunov exponents
- 37L40 Invariant measures
- 37L45 Hyperbolicity; Lyapunov functions
- 37L50 Noncompact semigroups; dispersive equations; perturbations of Hamiltonian systems
- 37L55 Infinite-dimensional random dynamical systems; stochastic equations [See also 35R60, 60H10, 60H15]
- 37L60 Lattice dynamics [See also 37K60]
- 37L65 Special approximation methods (nonlinear Galerkin, etc.)
- 37L99 None of the above, but in this section
- 37Mxx Approximation methods and numerical treatment of dynamical systems [See also 65Pxx]**
- 37M05 Simulation

- 37M10 Time series analysis
- 37M15 Symplectic integrators
- 37M20 Computational methods for bifurcation problems
- 37M25 Computational methods for ergodic theory (approximation of invariant measures, computation of Lyapunov exponents, entropy)
- 37M99 None of the above, but in this section
- 37Nxx Applications**
- 37N05 Dynamical systems in classical and celestial mechanics [See mainly 70Fxx, 70Hxx, 70Kxx]
- 37N10 Dynamical systems in fluid mechanics, oceanography and meteorology [See mainly 76–XX, especially 76D05, 76F20, 86A05, 86A10]
- 37N15 Dynamical systems in solid mechanics [See mainly 74Hxx]
- 37N20 Dynamical systems in other branches of physics (quantum mechanics, general relativity, laser physics)
- 37N25 Dynamical systems in biology [See mainly 92–XX, but also 91–XX]
- 37N30 Dynamical systems in numerical analysis
- 37N35 Dynamical systems in control
- 37N40 Dynamical systems in optimization and economics
- 37N99 None of the above, but in this section
- 37Pxx Arithmetic and non-Archimedean dynamical systems**
- 37P05 Polynomial and rational maps
- 37P10 Analytic and meromorphic maps
- 37P15 Global ground fields
- 37P20 Non-Archimedean local ground fields
- 37P25 Finite ground fields
- 37P30 Height functions; Green functions; invariant measures [See also 11G50, 14G40]
- 37P35 Arithmetic properties of periodic points
- 37P40 Non-Archimedean Fatou and Julia sets
- 37P45 Families and moduli spaces
- 37P50 Dynamical systems on Berkovich spaces
- 37P55 Arithmetic dynamics on general algebraic varieties
- 37P99 None of the above, but in this section
- 39–XX DIFFERENCE AND FUNCTIONAL EQUATIONS**
- 39–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 39–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 39–02 Research exposition (monographs, survey articles)
- 39–03 Historical (must also be assigned at least one classification number from Section 01)
- 39–04 Explicit machine computation and programs (not the theory of computation or programming)
- 39–06 Proceedings, conferences, collections, etc.
- 39Axx Difference equations  $\{\{\}\}$  For dynamical systems, see 37–XX, for dynamic equations on time scales, see 34N05**
- 39A05 General theory
- 39A06 Linear equations
- 39A10 Difference equations, additive
- 39A12 Discrete version of topics in analysis
- 39A13 Difference equations, scaling ( $q$ -differences) [See also 33Dxx]

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- 39A14 Partial difference equations
- 39A20 Multiplicative and other generalized difference equations, e.g. of Lyness type
- 39A21 Oscillation theory
- 39A22 Growth, boundedness, comparison of solutions
- 39A23 Periodic solutions
- 39A24 Almost periodic solutions
- 39A28 Bifurcation theory
- 39A30 Stability theory
- 39A33 Complex (chaotic) behavior of solutions
- 39A45 Equations in the complex domain
- 39A50 Stochastic difference equations
- 39A60 Applications
- 39A70 Difference operators [See also 47B39]
- 39A99 None of the above, but in this section
- 39Bxx Functional equations and inequalities [See also 30D05]**
- 39B05 General
- 39B12 Iteration theory, iterative and composite equations [See also 26A18, 30D05, 37-XX]
- 39B22 Equations for real functions [See also 26A51, 26B25]
- 39B32 Equations for complex functions [See also 30D05]
- 39B42 Matrix and operator equations [See also 47Jxx]
- 39B52 Equations for functions with more general domains and/or ranges
- 39B55 Orthogonal additivity and other conditional equations
- 39B62 Functional inequalities, including subadditivity, convexity, etc. [See also 26A51, 26B25, 26Dxx]
- 39B72 Systems of functional equations and inequalities
- 39B82 Stability, separation, extension, and related topics [See also 46A22]
- 39B99 None of the above, but in this section
- 40-XX SEQUENCES, SERIES, SUMMABILITY**
- 40-00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 40-01 Instructional exposition (textbooks, tutorial papers, etc.)
- 40-02 Research exposition (monographs, survey articles)
- 40-03 Historical (must also be assigned at least one classification number from Section 01)
- 40-04 Explicit machine computation and programs (not the theory of computation or programming)
- 40-06 Proceedings, conferences, collections, etc.
- 40Axx Convergence and divergence of infinite limiting processes**
- 40A05 Convergence and divergence of series and sequences
- 40A10 Convergence and divergence of integrals
- 40A15 Convergence and divergence of continued fractions [See also 30B70]
- 40A20 Convergence and divergence of infinite products
- 40A25 Approximation to limiting values (summation of series, etc.) {{{}}For the Euler-Maclaurin summation formula, see 65B15
- 40A30 Convergence and divergence of series and sequences of functions
- 40A35 Ideal and statistical convergence [See also 40G15]
- 40A99 None of the above, but in this section

- 40Bxx Multiple sequences and series**
- 40B05 Multiple sequences and series (should also be assigned at least one other classification number in this section)
- 40B99 None of the above, but in this section
- 40Cxx General summability methods**
- 40C05 Matrix methods
- 40C10 Integral methods
- 40C15 Function-theoretic methods (including power series methods and semicontinuous methods)
- 40C99 None of the above, but in this section
- 40Dxx Direct theorems on summability**
- 40D05 General theorems
- 40D09 Structure of summability fields
- 40D10 Tauberian constants and oscillation limits
- 40D15 Convergence factors and summability factors
- 40D20 Summability and bounded fields of methods
- 40D25 Inclusion and equivalence theorems
- 40D99 None of the above, but in this section
- 40Exx Inversion theorems**
- 40E05 Tauberian theorems, general
- 40E10 Growth estimates
- 40E15 Lacunary inversion theorems
- 40E20 Tauberian constants
- 40E99 None of the above, but in this section
- 40Fxx Absolute and strong summability**
- 40F05 Absolute and strong summability (should also be assigned at least one other classification number in this section)
- 40F99 None of the above, but in this section
- 40Gxx Special methods of summability**
- 40G05 Cesàro, Euler, Nörlund and Hausdorff methods
- 40G10 Abel, Borel and power series methods
- 40G15 Summability methods using statistical convergence [See also 40A35]
- 40G99 None of the above, but in this section
- 40Hxx Functional analytic methods in summability**
- 40H05 Functional analytic methods in summability (should also be assigned at least one other classification number in this section)
- 40H99 None of the above, but in this section
- 40Jxx Summability in abstract structures [See also 43A55, 46A35, 46B15]**
- 40J05 Summability in abstract structures [See also 43A55, 46A35, 46B15] (should also be assigned at least one other classification number in this section)
- 40J99 None of the above, but in this section
- 41–XX APPROXIMATIONS AND EXPANSIONS FOR ALL APPROXIMATION THEORY IN THE COMPLEX DOMAIN, SEE 30E05 AND 30E10; FOR ALL TRIGONOMETRIC APPROXIMATION AND INTERPOLATION, SEE 42A10 AND 42A15; FOR NUMERICAL APPROXIMATION, SEE 65DXX{}**
- 41–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 41–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 41–02 Research exposition (monographs, survey articles)

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- 41–03 Historical (must also be assigned at least one classification number from Section 01)
- 41–04 Explicit machine computation and programs (not the theory of computation or programming)
- 41–06 Proceedings, conferences, collections, etc.
- 41Axx Approximations and expansions**
- 41A05 Interpolation [See also 42A15 and 65D05]
- 41A10 Approximation by polynomials  $\{\{\}\}$ For approximation by trigonometric polynomials, see 42A10
- 41A15 Spline approximation
- 41A17 Inequalities in approximation (Bernstein, Jackson, Nikol'skiĭ-type inequalities)
- 41A20 Approximation by rational functions
- 41A21 Padé approximation
- 41A25 Rate of convergence, degree of approximation
- 41A27 Inverse theorems
- 41A28 Simultaneous approximation
- 41A29 Approximation with constraints
- 41A30 Approximation by other special function classes
- 41A35 Approximation by operators (in particular, by integral operators)
- 41A36 Approximation by positive operators
- 41A40 Saturation
- 41A44 Best constants
- 41A45 Approximation by arbitrary linear expressions
- 41A46 Approximation by arbitrary nonlinear expressions; widths and entropy
- 41A50 Best approximation, Chebyshev systems
- 41A52 Uniqueness of best approximation
- 41A55 Approximate quadratures
- 41A58 Series expansions (e.g. Taylor, Lidstone series, but not Fourier series)
- 41A60 Asymptotic approximations, asymptotic expansions (steepest descent, etc.) [See also 30E15]
- 41A63 Multidimensional problems (should also be assigned at least one other classification number in this section)
- 41A65 Abstract approximation theory (approximation in normed linear spaces and other abstract spaces)
- 41A80 Remainders in approximation formulas
- 41A99 None of the above, but in this section
- 42–XX FOURIER ANALYSIS**
- 42–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 42–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 42–02 Research exposition (monographs, survey articles)
- 42–03 Historical (must also be assigned at least one classification number from Section 01)
- 42–04 Explicit machine computation and programs (not the theory of computation or programming)
- 42–06 Proceedings, conferences, collections, etc.
- 42Axx Harmonic analysis in one variable**
- 42A05 Trigonometric polynomials, inequalities, extremal problems
- 42A10 Trigonometric approximation

- 42A15 Trigonometric interpolation
- 42A16 Fourier coefficients, Fourier series of functions with special properties, special Fourier series  $\{\{\}\}$  For automorphic theory, see mainly 11F30
- 42A20 Convergence and absolute convergence of Fourier and trigonometric series
- 42A24 Summability and absolute summability of Fourier and trigonometric series
- 42A32 Trigonometric series of special types (positive coefficients, monotonic coefficients, etc.)
- 42A38 Fourier and Fourier-Stieltjes transforms and other transforms of Fourier type
- 42A45 Multipliers
- 42A50 Conjugate functions, conjugate series, singular integrals
- 42A55 Lacunary series of trigonometric and other functions; Riesz products
- 42A61 Probabilistic methods
- 42A63 Uniqueness of trigonometric expansions, uniqueness of Fourier expansions, Riemann theory, localization
- 42A65 Completeness of sets of functions
- 42A70 Trigonometric moment problems
- 42A75 Classical almost periodic functions, mean periodic functions  
[See also 43A60]
- 42A82 Positive definite functions
- 42A85 Convolution, factorization
- 42A99 None of the above, but in this section
- 42Bxx Harmonic analysis in several variables  $\{\{\}\}$  For automorphic theory, see mainly 11F30**
- 42B05 Fourier series and coefficients
- 42B08 Summability
- 42B10 Fourier and Fourier-Stieltjes transforms and other transforms of Fourier type
- 42B15 Multipliers
- 42B20 Singular and oscillatory integrals (Calderón-Zygmund, etc.)
- 42B25 Maximal functions, Littlewood-Paley theory
- 42B30  $H^p$ -spaces
- 42B35 Function spaces arising in harmonic analysis
- 42B37 Harmonic analysis and PDE [See also 35–XX]
- 42B99 None of the above, but in this section
- 42Cxx Nontrigonometric harmonic analysis**
- 42C05 Orthogonal functions and polynomials, general theory  
[See also 33C45, 33C50, 33D45]
- 42C10 Fourier series in special orthogonal functions (Legendre polynomials, Walsh functions, etc.)
- 42C15 General harmonic expansions, frames
- 42C20 Other transformations of harmonic type
- 42C25 Uniqueness and localization for orthogonal series
- 42C30 Completeness of sets of functions
- 42C40 Wavelets and other special systems
- 42C99 None of the above, but in this section

- 43-XX ABSTRACT HARMONIC ANALYSIS FOR OTHER ANALYSIS ON TOPOLOGICAL AND LIE GROUPS, SEE 22EXX{}**
- 43-00 General reference works (handbooks, dictionaries, bibliographies, etc.)
  - 43-01 Instructional exposition (textbooks, tutorial papers, etc.)
  - 43-02 Research exposition (monographs, survey articles)
  - 43-03 Historical (must also be assigned at least one classification number from Section 01)
  - 43-04 Explicit machine computation and programs (not the theory of computation or programming)
  - 43-06 Proceedings, conferences, collections, etc.
  - 43Axx Abstract harmonic analysis**
  - 43A05 Measures on groups and semigroups, etc.
  - 43A07 Means on groups, semigroups, etc.; amenable groups
  - 43A10 Measure algebras on groups, semigroups, etc.
  - 43A15  $L^p$ -spaces and other function spaces on groups, semigroups, etc.
  - 43A17 Analysis on ordered groups,  $H^p$ -theory
  - 43A20  $L^1$ -algebras on groups, semigroups, etc.
  - 43A22 Homomorphisms and multipliers of function spaces on groups, semigroups, etc.
  - 43A25 Fourier and Fourier-Stieltjes transforms on locally compact and other abelian groups
  - 43A30 Fourier and Fourier-Stieltjes transforms on nonabelian groups and on semigroups, etc.
  - 43A32 Other transforms and operators of Fourier type
  - 43A35 Positive definite functions on groups, semigroups, etc.
  - 43A40 Character groups and dual objects
  - 43A45 Spectral synthesis on groups, semigroups, etc.
  - 43A46 Special sets (thin sets, Kronecker sets, Helson sets, Ditkin sets, Sidon sets, etc.)
  - 43A50 Convergence of Fourier series and of inverse transforms
  - 43A55 Summability methods on groups, semigroups, etc. [See also 40J05]
  - 43A60 Almost periodic functions on groups and semigroups and their generalizations (recurrent functions, distal functions, etc.); almost automorphic functions
  - 43A62 Hypergroups
  - 43A65 Representations of groups, semigroups, etc. [See also 22A10, 22A20, 22Dxx, 22E45]
  - 43A70 Analysis on specific locally compact and other abelian groups [See also 11R56, 22B05]
  - 43A75 Analysis on specific compact groups
  - 43A77 Analysis on general compact groups
  - 43A80 Analysis on other specific Lie groups [See also 22Exx]
  - 43A85 Analysis on homogeneous spaces
  - 43A90 Spherical functions [See also 22E45, 22E46, 33C55]
  - 43A95 Categorical methods [See also 46Mxx]
  - 43A99 None of the above, but in this section

- 44–XX INTEGRAL TRANSFORMS, OPERATIONAL CALCULUS FOR FRACTIONAL DERIVATIVES AND INTEGRALS, SEE 26A33. FOR FOURIER TRANSFORMS, SEE 42A38, 42B10. FOR INTEGRAL TRANSFORMS IN DISTRIBUTION SPACES, SEE 46F12. FOR NUMERICAL METHODS, SEE 65R10{}**
- 44–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 44–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 44–02 Research exposition (monographs, survey articles)
- 44–03 Historical (must also be assigned at least one classification number from Section 01)
- 44–04 Explicit machine computation and programs (not the theory of computation or programming)
- 44–06 Proceedings, conferences, collections, etc.
- 44Axx Integral transforms, operational calculus**
- 44A05 General transforms [See also 42A38]
- 44A10 Laplace transform
- 44A12 Radon transform [See also 92C55]
- 44A15 Special transforms (Legendre, Hilbert, etc.)
- 44A20 Transforms of special functions
- 44A30 Multiple transforms
- 44A35 Convolution
- 44A40 Calculus of Mikusiński and other operational calculi
- 44A45 Classical operational calculus
- 44A55 Discrete operational calculus
- 44A60 Moment problems
- 44A99 None of the above, but in this section
- 45–XX INTEGRAL EQUATIONS**
- 45–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 45–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 45–02 Research exposition (monographs, survey articles)
- 45–03 Historical (must also be assigned at least one classification number from Section 01)
- 45–04 Explicit machine computation and programs (not the theory of computation or programming)
- 45–06 Proceedings, conferences, collections, etc.
- 45Axx Linear integral equations**
- 45A05 Linear integral equations
- 45A99 None of the above, but in this section
- 45Bxx Fredholm integral equations**
- 45B05 Fredholm integral equations
- 45B99 None of the above, but in this section
- 45Cxx Eigenvalue problems [See also 34Lxx, 35Pxx, 45P05, 47A75]**
- 45C05 Eigenvalue problems [See also 34Lxx, 35Pxx, 45P05, 47A75]
- 45C99 None of the above, but in this section
- 45Dxx Volterra integral equations [See also 34A12]**
- 45D05 Volterra integral equations [See also 34A12]
- 45D99 None of the above, but in this section
- 45Exx Singular integral equations [See also 30E20, 30E25, 44A15, 44A35]**
- 45E05 Integral equations with kernels of Cauchy type [See also 35J15]

- 45E10 Integral equations of the convolution type (Abel, Picard, Toeplitz and Wiener-Hopf type) [See also 47B35]
- 45E99 None of the above, but in this section
- 45Fxx Systems of linear integral equations**
- 45F05 Systems of nonsingular linear integral equations
- 45F10 Dual, triple, etc., integral and series equations
- 45F15 Systems of singular linear integral equations
- 45F99 None of the above, but in this section
- 45Gxx Nonlinear integral equations [See also 47H30, 47Jxx]**
- 45G05 Singular nonlinear integral equations
- 45G10 Other nonlinear integral equations
- 45G15 Systems of nonlinear integral equations
- 45G99 None of the above, but in this section
- 45Hxx Miscellaneous special kernels [See also 44A15]**
- 45H05 Miscellaneous special kernels [See also 44A15]
- 45H99 None of the above, but in this section
- 45Jxx Integro-ordinary differential equations [See also 34K05, 34K30, 47G20]**
- 45J05 Integro-ordinary differential equations [See also 34K05, 34K30, 47G20]
- 45J99 None of the above, but in this section
- 45Kxx Integro-partial differential equations [See also 34K30, 35R09, 35R10, 47G20]**
- 45K05 Integro-partial differential equations [See also 34K30, 35R09, 35R10, 47G20]
- 45K99 None of the above, but in this section
- 45Lxx Theoretical approximation of solutions  $\{\{\}\}$ For numerical analysis, see 65Rxx**
- 45L05 Theoretical approximation of solutions  $\{\{\}\}$ For numerical analysis, see 65Rxx
- 45L99 None of the above, but in this section
- 45Mxx Qualitative behavior**
- 45M05 Asymptotics
- 45M10 Stability theory
- 45M15 Periodic solutions
- 45M20 Positive solutions
- 45M99 None of the above, but in this section
- 45Nxx Abstract integral equations, integral equations in abstract spaces**
- 45N05 Abstract integral equations, integral equations in abstract spaces
- 45N99 None of the above, but in this section
- 45Pxx Integral operators [See also 47B38, 47G10]**
- 45P05 Integral operators [See also 47B38, 47G10]
- 45P99 None of the above, but in this section
- 45Qxx Inverse problems**
- 45Q05 Inverse problems
- 45Q99 None of the above, but in this section
- 45Rxx Random integral equations [See also 60H20]**
- 45R05 Random integral equations [See also 60H20]
- 45R99 None of the above, but in this section

- 46-XX FUNCTIONAL ANALYSIS FOR MANIFOLDS MODELED ON TOPOLOGICAL LINEAR SPACES, SEE 57NXX, 58BXX {}**
- 46-00 General reference works (handbooks, dictionaries, bibliographies, etc.)
  - 46-01 Instructional exposition (textbooks, tutorial papers, etc.)
  - 46-02 Research exposition (monographs, survey articles)
  - 46-03 Historical (must also be assigned at least one classification number from Section 01)
  - 46-04 Explicit machine computation and programs (not the theory of computation or programming)
  - 46-06 Proceedings, conferences, collections, etc.
  - 46Axx Topological linear spaces and related structures {} {} For function spaces, see 46Exx**
  - 46A03 General theory of locally convex spaces
  - 46A04 Locally convex Fréchet spaces and (DF)-spaces
  - 46A08 Barrelled spaces, bornological spaces
  - 46A11 Spaces determined by compactness or summability properties (nuclear spaces, Schwartz spaces, Montel spaces, etc.)
  - 46A13 Spaces defined by inductive or projective limits (LB, LF, etc.) [See also 46M40]
  - 46A16 Not locally convex spaces (metrizable topological linear spaces, locally bounded spaces, quasi-Banach spaces, etc.)
  - 46A17 Bornologies and related structures; Mackey convergence, etc.
  - 46A19 Other “topological” linear spaces (convergence spaces, ranked spaces, spaces with a metric taking values in an ordered structure more general than  $\mathbf{R}$ , etc.)
  - 46A20 Duality theory
  - 46A22 Theorems of Hahn-Banach type; extension and lifting of functionals and operators [See also 46M10]
  - 46A25 Reflexivity and semi-reflexivity [See also 46B10]
  - 46A30 Open mapping and closed graph theorems; completeness (including  $B$ -,  $B_r$ -completeness)
  - 46A32 Spaces of linear operators; topological tensor products; approximation properties [See also 46B28, 46M05, 47L05, 47L20]
  - 46A35 Summability and bases [See also 46B15]
  - 46A40 Ordered topological linear spaces, vector lattices [See also 06F20, 46B40, 46B42]
  - 46A45 Sequence spaces (including Köthe sequence spaces) [See also 46B45]
  - 46A50 Compactness in topological linear spaces; angelic spaces, etc.
  - 46A55 Convex sets in topological linear spaces; Choquet theory [See also 52A07]
  - 46A61 Graded Fréchet spaces and tame operators
  - 46A63 Topological invariants ((DN),  $(\Omega)$ , etc.)
  - 46A70 Saks spaces and their duals (strict topologies, mixed topologies, two-norm spaces, co-Saks spaces, etc.)
  - 46A80 Modular spaces
  - 46A99 None of the above, but in this section
  - 46Bxx Normed linear spaces and Banach spaces; Banach lattices {} {} For function spaces, see 46Exx**
  - 46B03 Isomorphic theory (including renorming) of Banach spaces
  - 46B04 Isometric theory of Banach spaces
  - 46B06 Asymptotic theory of Banach spaces [See also 52A23]

- 46B07 Local theory of Banach spaces
- 46B08 Ultraproduct techniques in Banach space theory [See also 46M07]
- 46B09 Probabilistic methods in Banach space theory [See also 60Bxx]
- 46B10 Duality and reflexivity [See also 46A25]
- 46B15 Summability and bases [See also 46A35]
- 46B20 Geometry and structure of normed linear spaces
- 46B22 Radon-Nikodým, Kreĭn-Milman and related properties  
[See also 46G10]
- 46B25 Classical Banach spaces in the general theory
- 46B26 Nonseparable Banach spaces
- 46B28 Spaces of operators; tensor products; approximation properties  
[See also 46A32, 46M05, 47L05, 47L20]
- 46B40 Ordered normed spaces [See also 46A40, 46B42]
- 46B42 Banach lattices [See also 46A40, 46B40]
- 46B45 Banach sequence spaces [See also 46A45]
- 46B50 Compactness in Banach (or normed) spaces
- 46B70 Interpolation between normed linear spaces [See also 46M35]
- 46B80 Nonlinear classification of Banach spaces; nonlinear quotients
- 46B85 Embeddings of discrete metric spaces into Banach spaces;  
applications in topology and computer science [See also 05C12,  
68Rxx]
- 46B99 None of the above, but in this section
- 46Cxx Inner product spaces and their generalizations, Hilbert spaces**  
**{{}}For function spaces, see 46Exx**
- 46C05 Hilbert and pre-Hilbert spaces: geometry and topology (including  
spaces with semidefinite inner product)
- 46C07 Hilbert subspaces (= operator ranges); complementation (Aronszajn,  
de Branges, etc.) [See also 46B70, 46M35]
- 46C15 Characterizations of Hilbert spaces
- 46C20 Spaces with indefinite inner product (Kreĭn spaces, Pontryagin  
spaces, etc.) [See also 47B50]
- 46C50 Generalizations of inner products (semi-inner products, partial inner  
products, etc.)
- 46C99 None of the above, but in this section
- 46Exx Linear function spaces and their duals [See also 30H05, 32A38,**  
**46F05] {{}}For function algebras, see 46J10**
- 46E05 Lattices of continuous, differentiable or analytic functions
- 46E10 Topological linear spaces of continuous, differentiable or analytic  
functions
- 46E15 Banach spaces of continuous, differentiable or analytic functions
- 46E20 Hilbert spaces of continuous, differentiable or analytic functions
- 46E22 Hilbert spaces with reproducing kernels (= [proper] functional  
Hilbert spaces, including de Branges-Rovnyak and other structured  
spaces) [See also 47B32]
- 46E25 Rings and algebras of continuous, differentiable or analytic functions  
{{}}For Banach function algebras, see 46J10, 46J15
- 46E27 Spaces of measures [See also 28A33, 46Gxx]
- 46E30 Spaces of measurable functions ( $L^p$ -spaces, Orlicz spaces, Köthe  
function spaces, Lorentz spaces, rearrangement invariant spaces, ideal  
spaces, etc.)
- 46E35 Sobolev spaces and other spaces of “smooth” functions, embedding  
theorems, trace theorems

- 46E39 Sobolev (and similar kinds of) spaces of functions of discrete variables
- 46E40 Spaces of vector- and operator-valued functions
- 46E50 Spaces of differentiable or holomorphic functions on infinite-dimensional spaces [See also 46G20, 46G25, 47H60]
- 46E99 None of the above, but in this section
- 46Fxx Distributions, generalized functions, distribution spaces [See also 46T30]**
- 46F05 Topological linear spaces of test functions, distributions and ultradistributions [See also 46E10, 46E35]
- 46F10 Operations with distributions
- 46F12 Integral transforms in distribution spaces [See also 42–XX, 44–XX]
- 46F15 Hyperfunctions, analytic functionals [See also 32A25, 32A45, 32C35, 58J15]
- 46F20 Distributions and ultradistributions as boundary values of analytic functions [See also 30D40, 30E25, 32A40]
- 46F25 Distributions on infinite-dimensional spaces [See also 58C35]
- 46F30 Generalized functions for nonlinear analysis (Rosinger, Colombeau, nonstandard, etc.)
- 46F99 None of the above, but in this section
- 46Gxx Measures, integration, derivative, holomorphy (all involving infinite-dimensional spaces) [See also 28–XX, 46Txx]**
- 46G05 Derivatives [See also 46T20, 58C20, 58C25]
- 46G10 Vector-valued measures and integration [See also 28Bxx, 46B22]
- 46G12 Measures and integration on abstract linear spaces [See also 28C20, 46T12]
- 46G15 Functional analytic lifting theory [See also 28A51]
- 46G20 Infinite-dimensional holomorphy [See also 32–XX, 46E50, 46T25, 58B12, 58C10]
- 46G25 (Spaces of) multilinear mappings, polynomials [See also 46E50, 46G20, 47H60]
- 46G99 None of the above, but in this section
- 46Hxx Topological algebras, normed rings and algebras, Banach algebras  $\{\}$ For group algebras, convolution algebras and measure algebras, see 43A10, 43A20**
- 46H05 General theory of topological algebras
- 46H10 Ideals and subalgebras
- 46H15 Representations of topological algebras
- 46H20 Structure, classification of topological algebras
- 46H25 Normed modules and Banach modules, topological modules (if not placed in 13–XX or 16–XX)
- 46H30 Functional calculus in topological algebras [See also 47A60]
- 46H35 Topological algebras of operators [See mainly 47Lxx]
- 46H40 Automatic continuity
- 46H70 Nonassociative topological algebras [See also 46K70, 46L70]
- 46H99 None of the above, but in this section
- 46Jxx Commutative Banach algebras and commutative topological algebras [See also 46E25]**
- 46J05 General theory of commutative topological algebras
- 46J10 Banach algebras of continuous functions, function algebras [See also 46E25]

- 46J15 Banach algebras of differentiable or analytic functions,  $H^p$ -spaces  
[See also 30H10, 32A35, 32A37, 32A38, 42B30]
- 46J20 Ideals, maximal ideals, boundaries
- 46J25 Representations of commutative topological algebras
- 46J30 Subalgebras
- 46J40 Structure, classification of commutative topological algebras
- 46J45 Radical Banach algebras
- 46J99 None of the above, but in this section
- 46Kxx Topological (rings and) algebras with an involution [See also 16W10]**
- 46K05 General theory of topological algebras with involution
- 46K10 Representations of topological algebras with involution
- 46K15 Hilbert algebras
- 46K50 Nonselfadjoint (sub)algebras in algebras with involution
- 46K70 Nonassociative topological algebras with an involution  
[See also 46H70, 46L70]
- 46K99 None of the above, but in this section
- 46Lxx Selfadjoint operator algebras ( $C^*$ -algebras, von Neumann ( $W^*$ -) algebras, etc.) [See also 22D25, 47Lxx]**
- 46L05 General theory of  $C^*$ -algebras
- 46L06 Tensor products of  $C^*$ -algebras
- 46L07 Operator spaces and completely bounded maps [See also 47L25]
- 46L08  $C^*$ -modules
- 46L09 Free products of  $C^*$ -algebras
- 46L10 General theory of von Neumann algebras
- 46L30 States
- 46L35 Classifications of  $C^*$ -algebras
- 46L36 Classification of factors
- 46L37 Subfactors and their classification
- 46L40 Automorphisms
- 46L45 Decomposition theory for  $C^*$ -algebras
- 46L51 Noncommutative measure and integration
- 46L52 Noncommutative function spaces
- 46L53 Noncommutative probability and statistics
- 46L54 Free probability and free operator algebras
- 46L55 Noncommutative dynamical systems [See also 28Dxx, 37Kxx, 37Lxx, 54H20]
- 46L57 Derivations, dissipations and positive semigroups in  $C^*$ -algebras
- 46L60 Applications of selfadjoint operator algebras to physics  
[See also 46N50, 46N55, 47L90, 81T05, 82B10, 82C10]
- 46L65 Quantizations, deformations
- 46L70 Nonassociative selfadjoint operator algebras [See also 46H70, 46K70]
- 46L80  $K$ -theory and operator algebras (including cyclic theory)  
[See also 18F25, 19Kxx, 46M20, 55Rxx, 58J22]
- 46L85 Noncommutative topology [See also 58B32, 58B34, 58J22]
- 46L87 Noncommutative differential geometry [See also 58B32, 58B34, 58J22]
- 46L89 Other “noncommutative” mathematics based on  $C^*$ -algebra theory  
[See also 58B32, 58B34, 58J22]
- 46L99 None of the above, but in this section
- 46Mxx Methods of category theory in functional analysis [See also 18–XX]**
- 46M05 Tensor products [See also 46A32, 46B28, 47A80]
- 46M07 Ultraproducts [See also 46B08, 46S20]

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- 46M10 Projective and injective objects [See also 46A22]
- 46M15 Categories, functors  $\{\{\}\}$  For  $K$ -theory, EXT, etc., see 19K33, 46L80, 46M18, 46M20
- 46M18 Homological methods (exact sequences, right inverses, lifting, etc.)
- 46M20 Methods of algebraic topology (cohomology, sheaf and bundle theory, etc.) [See also 14F05, 18Fxx, 19Kxx, 32Cxx, 32Lxx, 46L80, 46M15, 46M18, 55Rxx]
- 46M35 Abstract interpolation of topological vector spaces [See also 46B70]
- 46M40 Inductive and projective limits [See also 46A13]
- 46M99 None of the above, but in this section
- 46Nxx Miscellaneous applications of functional analysis [See also 47Nxx]**
- 46N10 Applications in optimization, convex analysis, mathematical programming, economics
- 46N20 Applications to differential and integral equations
- 46N30 Applications in probability theory and statistics
- 46N40 Applications in numerical analysis [See also 65Jxx]
- 46N50 Applications in quantum physics
- 46N55 Applications in statistical physics
- 46N60 Applications in biology and other sciences
- 46N99 None of the above, but in this section
- 46Sxx Other (nonclassical) types of functional analysis [See also 47Sxx]**
- 46S10 Functional analysis over fields other than  $\mathbf{R}$  or  $\mathbf{C}$  or the quaternions; non-Archimedean functional analysis [See also 12J25, 32P05]
- 46S20 Nonstandard functional analysis [See also 03H05]
- 46S30 Constructive functional analysis [See also 03F60]
- 46S40 Fuzzy functional analysis [See also 03E72]
- 46S50 Functional analysis in probabilistic metric linear spaces
- 46S60 Functional analysis on superspaces (supermanifolds) or graded spaces [See also 58A50 and 58C50]
- 46S99 None of the above, but in this section
- 46Txx Nonlinear functional analysis [See also 47Hxx, 47Jxx, 58Cxx, 58Dxx]**
- 46T05 Infinite-dimensional manifolds [See also 53Axx, 57N20, 58Bxx, 58Dxx]
- 46T10 Manifolds of mappings
- 46T12 Measure (Gaussian, cylindrical, etc.) and integrals (Feynman, path, Fresnel, etc.) on manifolds [See also 28Cxx, 46G12, 60-XX]
- 46T20 Continuous and differentiable maps [See also 46G05]
- 46T25 Holomorphic maps [See also 46G20]
- 46T30 Distributions and generalized functions on nonlinear spaces [See also 46Fxx]
- 46T99 None of the above, but in this section
- 47-XX OPERATOR THEORY**
- 47-00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 47-01 Instructional exposition (textbooks, tutorial papers, etc.)
- 47-02 Research exposition (monographs, survey articles)
- 47-03 Historical (must also be assigned at least one classification number from Section 01)
- 47-04 Explicit machine computation and programs (not the theory of computation or programming)
- 47-06 Proceedings, conferences, collections, etc.

- 47Axx General theory of linear operators**
- 47A05 General (adjoints, conjugates, products, inverses, domains, ranges, etc.)
- 47A06 Linear relations (multivalued linear operators)
- 47A07 Forms (bilinear, sesquilinear, multilinear)
- 47A10 Spectrum, resolvent
- 47A11 Local spectral properties
- 47A12 Numerical range, numerical radius
- 47A13 Several-variable operator theory (spectral, Fredholm, etc.)
- 47A15 Invariant subspaces [See also 47A46]
- 47A16 Cyclic vectors, hypercyclic and chaotic operators
- 47A20 Dilations, extensions, compressions
- 47A25 Spectral sets
- 47A30 Norms (inequalities, more than one norm, etc.)
- 47A35 Ergodic theory [See also 28Dxx, 37Axx]
- 47A40 Scattering theory [See also 34L25, 35P25, 37K15, 58J50, 81Uxx]
- 47A45 Canonical models for contractions and nonselfadjoint operators
- 47A46 Chains (nests) of projections or of invariant subspaces, integrals along chains, etc.
- 47A48 Operator colligations (= nodes), vessels, linear systems, characteristic functions, realizations, etc.
- 47A50 Equations and inequalities involving linear operators, with vector unknowns
- 47A52 Ill-posed problems, regularization [See also 35R25, 47J06, 65F22, 65J20, 65L08, 65M30, 65R30]
- 47A53 (Semi-) Fredholm operators; index theories [See also 58B15, 58J20]
- 47A55 Perturbation theory [See also 47H14, 58J37, 70H09, 81Q15]
- 47A56 Functions whose values are linear operators (operator and matrix valued functions, etc., including analytic and meromorphic ones)
- 47A57 Operator methods in interpolation, moment and extension problems [See also 30E05, 42A70, 42A82, 44A60]
- 47A58 Operator approximation theory
- 47A60 Functional calculus
- 47A62 Equations involving linear operators, with operator unknowns
- 47A63 Operator inequalities
- 47A64 Operator means, shorted operators, etc.
- 47A65 Structure theory
- 47A66 Quasitriangular and nonquasitriangular, quasideagonal and nonquasideagonal operators
- 47A67 Representation theory
- 47A68 Factorization theory (including Wiener-Hopf and spectral factorizations)
- 47A70 (Generalized) eigenfunction expansions; rigged Hilbert spaces
- 47A75 Eigenvalue problems [See also 47J10, 49R05]
- 47A80 Tensor products of operators [See also 46M05]
- 47A99 None of the above, but in this section
- 47Bxx Special classes of linear operators**
- 47B06 Riesz operators; eigenvalue distributions; approximation numbers,  $s$ -numbers, Kolmogorov numbers, entropy numbers, etc. of operators
- 47B07 Operators defined by compactness properties
- 47B10 Operators belonging to operator ideals (nuclear,  $p$ -summing, in the Schatten-von Neumann classes, etc.) [See also 47L20]

- 47B15 Hermitian and normal operators (spectral measures, functional calculus, etc.)
- 47B20 Subnormal operators, hyponormal operators, etc.
- 47B25 Symmetric and selfadjoint operators (unbounded)
- 47B32 Operators in reproducing-kernel Hilbert spaces (including de Branges, de Branges-Rovnyak, and other structured spaces)  
[See also 46E22]
- 47B33 Composition operators
- 47B34 Kernel operators
- 47B35 Toeplitz operators, Hankel operators, Wiener-Hopf operators  
[See also 45P05, 47G10 for other integral operators; see also 32A25, 32M15]
- 47B36 Jacobi (tridiagonal) operators (matrices) and generalizations
- 47B37 Operators on special spaces (weighted shifts, operators on sequence spaces, etc.)
- 47B38 Operators on function spaces (general)
- 47B39 Difference operators [See also 39A70]
- 47B40 Spectral operators, decomposable operators, well-bounded operators, etc.
- 47B44 Accretive operators, dissipative operators, etc.
- 47B47 Commutators, derivations, elementary operators, etc.
- 47B48 Operators on Banach algebras
- 47B49 Transformers, preservers (operators on spaces of operators)
- 47B50 Operators on spaces with an indefinite metric [See also 46C50]
- 47B60 Operators on ordered spaces
- 47B65 Positive operators and order-bounded operators
- 47B80 Random operators [See also 47H40, 60H25]
- 47B99 None of the above, but in this section
- 47Cxx Individual linear operators as elements of algebraic systems**
- 47C05 Operators in algebras
- 47C10 Operators in \*-algebras
- 47C15 Operators in  $C^*$ - or von Neumann algebras
- 47C99 None of the above, but in this section
- 47Dxx Groups and semigroups of linear operators, their generalizations and applications**
- 47D03 Groups and semigroups of linear operators  $\{\{\}\}$ For nonlinear operators, see 47H20; see also 20M20
- 47D06 One-parameter semigroups and linear evolution equations  
[See also 34G10, 34K30]
- 47D07 Markov semigroups and applications to diffusion processes  $\{\{\}\}$ For Markov processes, see 60Jxx
- 47D08 Schrödinger and Feynman-Kac semigroups
- 47D09 Operator sine and cosine functions and higher-order Cauchy problems  
[See also 34G10]
- 47D60  $C$ -semigroups, regularized semigroups
- 47D62 Integrated semigroups
- 47D99 None of the above, but in this section
- 47Exx Ordinary differential operators [See also 34Bxx, 34Lxx]**
- 47E05 Ordinary differential operators [See also 34Bxx, 34Lxx] (should also be assigned at least one other classification number in section 47)
- 47E99 None of the above, but in this section

- 47Fxx Partial differential operators [See also 35Pxx, 58Jxx]**  
 47F05 Partial differential operators [See also 35Pxx, 58Jxx] (should also be assigned at least one other classification number in section 47)  
 47F99 None of the above, but in this section  
**47Gxx Integral, integro-differential, and pseudodifferential operators [See also 58Jxx]**  
 47G10 Integral operators [See also 45P05]  
 47G20 Integro-differential operators [See also 34K30, 35R09, 35R10, 45Jxx, 45Kxx]  
 47G30 Pseudodifferential operators [See also 35Sxx, 58Jxx]  
 47G40 Potential operators [See also 31–XX]  
 47G99 None of the above, but in this section  
**47Hxx Nonlinear operators and their properties { } For global and geometric aspects, see 58–XX, especially 58Cxx**  
 47H04 Set-valued operators [See also 28B20, 54C60, 58C06]  
 47H05 Monotone operators and generalizations  
 47H06 Accretive operators, dissipative operators, etc.  
 47H07 Monotone and positive operators on ordered Banach spaces or other ordered topological vector spaces  
 47H08 Measures of noncompactness and condensing mappings,  $K$ -set contractions, etc.  
 47H09 Contraction-type mappings, nonexpansive mappings,  $A$ -proper mappings, etc.  
 47H10 Fixed-point theorems [See also 37C25, 54H25, 55M20, 58C30]  
 47H11 Degree theory [See also 55M25, 58C30]  
 47H14 Perturbations of nonlinear operators [See also 47A55, 58J37, 70H09, 70K60, 81Q15]  
 47H20 Semigroups of nonlinear operators [See also 37L05, 47J35, 54H15, 58D07]  
 47H25 Nonlinear ergodic theorems [See also 28Dxx, 37Axx, 47A35]  
 47H30 Particular nonlinear operators (superposition, Hammerstein, Nemytskiĭ, Uryson, etc.) [See also 45Gxx, 45P05]  
 47H40 Random operators [See also 47B80, 60H25]  
 47H60 Multilinear and polynomial operators [See also 46G25]  
 47H99 None of the above, but in this section  
**47Jxx Equations and inequalities involving nonlinear operators [See also 46Txx] { } For global and geometric aspects, see 58–XX**  
 47J05 Equations involving nonlinear operators (general) [See also 47H10, 47J25]  
 47J06 Nonlinear ill-posed problems [See also 35R25, 47A52, 65F22, 65J20, 65L08, 65M30, 65R30]  
 47J07 Abstract inverse mapping and implicit function theorems [See also 46T20 and 58C15]  
 47J10 Nonlinear spectral theory, nonlinear eigenvalue problems [See also 49R05]  
 47J15 Abstract bifurcation theory [See also 34C23, 37Gxx, 58E07, 58E09]  
 47J20 Variational and other types of inequalities involving nonlinear operators (general) [See also 49J40]  
 47J22 Variational and other types of inclusions [See also 34A60, 49J21, 49K21]  
 47J25 Iterative procedures [See also 65J15]  
 47J30 Variational methods [See also 58Exx]

- 47J35 Nonlinear evolution equations [See also 34G20, 35K90, 35L90, 35Qxx, 35R20, 37Kxx, 37Lxx, 47H20, 58D25]
- 47J40 Equations with hysteresis operators [See also 34C55, 74N30]
- 47J99 None of the above, but in this section
- 47Lxx Linear spaces and algebras of operators [See also 46Lxx]**
- 47L05 Linear spaces of operators [See also 46A32 and 46B28]
- 47L07 Convex sets and cones of operators [See also 46A55]
- 47L10 Algebras of operators on Banach spaces and other topological linear spaces
- 47L15 Operator algebras with symbol structure
- 47L20 Operator ideals [See also 47B10]
- 47L22 Ideals of polynomials and of multilinear mappings
- 47L25 Operator spaces (= matricially normed spaces) [See also 46L07]
- 47L30 Abstract operator algebras on Hilbert spaces
- 47L35 Nest algebras, CSL algebras
- 47L40 Limit algebras, subalgebras of  $C^*$ -algebras
- 47L45 Dual algebras; weakly closed singly generated operator algebras
- 47L50 Dual spaces of operator algebras
- 47L55 Representations of (nonselfadjoint) operator algebras
- 47L60 Algebras of unbounded operators; partial algebras of operators
- 47L65 Crossed product algebras (analytic crossed products)
- 47L70 Nonassociative nonselfadjoint operator algebras
- 47L75 Other nonselfadjoint operator algebras
- 47L80 Algebras of specific types of operators (Toeplitz, integral, pseudodifferential, etc.)
- 47L90 Applications of operator algebras to physics
- 47L99 None of the above, but in this section
- 47Nxx Miscellaneous applications of operator theory [See also 46Nxx]**
- 47N10 Applications in optimization, convex analysis, mathematical programming, economics
- 47N20 Applications to differential and integral equations
- 47N30 Applications in probability theory and statistics
- 47N40 Applications in numerical analysis [See also 65Jxx]
- 47N50 Applications in the physical sciences
- 47N60 Applications in chemistry and life sciences
- 47N70 Applications in systems theory, circuits, and control theory
- 47N99 None of the above, but in this section
- 47Sxx Other (nonclassical) types of operator theory [See also 46Sxx]**
- 47S10 Operator theory over fields other than  $\mathbf{R}$ ,  $\mathbf{C}$  or the quaternions; non-Archimedean operator theory
- 47S20 Nonstandard operator theory [See also 03H05]
- 47S30 Constructive operator theory [See also 03F60]
- 47S40 Fuzzy operator theory [See also 03E72]
- 47S50 Operator theory in probabilistic metric linear spaces [See also 54E70]
- 47S99 None of the above, but in this section
- 49–XX CALCULUS OF VARIATIONS AND OPTIMAL CONTROL; OPTIMIZATION [See also 34H05, 34K35, 65Kxx, 90Cxx, 93–XX]**
- 49–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 49–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 49–02 Research exposition (monographs, survey articles)

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- 49-03 Historical (must also be assigned at least one classification number from Section 01)
- 49-04 Explicit machine computation and programs (not the theory of computation or programming)
- 49-06 Proceedings, conferences, collections, etc.
- 49Jxx Existence theories**
- 49J05 Free problems in one independent variable
- 49J10 Free problems in two or more independent variables
- 49J15 Optimal control problems involving ordinary differential equations
- 49J20 Optimal control problems involving partial differential equations
- 49J21 Optimal control problems involving relations other than differential equations
- 49J27 Problems in abstract spaces [See also 90C48, 93C25]
- 49J30 Optimal solutions belonging to restricted classes (Lipschitz controls, bang-bang controls, etc.)
- 49J35 Minimax problems
- 49J40 Variational methods including variational inequalities [See also 47J20]
- 49J45 Methods involving semicontinuity and convergence; relaxation
- 49J50 Fréchet and Gateaux differentiability [See also 46G05, 58C20]
- 49J52 Nonsmooth analysis [See also 46G05, 58C50, 90C56]
- 49J53 Set-valued and variational analysis [See also 28B20, 47H04, 54C60, 58C06]
- 49J55 Problems involving randomness [See also 93E20]
- 49J99 None of the above, but in this section
- 49Kxx Optimality conditions**
- 49K05 Free problems in one independent variable
- 49K10 Free problems in two or more independent variables
- 49K15 Problems involving ordinary differential equations
- 49K20 Problems involving partial differential equations
- 49K21 Problems involving relations other than differential equations
- 49K27 Problems in abstract spaces [See also 90C48, 93C25]
- 49K30 Optimal solutions belonging to restricted classes
- 49K35 Minimax problems
- 49K40 Sensitivity, stability, well-posedness [See also 90C31]
- 49K45 Problems involving randomness [See also 93E20]
- 49K99 None of the above, but in this section
- 49Lxx Hamilton-Jacobi theories, including dynamic programming**
- 49L20 Dynamic programming method
- 49L25 Viscosity solutions
- 49L99 None of the above, but in this section
- 49Mxx Numerical methods [See also 90Cxx, 65Kxx]**
- 49M05 Methods based on necessary conditions
- 49M15 Newton-type methods
- 49M20 Methods of relaxation type
- 49M25 Discrete approximations
- 49M27 Decomposition methods
- 49M29 Methods involving duality
- 49M30 Other methods
- 49M37 Methods of nonlinear programming type [See also 90C30, 65Kxx]
- 49M99 None of the above, but in this section

- 49Nxx** **Miscellaneous topics**
- 49N05 Linear optimal control problems [See also 93C05]
- 49N10 Linear-quadratic problems
- 49N15 Duality theory
- 49N20 Periodic optimization
- 49N25 Impulsive optimal control problems
- 49N30 Problems with incomplete information [See also 93C41]
- 49N35 Optimal feedback synthesis [See also 93B52]
- 49N45 Inverse problems
- 49N60 Regularity of solutions
- 49N70 Differential games
- 49N75 Pursuit and evasion games
- 49N90 Applications of optimal control and differential games  
[See also 90C90, 93C95]
- 49N99 None of the above, but in this section
- 49Qxx** **Manifolds [See also 58Exx]**
- 49Q05 Minimal surfaces [See also 53A10, 58E12]
- 49Q10 Optimization of shapes other than minimal surfaces [See also 90C90]
- 49Q12 Sensitivity analysis
- 49Q15 Geometric measure and integration theory, integral and normal  
currents [See also 28A75, 32C30, 58A25, 58C35]
- 49Q20 Variational problems in a geometric measure-theoretic setting
- 49Q99 None of the above, but in this section
- 49Rxx** **Variational methods for eigenvalues of operators [See also 47A75]**  
**(should also be assigned at least one other classification number in  
this section)**
- 49R05 Variational methods for eigenvalues of operators [See also 47A75]  
(should also be assigned at least one other classification number in  
section 49)
- 49R99 None of the above, but in this section
- 49Sxx** **Variational principles of physics (should also be assigned at least one  
other classification number in this section)**
- 49S05 Variational principles of physics (should also be assigned at least one  
other classification number in section 49)
- 49S99 None of the above, but in this section
- 51-XX** **GEOMETRY FOR ALGEBRAIC GEOMETRY, SEE 14-XX{}**
- 51-00 General reference works (handbooks, dictionaries, bibliographies,  
etc.)
- 51-01 Instructional exposition (textbooks, tutorial papers, etc.)
- 51-02 Research exposition (monographs, survey articles)
- 51-03 Historical (must also be assigned at least one classification number  
from Section 01)
- 51-04 Explicit machine computation and programs (not the theory of  
computation or programming)
- 51-06 Proceedings, conferences, collections, etc.
- 51Axx** **Linear incidence geometry**
- 51A05 General theory and projective geometries
- 51A10 Homomorphism, automorphism and dualities
- 51A15 Structures with parallelism
- 51A20 Configuration theorems
- 51A25 Algebraization [See also 12Kxx, 20N05]

- 51A30 Desarguesian and Pappian geometries
- 51A35 Non-Desarguesian affine and projective planes
- 51A40 Translation planes and spreads
- 51A45 Incidence structures imbeddable into projective geometries
- 51A50 Polar geometry, symplectic spaces, orthogonal spaces
- 51A99 None of the above, but in this section
- 51Bxx Nonlinear incidence geometry**
- 51B05 General theory
- 51B10 Möbius geometries
- 51B15 Laguerre geometries
- 51B20 Minkowski geometries
- 51B25 Lie geometries
- 51B99 None of the above, but in this section
- 51Cxx Ring geometry (Hjelmslev, Barbilian, etc.)**
- 51C05 Ring geometry (Hjelmslev, Barbilian, etc.)
- 51C99 None of the above, but in this section
- 51Dxx Geometric closure systems**
- 51D05 Abstract (Maeda) geometries
- 51D10 Abstract geometries with exchange axiom
- 51D15 Abstract geometries with parallelism
- 51D20 Combinatorial geometries [See also 05B25, 05B35]
- 51D25 Lattices of subspaces [See also 05B35]
- 51D30 Continuous geometries and related topics [See also 06Cxx]
- 51D99 None of the above, but in this section
- 51Exx Finite geometry and special incidence structures**
- 51E05 General block designs [See also 05B05]
- 51E10 Steiner systems
- 51E12 Generalized quadrangles, generalized polygons
- 51E14 Finite partial geometries (general), nets, partial spreads
- 51E15 Affine and projective planes
- 51E20 Combinatorial structures in finite projective spaces [See also 05Bxx]
- 51E21 Blocking sets, ovals,  $k$ -arcs
- 51E22 Linear codes and caps in Galois spaces [See also 94B05]
- 51E23 Spreads and packing problems
- 51E24 Buildings and the geometry of diagrams
- 51E25 Other finite nonlinear geometries
- 51E26 Other finite linear geometries
- 51E30 Other finite incidence structures [See also 05B30]
- 51E99 None of the above, but in this section
- 51Fxx Metric geometry**
- 51F05 Absolute planes
- 51F10 Absolute spaces
- 51F15 Reflection groups, reflection geometries [See also 20H10, 20H15; for Coxeter groups, see 20F55]
- 51F20 Congruence and orthogonality [See also 20H05]
- 51F25 Orthogonal and unitary groups [See also 20H05]
- 51F99 None of the above, but in this section
- 51Gxx Ordered geometries (ordered incidence structures, etc.)**
- 51G05 Ordered geometries (ordered incidence structures, etc.)
- 51G99 None of the above, but in this section

- 51Hxx Topological geometry**
- 51H05 General theory
- 51H10 Topological linear incidence structures
- 51H15 Topological nonlinear incidence structures
- 51H20 Topological geometries on manifolds [See also 57–XX]
- 51H25 Geometries with differentiable structure [See also 53Cxx, 53C70]
- 51H30 Geometries with algebraic manifold structure [See also 14–XX]
- 51H99 None of the above, but in this section
- 51Jxx Incidence groups**
- 51J05 General theory
- 51J10 Projective incidence groups
- 51J15 Kinematic spaces
- 51J20 Representation by near-fields and near-algebras [See also 12K05, 16Y30]
- 51J99 None of the above, but in this section
- 51Kxx Distance geometry**
- 51K05 General theory
- 51K10 Synthetic differential geometry
- 51K99 None of the above, but in this section
- 51Lxx Geometric order structures [See also 53C75]**
- 51L05 Geometry of orders of nondifferentiable curves
- 51L10 Directly differentiable curves
- 51L15  $n$ -vertex theorems via direct methods
- 51L20 Geometry of orders of surfaces
- 51L99 None of the above, but in this section
- 51Mxx Real and complex geometry**
- 51M04 Elementary problems in Euclidean geometries
- 51M05 Euclidean geometries (general) and generalizations
- 51M09 Elementary problems in hyperbolic and elliptic geometries
- 51M10 Hyperbolic and elliptic geometries (general) and generalizations
- 51M15 Geometric constructions
- 51M16 Inequalities and extremum problems  $\{\{\}\}$ For convex problems, see 52A40
- 51M20 Polyhedra and polytopes; regular figures, division of spaces  
[See also 51F15]
- 51M25 Length, area and volume [See also 26B15]
- 51M30 Line geometries and their generalizations [See also 53A25]
- 51M35 Synthetic treatment of fundamental manifolds in projective geometries (Grassmannians, Veronesians and their generalizations)  
[See also 14M15]
- 51M99 None of the above, but in this section
- 51Nxx Analytic and descriptive geometry**
- 51N05 Descriptive geometry [See also 65D17, 68U07]
- 51N10 Affine analytic geometry
- 51N15 Projective analytic geometry
- 51N20 Euclidean analytic geometry
- 51N25 Analytic geometry with other transformation groups
- 51N30 Geometry of classical groups [See also 20Gxx, 14L35]
- 51N35 Questions of classical algebraic geometry [See also 14Nxx]
- 51N99 None of the above, but in this section

- 51Pxx**    **Geometry and physics (should also be assigned at least one other classification number from Sections 70–86)**
- 51P05    Geometry and physics (should also be assigned at least one other classification number from Sections 70–86)
- 51P99    None of the above, but in this section
- 52–XX**    **CONVEX AND DISCRETE GEOMETRY**
- 52–00    General reference works (handbooks, dictionaries, bibliographies, etc.)
- 52–01    Instructional exposition (textbooks, tutorial papers, etc.)
- 52–02    Research exposition (monographs, survey articles)
- 52–03    Historical (must also be assigned at least one classification number from Section 01)
- 52–04    Explicit machine computation and programs (not the theory of computation or programming)
- 52–06    Proceedings, conferences, collections, etc.
- 52Axx**    **General convexity**
- 52A01    Axiomatic and generalized convexity
- 52A05    Convex sets without dimension restrictions
- 52A07    Convex sets in topological vector spaces [See also 46A55]
- 52A10    Convex sets in 2 dimensions (including convex curves)  
[See also 53A04]
- 52A15    Convex sets in 3 dimensions (including convex surfaces)  
[See also 53A05, 53C45]
- 52A20    Convex sets in  $n$  dimensions (including convex hypersurfaces)  
[See also 53A07, 53C45]
- 52A21    Finite-dimensional Banach spaces (including special norms, zonoids, etc.) [See also 46Bxx]
- 52A22    Random convex sets and integral geometry [See also 53C65, 60D05]
- 52A23    Asymptotic theory of convex bodies [See also 46B06]
- 52A27    Approximation by convex sets
- 52A30    Variants of convex sets (star-shaped,  $(m, n)$ -convex, etc.)
- 52A35    Helly-type theorems and geometric transversal theory
- 52A37    Other problems of combinatorial convexity
- 52A38    Length, area, volume [See also 26B15, 28A75, 49Q20]
- 52A39    Mixed volumes and related topics
- 52A40    Inequalities and extremum problems
- 52A41    Convex functions and convex programs [See also 26B25, 90C25]
- 52A55    Spherical and hyperbolic convexity
- 52A99    None of the above, but in this section
- 52Bxx**    **Polytopes and polyhedra**
- 52B05    Combinatorial properties (number of faces, shortest paths, etc.)  
[See also 05Cxx]
- 52B10    Three-dimensional polytopes
- 52B11     $n$ -dimensional polytopes
- 52B12    Special polytopes (linear programming, centrally symmetric, etc.)
- 52B15    Symmetry properties of polytopes
- 52B20    Lattice polytopes (including relations with commutative algebra and algebraic geometry) [See also 06A11, 13F20, 13Hxx]
- 52B22    Shellability
- 52B35    Gale and other diagrams

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- 52B40 Matroids (realizations in the context of convex polytopes, convexity in combinatorial structures, etc.) [See also 05B35, 52Cxx]
- 52B45 Dissections and valuations (Hilbert's third problem, etc.)
- 52B55 Computational aspects related to convexity {}{}For computational geometry and algorithms, see 68Q25, 68U05; for numerical algorithms, see 65Yxx [See also 68Uxx]
- 52B60 Isoperimetric problems for polytopes
- 52B70 Polyhedral manifolds
- 52B99 None of the above, but in this section
- 52Cxx Discrete geometry**
- 52C05 Lattices and convex bodies in 2 dimensions [See also 11H06, 11H31, 11P21]
- 52C07 Lattices and convex bodies in  $n$  dimensions [See also 11H06, 11H31, 11P21]
- 52C10 Erdős problems and related topics of discrete geometry [See also 11Hxx]
- 52C15 Packing and covering in 2 dimensions [See also 05B40, 11H31]
- 52C17 Packing and covering in  $n$  dimensions [See also 05B40, 11H31]
- 52C20 Tilings in 2 dimensions [See also 05B45, 51M20]
- 52C22 Tilings in  $n$  dimensions [See also 05B45, 51M20]
- 52C23 Quasicrystals, aperiodic tilings
- 52C25 Rigidity and flexibility of structures [See also 70B15]
- 52C26 Circle packings and discrete conformal geometry
- 52C30 Planar arrangements of lines and pseudolines
- 52C35 Arrangements of points, flats, hyperplanes [See also 32S22]
- 52C40 Oriented matroids
- 52C45 Combinatorial complexity of geometric structures [See also 68U05]
- 52C99 None of the above, but in this section
- 53–XX DIFFERENTIAL GEOMETRY FOR DIFFERENTIAL TOPOLOGY, SEE 57RXX. FOR FOUNDATIONAL QUESTIONS OF DIFFERENTIABLE MANIFOLDS, SEE 58Axx {}**
- 53–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 53–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 53–02 Research exposition (monographs, survey articles)
- 53–03 Historical (must also be assigned at least one classification number from Section 01)
- 53–04 Explicit machine computation and programs (not the theory of computation or programming)
- 53–06 Proceedings, conferences, collections, etc.
- 53Axx Classical differential geometry**
- 53A04 Curves in Euclidean space
- 53A05 Surfaces in Euclidean space
- 53A07 Higher-dimensional and  $-$ -codimensional surfaces in Euclidean  $n$ -space
- 53A10 Minimal surfaces, surfaces with prescribed mean curvature [See also 49Q05, 49Q10, 53C42]
- 53A15 Affine differential geometry
- 53A17 Kinematics
- 53A20 Projective differential geometry
- 53A25 Differential line geometry
- 53A30 Conformal differential geometry

- 53A35 Non-Euclidean differential geometry
- 53A40 Other special differential geometries
- 53A45 Vector and tensor analysis
- 53A55 Differential invariants (local theory), geometric objects
- 53A60 Geometry of webs [See also 14C21, 20N05]
- 53A99 None of the above, but in this section
- 53Bxx Local differential geometry**
- 53B05 Linear and affine connections
- 53B10 Projective connections
- 53B15 Other connections
- 53B20 Local Riemannian geometry
- 53B21 Methods of Riemannian geometry
- 53B25 Local submanifolds [See also 53C40]
- 53B30 Lorentz metrics, indefinite metrics
- 53B35 Hermitian and Kählerian structures [See also 32Cxx]
- 53B40 Finsler spaces and generalizations (areal metrics)
- 53B50 Applications to physics
- 53B99 None of the above, but in this section
- 53Cxx Global differential geometry [See also 51H25, 58–XX; for related bundle theory, see 55Rxx, 57Rxx]**
- 53C05 Connections, general theory
- 53C07 Special connections and metrics on vector bundles (Hermite-Einstein-Yang-Mills) [See also 32Q20]
- 53C08 Gerbes, differential characters: differential geometric aspects
- 53C10  $G$ -structures
- 53C12 Foliations (differential geometric aspects) [See also 57R30, 57R32]
- 53C15 General geometric structures on manifolds (almost complex, almost product structures, etc.)
- 53C17 Sub-Riemannian geometry
- 53C20 Global Riemannian geometry, including pinching [See also 31C12, 58B20]
- 53C21 Methods of Riemannian geometry, including PDE methods; curvature restrictions [See also 58J60]
- 53C22 Geodesics [See also 58E10]
- 53C23 Global geometric and topological methods (à la Gromov); differential geometric analysis on metric spaces
- 53C24 Rigidity results
- 53C25 Special Riemannian manifolds (Einstein, Sasakian, etc.)
- 53C26 Hyper-Kähler and quaternionic Kähler geometry, “special” geometry
- 53C27 Spin and Spin<sup>c</sup> geometry
- 53C28 Twistor methods [See also 32L25]
- 53C29 Issues of holonomy
- 53C30 Homogeneous manifolds [See also 14M15, 14M17, 32M10, 57T15]
- 53C35 Symmetric spaces [See also 32M15, 57T15]
- 53C38 Calibrations and calibrated geometries
- 53C40 Global submanifolds [See also 53B25]
- 53C42 Immersions (minimal, prescribed curvature, tight, etc.) [See also 49Q05, 49Q10, 53A10, 57R40, 57R42]
- 53C43 Differential geometric aspects of harmonic maps [See also 58E20]
- 53C44 Geometric evolution equations (mean curvature flow, Ricci flow, etc.)
- 53C45 Global surface theory (convex surfaces à la A. D. Aleksandrov)

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- 53C50 Lorentz manifolds, manifolds with indefinite metrics
- 53C55 Hermitian and Kählerian manifolds [See also 32Cxx]
- 53C56 Other complex differential geometry [See also 32Cxx]
- 53C60 Finsler spaces and generalizations (areal metrics) [See also 58B20]
- 53C65 Integral geometry [See also 52A22, 60D05]; differential forms, currents, etc. [See mainly 58Axx]
- 53C70 Direct methods ( $G$ -spaces of Busemann, etc.)
- 53C75 Geometric orders, order geometry [See also 51Lxx]
- 53C80 Applications to physics
- 53C99 None of the above, but in this section
- 53Dxx Symplectic geometry, contact geometry [See also 37Jxx, 70Gxx, 70Hxx]**
- 53D05 Symplectic manifolds, general
- 53D10 Contact manifolds, general
- 53D12 Lagrangian submanifolds; Maslov index
- 53D15 Almost contact and almost symplectic manifolds
- 53D17 Poisson manifolds; Poisson groupoids and algebroids
- 53D18 Generalized geometries (à la Hitchin)
- 53D20 Momentum maps; symplectic reduction
- 53D22 Canonical transformations
- 53D25 Geodesic flows
- 53D30 Symplectic structures of moduli spaces
- 53D35 Global theory of symplectic and contact manifolds [See also 57Rxx]
- 53D37 Mirror symmetry, symplectic aspects; homological mirror symmetry; Fukaya category [See also 14J33]
- 53D40 Floer homology and cohomology, symplectic aspects
- 53D42 Symplectic field theory; contact homology
- 53D45 Gromov-Witten invariants, quantum cohomology, Frobenius manifolds [See also 14N35]
- 53D50 Geometric quantization
- 53D55 Deformation quantization, star products
- 53D99 None of the above, but in this section
- 53Zxx Applications to physics**
- 53Z05 Applications to physics
- 53Z99 None of the above, but in this section
- 54–XX GENERAL TOPOLOGY FOR THE TOPOLOGY OF MANIFOLDS OF ALL DIMENSIONS, SEE 57NXX{}**
- 54–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 54–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 54–02 Research exposition (monographs, survey articles)
- 54–03 Historical (must also be assigned at least one classification number from Section 01)
- 54–04 Explicit machine computation and programs (not the theory of computation or programming)
- 54–06 Proceedings, conferences, collections, etc.
- 54Axx Generalities**
- 54A05 Topological spaces and generalizations (closure spaces, etc.)
- 54A10 Several topologies on one set (change of topology, comparison of topologies, lattices of topologies)
- 54A15 Syntopogeneous structures

- 54A20 Convergence in general topology (sequences, filters, limits, convergence spaces, etc.)
- 54A25 Cardinality properties (cardinal functions and inequalities, discrete subsets) [See also 03Exx] For ultrafilters, see 54D80
- 54A35 Consistency and independence results [See also 03E35]
- 54A40 Fuzzy topology [See also 03E72]
- 54A99 None of the above, but in this section
- 54Bxx Basic constructions**
- 54B05 Subspaces
- 54B10 Product spaces
- 54B15 Quotient spaces, decompositions
- 54B17 Adjunction spaces and similar constructions
- 54B20 Hyperspaces
- 54B30 Categorical methods [See also 18B30]
- 54B35 Spectra
- 54B40 Presheaves and sheaves [See also 18F20]
- 54B99 None of the above, but in this section
- 54Cxx Maps and general types of spaces defined by maps**
- 54C05 Continuous maps
- 54C08 Weak and generalized continuity
- 54C10 Special maps on topological spaces (open, closed, perfect, etc.)
- 54C15 Retraction
- 54C20 Extension of maps
- 54C25 Embedding
- 54C30 Real-valued functions [See also 26-XX]
- 54C35 Function spaces [See also 46Exx, 58D15]
- 54C40 Algebraic properties of function spaces [See also 46J10]
- 54C45  $C$ - and  $C^*$ -embedding
- 54C50 Special sets defined by functions [See also 26A21]
- 54C55 Absolute neighborhood extensor, absolute extensor, absolute neighborhood retract (ANR), absolute retract spaces (general properties) [See also 55M15]
- 54C56 Shape theory [See also 55P55, 57N25]
- 54C60 Set-valued maps [See also 26E25, 28B20, 47H04, 58C06]
- 54C65 Selections [See also 28B20]
- 54C70 Entropy
- 54C99 None of the above, but in this section
- 54Dxx Fairly general properties**
- 54D05 Connected and locally connected spaces (general aspects)
- 54D10 Lower separation axioms ( $T_0$ - $T_3$ , etc.)
- 54D15 Higher separation axioms (completely regular, normal, perfectly or collectionwise normal, etc.)
- 54D20 Noncompact covering properties (paracompact, Lindelöf, etc.)
- 54D25 “ $P$ -minimal” and “ $P$ -closed” spaces
- 54D30 Compactness
- 54D35 Extensions of spaces (compactifications, supercompactifications, completions, etc.)
- 54D40 Remainders
- 54D45 Local compactness,  $\sigma$ -compactness
- 54D50  $k$ -spaces
- 54D55 Sequential spaces

- 54D60 Realcompactness and realcompactification
- 54D65 Separability
- 54D70 Base properties
- 54D80 Special constructions of spaces (spaces of ultrafilters, etc.)
- 54D99 None of the above, but in this section
- 54Exx Spaces with richer structures**
- 54E05 Proximity structures and generalizations
- 54E15 Uniform structures and generalizations
- 54E17 Nearness spaces
- 54E18  $p$ -spaces,  $M$ -spaces,  $\sigma$ -spaces, etc.
- 54E20 Stratifiable spaces, cosmic spaces, etc.
- 54E25 Semimetric spaces
- 54E30 Moore spaces
- 54E35 Metric spaces, metrizability
- 54E40 Special maps on metric spaces
- 54E45 Compact (locally compact) metric spaces
- 54E50 Complete metric spaces
- 54E52 Baire category, Baire spaces
- 54E55 Bitopologies
- 54E70 Probabilistic metric spaces
- 54E99 None of the above, but in this section
- 54Fxx Special properties**
- 54F05 Linearly ordered topological spaces, generalized ordered spaces, and partially ordered spaces [See also 06B30, 06F30]
- 54F15 Continua and generalizations
- 54F35 Higher-dimensional local connectedness [See also 55Mxx, 55Nxx]
- 54F45 Dimension theory [See also 55M10]
- 54F50 Spaces of dimension  $\leq 1$ ; curves, dendrites [See also 26A03]
- 54F55 Unicoherence, multicoherence
- 54F65 Topological characterizations of particular spaces
- 54F99 None of the above, but in this section
- 54Gxx Peculiar spaces**
- 54G05 Extremely disconnected spaces,  $F$ -spaces, etc.
- 54G10  $P$ -spaces
- 54G12 Scattered spaces
- 54G15 Pathological spaces
- 54G20 Counterexamples
- 54G99 None of the above, but in this section
- 54Hxx Connections with other structures, applications**
- 54H05 Descriptive set theory (topological aspects of Borel, analytic, projective, etc. sets) [See also 03E15, 26A21, 28A05]
- 54H10 Topological representations of algebraic systems [See also 22-XX]
- 54H11 Topological groups [See also 22A05]
- 54H12 Topological lattices, etc. [See also 06B30, 06F30]
- 54H13 Topological fields, rings, etc. [See also 12Jxx]  $\{\{\}\}$ For algebraic aspects, see 13Jxx, 16W80
- 54H15 Transformation groups and semigroups [See also 20M20, 22-XX, 57Sxx]
- 54H20 Topological dynamics [See also 28Dxx, 37Bxx]
- 54H25 Fixed-point and coincidence theorems [See also 47H10, 55M20]
- 54H99 None of the above, but in this section

- 54Jxx **Nonstandard topology** [See also 03H05]
- 54J05 Nonstandard topology [See also 03H05]
- 54J99 None of the above, but in this section
- 55–XX ALGEBRAIC TOPOLOGY**
- 55–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 55–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 55–02 Research exposition (monographs, survey articles)
- 55–03 Historical (must also be assigned at least one classification number from Section 01)
- 55–04 Explicit machine computation and programs (not the theory of computation or programming)
- 55–06 Proceedings, conferences, collections, etc.
- 55Mxx Classical topics {}{}For the topology of Euclidean spaces and manifolds, see 57Nxx**
- 55M05 Duality
- 55M10 Dimension theory [See also 54F45]
- 55M15 Absolute neighborhood retracts [See also 54C55]
- 55M20 Fixed points and coincidences [See also 54H25]
- 55M25 Degree, winding number
- 55M30 Ljusternik-Schnirelman (Lyusternik-Shnirel'man) category of a space
- 55M35 Finite groups of transformations (including Smith theory) [See also 57S17]
- 55M99 None of the above, but in this section
- 55Nxx Homology and cohomology theories** [See also 57Txx]
- 55N05 Čech types
- 55N07 Steenrod-Sitnikov homologies
- 55N10 Singular theory
- 55N15  $K$ -theory [See also 19Lxx] {}{}For algebraic  $K$ -theory, see 18F25, 19–XX
- 55N20 Generalized (extraordinary) homology and cohomology theories
- 55N22 Bordism and cobordism theories, formal group laws [See also 14L05, 19L41, 57R75, 57R77, 57R85, 57R90]
- 55N25 Homology with local coefficients, equivariant cohomology
- 55N30 Sheaf cohomology [See also 18F20, 32C35, 32L10]
- 55N32 Orbifold cohomology
- 55N33 Intersection homology and cohomology
- 55N34 Elliptic cohomology
- 55N35 Other homology theories
- 55N40 Axioms for homology theory and uniqueness theorems
- 55N45 Products and intersections
- 55N91 Equivariant homology and cohomology [See also 19L47]
- 55N99 None of the above, but in this section
- 55Pxx Homotopy theory {}{}For simple homotopy type, see 57Q10**
- 55P05 Homotopy extension properties, cofibrations
- 55P10 Homotopy equivalences
- 55P15 Classification of homotopy type
- 55P20 Eilenberg-Mac Lane spaces
- 55P25 Spanier-Whitehead duality
- 55P30 Eckmann-Hilton duality
- 55P35 Loop spaces

- 55P40 Suspensions
- 55P42 Stable homotopy theory, spectra
- 55P43 Spectra with additional structure ( $E_\infty$ ,  $A_\infty$ , ring spectra, etc.)
- 55P45  $H$ -spaces and duals
- 55P47 Infinite loop spaces
- 55P48 Loop space machines, operads [See also 18D50]
- 55P50 String topology
- 55P55 Shape theory [See also 54C56, 55Q07]
- 55P57 Proper homotopy theory
- 55P60 Localization and completion
- 55P62 Rational homotopy theory
- 55P65 Homotopy functors
- 55P91 Equivariant homotopy theory [See also 19L47]
- 55P92 Relations between equivariant and nonequivariant homotopy theory
- 55P99 None of the above, but in this section
- 55Qxx Homotopy groups**
- 55Q05 Homotopy groups, general; sets of homotopy classes
- 55Q07 Shape groups
- 55Q10 Stable homotopy groups
- 55Q15 Whitehead products and generalizations
- 55Q20 Homotopy groups of wedges, joins, and simple spaces
- 55Q25 Hopf invariants
- 55Q35 Operations in homotopy groups
- 55Q40 Homotopy groups of spheres
- 55Q45 Stable homotopy of spheres
- 55Q50  $J$ -morphism [See also 19L20]
- 55Q51  $v_n$ -periodicity
- 55Q52 Homotopy groups of special spaces
- 55Q55 Cohomotopy groups
- 55Q70 Homotopy groups of special types [See also 55N05, 55N07]
- 55Q91 Equivariant homotopy groups [See also 19L47]
- 55Q99 None of the above, but in this section
- 55Rxx Fiber spaces and bundles [See also 18F15, 32Lxx, 46M20, 57R20, 57R22, 57R25]**
- 55R05 Fiber spaces
- 55R10 Fiber bundles
- 55R12 Transfer
- 55R15 Classification
- 55R20 Spectral sequences and homology of fiber spaces [See also 55Txx]
- 55R25 Sphere bundles and vector bundles
- 55R35 Classifying spaces of groups and  $H$ -spaces
- 55R37 Maps between classifying spaces
- 55R40 Homology of classifying spaces, characteristic classes [See also 57Txx, 57R20]
- 55R45 Homology and homotopy of  $BO$  and  $BU$ ; Bott periodicity
- 55R50 Stable classes of vector space bundles,  $K$ -theory [See also 19Lxx]  
 {{{}}For algebraic  $K$ -theory, see 18F25, 19-XX
- 55R55 Fiberings with singularities
- 55R60 Microbundles and block bundles [See also 57N55, 57Q50]
- 55R65 Generalizations of fiber spaces and bundles
- 55R70 Fibrewise topology

- 55R80 Discriminantal varieties, configuration spaces
- 55R91 Equivariant fiber spaces and bundles [See also 19L47]
- 55R99 None of the above, but in this section
- 55Sxx Operations and obstructions**
- 55S05 Primary cohomology operations
- 55S10 Steenrod algebra
- 55S12 Dyer-Lashof operations
- 55S15 Symmetric products, cyclic products
- 55S20 Secondary and higher cohomology operations
- 55S25  $K$ -theory operations and generalized cohomology operations  
[See also 19D55, 19Lxx]
- 55S30 Massey products
- 55S35 Obstruction theory
- 55S36 Extension and compression of mappings
- 55S37 Classification of mappings
- 55S40 Sectioning fiber spaces and bundles
- 55S45 Postnikov systems,  $k$ -invariants
- 55S91 Equivariant operations and obstructions [See also 19L47]
- 55S99 None of the above, but in this section
- 55Txx Spectral sequences [See also 18G40, 55R20]**
- 55T05 General
- 55T10 Serre spectral sequences
- 55T15 Adams spectral sequences
- 55T20 Eilenberg-Moore spectral sequences [See also 57T35]
- 55T25 Generalized cohomology
- 55T99 None of the above, but in this section
- 55Uxx Applied homological algebra and category theory [See also 18Gxx]**
- 55U05 Abstract complexes
- 55U10 Simplicial sets and complexes
- 55U15 Chain complexes
- 55U20 Universal coefficient theorems, Bockstein operator
- 55U25 Homology of a product, Künneth formula
- 55U30 Duality
- 55U35 Abstract and axiomatic homotopy theory
- 55U40 Topological categories, foundations of homotopy theory
- 55U99 None of the above, but in this section
- 57-XX MANIFOLDS AND CELL COMPLEXES FOR COMPLEX  
MANIFOLDS, SEE 32QXX{}**
- 57-00 General reference works (handbooks, dictionaries, bibliographies,  
etc.)
- 57-01 Instructional exposition (textbooks, tutorial papers, etc.)
- 57-02 Research exposition (monographs, survey articles)
- 57-03 Historical (must also be assigned at least one classification number  
from Section 01)
- 57-04 Explicit machine computation and programs (not the theory of  
computation or programming)
- 57-06 Proceedings, conferences, collections, etc.
- 57Mxx Low-dimensional topology**
- 57M05 Fundamental group, presentations, free differential calculus
- 57M07 Topological methods in group theory
- 57M10 Covering spaces

- 57M12 Special coverings, e.g. branched
- 57M15 Relations with graph theory [See also 05Cxx]
- 57M20 Two-dimensional complexes
- 57M25 Knots and links in  $S^3$  For higher dimensions, see 57Q45
- 57M27 Invariants of knots and 3-manifolds
- 57M30 Wild knots and surfaces, etc., wild embeddings
- 57M35 Dehn's lemma, sphere theorem, loop theorem, asphericity
- 57M40 Characterizations of  $E^3$  and  $S^3$  (Poincaré conjecture)  
[See also 57N12]
- 57M50 Geometric structures on low-dimensional manifolds
- 57M60 Group actions in low dimensions
- 57M99 None of the above, but in this section
- 57Nxx Topological manifolds**
- 57N05 Topology of  $E^2$ , 2-manifolds
- 57N10 Topology of general 3-manifolds [See also 57Mxx]
- 57N12 Topology of  $E^3$  and  $S^3$  [See also 57M40]
- 57N13 Topology of  $E^4$ , 4-manifolds [See also 14Jxx, 32Jxx]
- 57N15 Topology of  $E^n$ ,  $n$ -manifolds ( $4 < n < \infty$ )
- 57N16 Geometric structures on manifolds [See also 57M50]
- 57N17 Topology of topological vector spaces
- 57N20 Topology of infinite-dimensional manifolds [See also 58Bxx]
- 57N25 Shapes [See also 54C56, 55P55, 55Q07]
- 57N30 Engulfing
- 57N35 Embeddings and immersions
- 57N37 Isotopy and pseudo-isotopy
- 57N40 Neighborhoods of submanifolds
- 57N45 Flatness and tameness
- 57N50  $S^{n-1} \subset E^n$ , Schoenflies problem
- 57N55 Microbundles and block bundles [See also 55R60, 57Q50]
- 57N60 Cellularity
- 57N65 Algebraic topology of manifolds
- 57N70 Cobordism and concordance
- 57N75 General position and transversality
- 57N80 Stratifications
- 57N99 None of the above, but in this section
- 57Pxx Generalized manifolds [See also 18F15]**
- 57P05 Local properties of generalized manifolds
- 57P10 Poincaré duality spaces
- 57P99 None of the above, but in this section
- 57Qxx PL-topology**
- 57Q05 General topology of complexes
- 57Q10 Simple homotopy type, Whitehead torsion, Reidemeister-Franz torsion, etc. [See also 19B28]
- 57Q12 Wall finiteness obstruction for CW-complexes
- 57Q15 Triangulating manifolds
- 57Q20 Cobordism
- 57Q25 Comparison of PL-structures: classification, Hauptvermutung
- 57Q30 Engulfing
- 57Q35 Embeddings and immersions
- 57Q37 Isotopy
- 57Q40 Regular neighborhoods

- 57Q45 Knots and links (in high dimensions) {}{}For the low-dimensional case, see 57M25
- 57Q50 Microbundles and block bundles [See also 55R60, 57N55]
- 57Q55 Approximations
- 57Q60 Cobordism and concordance
- 57Q65 General position and transversality
- 57Q91 Equivariant PL-topology
- 57Q99 None of the above, but in this section
- 57Rxx Differential topology {}{}For foundational questions of differentiable manifolds, see 58Axx; for infinite-dimensional manifolds, see 58Bxx**
- 57R05 Triangulating
- 57R10 Smoothing
- 57R12 Smooth approximations
- 57R15 Specialized structures on manifolds (spin manifolds, framed manifolds, etc.)
- 57R17 Symplectic and contact topology
- 57R18 Topology and geometry of orbifolds
- 57R19 Algebraic topology on manifolds
- 57R20 Characteristic classes and numbers
- 57R22 Topology of vector bundles and fiber bundles [See also 55Rxx]
- 57R25 Vector fields, frame fields
- 57R27 Controllability of vector fields on  $C^\infty$  and real-analytic manifolds [See also 49Qxx, 37C10, 93B05]
- 57R30 Foliations; geometric theory
- 57R32 Classifying spaces for foliations; Gelfand-Fuks cohomology [See also 58H10]
- 57R35 Differentiable mappings
- 57R40 Embeddings
- 57R42 Immersions
- 57R45 Singularities of differentiable mappings
- 57R50 Diffeomorphisms
- 57R52 Isotopy
- 57R55 Differentiable structures
- 57R56 Topological quantum field theories
- 57R57 Applications of global analysis to structures on manifolds, Donaldson and Seiberg-Witten invariants [See also 58-XX]
- 57R58 Floer homology
- 57R60 Homotopy spheres, Poincaré conjecture
- 57R65 Surgery and handlebodies
- 57R67 Surgery obstructions, Wall groups [See also 19J25]
- 57R70 Critical points and critical submanifolds
- 57R75 O- and SO-cobordism
- 57R77 Complex cobordism (U- and SU-cobordism) [See also 55N22]
- 57R80  $h$ - and  $s$ -cobordism
- 57R85 Equivariant cobordism
- 57R90 Other types of cobordism [See also 55N22]
- 57R91 Equivariant algebraic topology of manifolds
- 57R95 Realizing cycles by submanifolds
- 57R99 None of the above, but in this section

- 57Sxx **Topological transformation groups** [See also 20F34, 22–XX, 37–XX, 54H15, 58D05]
- 57S05 Topological properties of groups of homeomorphisms or diffeomorphisms
- 57S10 Compact groups of homeomorphisms
- 57S15 Compact Lie groups of differentiable transformations
- 57S17 Finite transformation groups
- 57S20 Noncompact Lie groups of transformations
- 57S25 Groups acting on specific manifolds
- 57S30 Discontinuous groups of transformations
- 57S99 None of the above, but in this section
- 57Txx **Homology and homotopy of topological groups and related structures**
- 57T05 Hopf algebras [See also 16T05]
- 57T10 Homology and cohomology of Lie groups
- 57T15 Homology and cohomology of homogeneous spaces of Lie groups
- 57T20 Homotopy groups of topological groups and homogeneous spaces
- 57T25 Homology and cohomology of  $H$ -spaces
- 57T30 Bar and cobar constructions [See also 18G55, 55Uxx]
- 57T35 Applications of Eilenberg-Moore spectral sequences [See also 55R20, 55T20]
- 57T99 None of the above, but in this section
- 58–XX **GLOBAL ANALYSIS, ANALYSIS ON MANIFOLDS FOR GEOMETRIC INTEGRATION THEORY, SEE 49Q15**[See also 32Cxx, 32Fxx, 32Wxx, 46–XX, 47Hxx, 53Cxx]{}
- 58–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 58–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 58–02 Research exposition (monographs, survey articles)
- 58–03 Historical (must also be assigned at least one classification number from Section 01)
- 58–04 Explicit machine computation and programs (not the theory of computation or programming)
- 58–06 Proceedings, conferences, collections, etc.
- 58Axx **General theory of differentiable manifolds** [See also 32Cxx]
- 58A03 Topos-theoretic approach to differentiable manifolds
- 58A05 Differentiable manifolds, foundations
- 58A07 Real-analytic and Nash manifolds [See also 14P20, 32C07]
- 58A10 Differential forms
- 58A12 de Rham theory [See also 14Fxx]
- 58A14 Hodge theory [See also 14C30, 14Fxx, 32J25, 32S35]
- 58A15 Exterior differential systems (Cartan theory)
- 58A17 Pfaffian systems
- 58A20 Jets
- 58A25 Currents [See also 32C30, 53C65]
- 58A30 Vector distributions (subbundles of the tangent bundles)
- 58A32 Natural bundles
- 58A35 Stratified sets [See also 32S60]
- 58A40 Differential spaces
- 58A50 Supermanifolds and graded manifolds [See also 14A22, 32C11]
- 58A99 None of the above, but in this section

- 58Bxx**     **Infinite-dimensional manifolds**
- 58B05     Homotopy and topological questions
- 58B10     Differentiability questions
- 58B12     Questions of holomorphy [See also 32–XX, 46G20]
- 58B15     Fredholm structures [See also 47A53]
- 58B20     Riemannian, Finsler and other geometric structures [See also 53C20, 53C60]
- 58B25     Group structures and generalizations on infinite-dimensional manifolds [See also 22E65, 58D05]
- 58B32     Geometry of quantum groups
- 58B34     Noncommutative geometry (à la Connes)
- 58B99     None of the above, but in this section
- 58Cxx**     **Calculus on manifolds; nonlinear operators** [See also 46Txx, 47Hxx, 47Jxx]
- 58C05     Real-valued functions
- 58C06     Set valued and function-space valued mappings [See also 47H04, 54C60]
- 58C07     Continuity properties of mappings
- 58C10     Holomorphic maps [See also 32–XX]
- 58C15     Implicit function theorems; global Newton methods
- 58C20     Differentiation theory (Gateaux, Fréchet, etc.) [See also 26Exx, 46G05]
- 58C25     Differentiable maps
- 58C30     Fixed point theorems on manifolds [See also 47H10]
- 58C35     Integration on manifolds; measures on manifolds [See also 28Cxx]
- 58C40     Spectral theory; eigenvalue problems [See also 47J10, 58E07]
- 58C50     Analysis on supermanifolds or graded manifolds
- 58C99     None of the above, but in this section
- 58Dxx**     **Spaces and manifolds of mappings (including nonlinear versions of 46Exx)** [See also 46Txx, 53Cxx]
- 58D05     Groups of diffeomorphisms and homeomorphisms as manifolds [See also 22E65, 57S05]
- 58D07     Groups and semigroups of nonlinear operators [See also 17B65, 47H20]
- 58D10     Spaces of imbeddings and immersions
- 58D15     Manifolds of mappings [See also 46T10, 54C35]
- 58D17     Manifolds of metrics (esp. Riemannian)
- 58D19     Group actions and symmetry properties
- 58D20     Measures (Gaussian, cylindrical, etc.) on manifolds of maps [See also 28Cxx, 46T12]
- 58D25     Equations in function spaces; evolution equations [See also 34Gxx, 35K90, 35L90, 35R15, 37Lxx, 47Jxx]
- 58D27     Moduli problems for differential geometric structures
- 58D29     Moduli problems for topological structures
- 58D30     Applications (in quantum mechanics (Feynman path integrals), relativity, fluid dynamics, etc.)
- 58D99     None of the above, but in this section
- 58Exx**     **Variational problems in infinite-dimensional spaces**
- 58E05     Abstract critical point theory (Morse theory, Ljusternik-Schnirelman (Lyusternik-Shnirel'man) theory, etc.)
- 58E07     Abstract bifurcation theory

- 58E09 Group-invariant bifurcation theory
- 58E10 Applications to the theory of geodesics (problems in one independent variable)
- 58E11 Critical metrics
- 58E12 Applications to minimal surfaces (problems in two independent variables) [See also 49Q05]
- 58E15 Application to extremal problems in several variables; Yang-Mills functionals [See also 81T13], etc.
- 58E17 Pareto optimality, etc., applications to economics [See also 90C29]
- 58E20 Harmonic maps [See also 53C43], etc.
- 58E25 Applications to control theory [See also 49-XX, 93-XX]
- 58E30 Variational principles
- 58E35 Variational inequalities (global problems)
- 58E40 Group actions
- 58E50 Applications
- 58E99 None of the above, but in this section
- 58Hxx Pseudogroups, differentiable groupoids and general structures on manifolds**
- 58H05 Pseudogroups and differentiable groupoids [See also 22A22, 22E65]
- 58H10 Cohomology of classifying spaces for pseudogroup structures (Spencer, Gelfand-Fuks, etc.) [See also 57R32]
- 58H15 Deformations of structures [See also 32Gxx, 58J10]
- 58H99 None of the above, but in this section
- 58Jxx Partial differential equations on manifolds; differential operators [See also 32Wxx, 35-XX, 53Cxx]**
- 58J05 Elliptic equations on manifolds, general theory [See also 35-XX]
- 58J10 Differential complexes [See also 35Nxx]; elliptic complexes
- 58J15 Relations with hyperfunctions
- 58J20 Index theory and related fixed point theorems [See also 19K56, 46L80]
- 58J22 Exotic index theories [See also 19K56, 46L05, 46L10, 46L80, 46M20]
- 58J26 Elliptic genera
- 58J28 Eta-invariants, Chern-Simons invariants
- 58J30 Spectral flows
- 58J32 Boundary value problems on manifolds
- 58J35 Heat and other parabolic equation methods
- 58J37 Perturbations; asymptotics
- 58J40 Pseudodifferential and Fourier integral operators on manifolds [See also 35Sxx]
- 58J42 Noncommutative global analysis, noncommutative residues
- 58J45 Hyperbolic equations [See also 35Lxx]
- 58J47 Propagation of singularities; initial value problems
- 58J50 Spectral problems; spectral geometry; scattering theory [See also 35Pxx]
- 58J51 Relations between spectral theory and ergodic theory, e.g. quantum unique ergodicity
- 58J52 Determinants and determinant bundles, analytic torsion
- 58J53 Isospectrality
- 58J55 Bifurcation [See also 35B32]
- 58J60 Relations with special manifold structures (Riemannian, Finsler, etc.)
- 58J65 Diffusion processes and stochastic analysis on manifolds [See also 35R60, 60H10, 60J60]

- 58J70 Invariance and symmetry properties [See also 35A30]
- 58J72 Correspondences and other transformation methods (e.g. Lie-Bäcklund) [See also 35A22]
- 58J90 Applications
- 58J99 None of the above, but in this section
- 58Kxx Theory of singularities and catastrophe theory [See also 32Sxx, 37–XX]**
- 58K05 Critical points of functions and mappings
- 58K10 Monodromy
- 58K15 Topological properties of mappings
- 58K20 Algebraic and analytic properties of mappings
- 58K25 Stability
- 58K30 Global theory
- 58K35 Catastrophe theory
- 58K40 Classification; finite determinacy of map germs
- 58K45 Singularities of vector fields, topological aspects
- 58K50 Normal forms
- 58K55 Asymptotic behavior
- 58K60 Deformation of singularities
- 58K65 Topological invariants
- 58K70 Symmetries, equivariance
- 58K99 None of the above, but in this section
- 58Zxx Applications to physics**
- 58Z05 Applications to physics
- 58Z99 None of the above, but in this section
- 60–XX PROBABILITY THEORY AND STOCHASTIC PROCESSES FOR ADDITIONAL APPLICATIONS, SEE 11KXX, 62–XX, 90–XX, 91–XX, 92–XX, 93–XX, 94–XX {}**
- 60–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 60–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 60–02 Research exposition (monographs, survey articles)
- 60–03 Historical (must also be assigned at least one classification number from Section 01)
- 60–04 Explicit machine computation and programs (not the theory of computation or programming)
- 60–06 Proceedings, conferences, collections, etc.
- 60–08 Computational methods (not classified at a more specific level) [See also 65C50]
- 60Axx Foundations of probability theory**
- 60A05 Axioms; other general questions
- 60A10 Probabilistic measure theory  $\{\{\}\}$ For ergodic theory, see 28Dxx and 60Fxx
- 60A86 Fuzzy probability
- 60A99 None of the above, but in this section
- 60Bxx Probability theory on algebraic and topological structures**
- 60B05 Probability measures on topological spaces
- 60B10 Convergence of probability measures
- 60B11 Probability theory on linear topological spaces [See also 28C20]
- 60B12 Limit theorems for vector-valued random variables (infinite-dimensional case)

- 60B15 Probability measures on groups or semigroups, Fourier transforms, factorization
- 60B20 Random matrices (probabilistic aspects; for algebraic aspects see 15B52)
- 60B99 None of the above, but in this section
- 60Cxx Combinatorial probability**
- 60C05 Combinatorial probability
- 60C99 None of the above, but in this section
- 60Dxx Geometric probability and stochastic geometry [See also 52A22, 53C65]**
- 60D05 Geometric probability and stochastic geometry [See also 52A22, 53C65]
- 60D99 None of the above, but in this section
- 60Exx Distribution theory [See also 62Exx, 62Hxx]**
- 60E05 Distributions: general theory
- 60E07 Infinitely divisible distributions; stable distributions
- 60E10 Characteristic functions; other transforms
- 60E15 Inequalities; stochastic orderings
- 60E99 None of the above, but in this section
- 60Fxx Limit theorems [See also 28Dxx, 60B12]**
- 60F05 Central limit and other weak theorems
- 60F10 Large deviations
- 60F15 Strong theorems
- 60F17 Functional limit theorems; invariance principles
- 60F20 Zero-one laws
- 60F25  $L^p$ -limit theorems
- 60F99 None of the above, but in this section
- 60Gxx Stochastic processes**
- 60G05 Foundations of stochastic processes
- 60G07 General theory of processes
- 60G09 Exchangeability
- 60G10 Stationary processes
- 60G12 General second-order processes
- 60G15 Gaussian processes
- 60G17 Sample path properties
- 60G18 Self-similar processes
- 60G20 Generalized stochastic processes
- 60G22 Fractional processes, including fractional Brownian motion
- 60G25 Prediction theory [See also 62M20]
- 60G30 Continuity and singularity of induced measures
- 60G35 Signal detection and filtering [See also 62M20, 93E10, 93E11, 94Axx]
- 60G40 Stopping times; optimal stopping problems; gambling theory [See also 62L15, 91A60]
- 60G42 Martingales with discrete parameter
- 60G44 Martingales with continuous parameter
- 60G46 Martingales and classical analysis
- 60G48 Generalizations of martingales
- 60G50 Sums of independent random variables; random walks
- 60G51 Processes with independent increments; Lévy processes
- 60G52 Stable processes
- 60G55 Point processes

- 60G57 Random measures
- 60G60 Random fields
- 60G70 Extreme value theory; extremal processes
- 60G99 None of the above, but in this section
- 60Hxx Stochastic analysis [See also 58J65]**
- 60H05 Stochastic integrals
- 60H07 Stochastic calculus of variations and the Malliavin calculus
- 60H10 Stochastic ordinary differential equations [See also 34F05]
- 60H15 Stochastic partial differential equations [See also 35R60]
- 60H20 Stochastic integral equations
- 60H25 Random operators and equations [See also 47B80]
- 60H30 Applications of stochastic analysis (to PDE, etc.)
- 60H35 Computational methods for stochastic equations [See also 65C30]
- 60H40 White noise theory
- 60H99 None of the above, but in this section
- 60Jxx Markov processes**
- 60J05 Discrete-time Markov processes on general state spaces
- 60J10 Markov chains (discrete-time Markov processes on discrete state spaces)
- 60J20 Applications of Markov chains and discrete-time Markov processes on general state spaces (social mobility, learning theory, industrial processes, etc.) [See also 90B30, 91D10, 91D35, 91E40]
- 60J22 Computational methods in Markov chains [See also 65C40]
- 60J25 Continuous-time Markov processes on general state spaces
- 60J27 Continuous-time Markov processes on discrete state spaces
- 60j28 Applications of continuous-time Markov processes on discrete state spaces
- 60J35 Transition functions, generators and resolvents [See also 47D03, 47D07]
- 60J40 Right processes
- 60J45 Probabilistic potential theory [See also 31Cxx, 31D05]
- 60J50 Boundary theory
- 60J55 Local time and additive functionals
- 60J57 Multiplicative functionals
- 60J60 Diffusion processes [See also 58J65]
- 60J65 Brownian motion [See also 58J65]
- 60J67 Stochastic (Schramm-)Loewner evolution (SLE)
- 60J68 Superprocesses
- 60J70 Applications of Brownian motions and diffusion theory (population genetics, absorption problems, etc.) [See also 92Dxx]
- 60J75 Jump processes
- 60J80 Branching processes (Galton-Watson, birth-and-death, etc.)
- 60J85 Applications of branching processes [See also 92Dxx]
- 60J99 None of the above, but in this section
- 60Kxx Special processes**
- 60K05 Renewal theory
- 60K10 Applications (reliability, demand theory, etc.)
- 60K15 Markov renewal processes, semi-Markov processes
- 60K20 Applications of Markov renewal processes (reliability, queueing networks, etc.) [See also 90Bxx]
- 60K25 Queueing theory [See also 68M20, 90B22]

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- 60K30 Applications (congestion, allocation, storage, traffic, etc.)  
[See also 90Bxx]
- 60K35 Interacting random processes; statistical mechanics type models;  
percolation theory [See also 82B43, 82C43]
- 60K37 Processes in random environments
- 60K40 Other physical applications of random processes
- 60K99 None of the above, but in this section
- 62-XX STATISTICS**
- 62-00 General reference works (handbooks, dictionaries, bibliographies,  
etc.)
- 62-01 Instructional exposition (textbooks, tutorial papers, etc.)
- 62-02 Research exposition (monographs, survey articles)
- 62-03 Historical (must also be assigned at least one classification number  
from Section 01)
- 62-04 Explicit machine computation and programs (not the theory of  
computation or programming)
- 62-06 Proceedings, conferences, collections, etc.
- 62-07 Data analysis
- 62-09 Graphical methods
- 62Axx Foundational and philosophical topics**
- 62A01 Foundations and philosophical topics
- 62A86 Fuzzy analysis in statistics
- 62A99 None of the above, but in this section
- 62Bxx Sufficiency and information**
- 62B05 Sufficient statistics and fields
- 62B10 Information-theoretic topics [See also 94A17]
- 62B15 Theory of statistical experiments
- 62B86 Fuzziness, sufficiency, and information
- 62B99 None of the above, but in this section
- 62Cxx Decision theory [See also 90B50, 91B06; for game theory, see 91A35]**
- 62C05 General considerations
- 62C07 Complete class results
- 62C10 Bayesian problems; characterization of Bayes procedures
- 62C12 Empirical decision procedures; empirical Bayes procedures
- 62C15 Admissibility
- 62C20 Minimax procedures
- 62C25 Compound decision problems
- 62C86 Decision theory and fuzziness
- 62C99 None of the above, but in this section
- 62Dxx Sampling theory, sample surveys**
- 62D05 Sampling theory, sample surveys
- 62D99 None of the above, but in this section
- 62Exx Distribution theory [See also 60Exx]**
- 62E10 Characterization and structure theory
- 62E15 Exact distribution theory
- 62E17 Approximations to distributions (nonasymptotic)
- 62E20 Asymptotic distribution theory
- 62E86 Fuzziness in connection with the topics on distributions in this  
section
- 62E99 None of the above, but in this section

<b>62Fxx</b>	<b>Parametric inference</b>
62F03	Hypothesis testing
62F05	Asymptotic properties of tests
62F07	Ranking and selection
62F10	Point estimation
62F12	Asymptotic properties of estimators
62F15	Bayesian inference
62F25	Tolerance and confidence regions
62F30	Inference under constraints
62F35	Robustness and adaptive procedures
62F40	Bootstrap, jackknife and other resampling methods
62F86	Parametric inference and fuzziness
62F99	None of the above, but in this section
<b>62Gxx</b>	<b>Nonparametric inference</b>
62G05	Estimation
62G07	Density estimation
62G08	Nonparametric regression
62G09	Resampling methods
62G10	Hypothesis testing
62G15	Tolerance and confidence regions
62G20	Asymptotic properties
62G30	Order statistics; empirical distribution functions
62G32	Statistics of extreme values; tail inference
62G35	Robustness
62G86	Nonparametric inference and fuzziness
62G99	None of the above, but in this section
<b>62Hxx</b>	<b>Multivariate analysis [See also 60Exx]</b>
62H05	Characterization and structure theory
62H10	Distribution of statistics
62H11	Directional data; spatial statistics
62H12	Estimation
62H15	Hypothesis testing
62H17	Contingency tables
62H20	Measures of association (correlation, canonical correlation, etc.)
62H25	Factor analysis and principal components; correspondence analysis
62H30	Classification and discrimination; cluster analysis [See also 68T10]
62H35	Image analysis
62H86	Multivariate analysis and fuzziness
62H99	None of the above, but in this section
<b>62Jxx</b>	<b>Linear inference, regression</b>
62J02	General nonlinear regression
62J05	Linear regression
62J07	Ridge regression; shrinkage estimators
62J10	Analysis of variance and covariance
62J12	Generalized linear models
62J15	Paired and multiple comparisons
62J20	Diagnostics
62J86	Fuzziness, and linear inference and regression
62J99	None of the above, but in this section

- 62Kxx**    **Design of experiments** [See also 05Bxx]
- 62K05    Optimal designs
- 62K10    Block designs
- 62K15    Factorial designs
- 62K20    Response surface designs
- 62K25    Robust parameter designs
- 62K86    Fuzziness and design of experiments
- 62K99    None of the above, but in this section
- 62Lxx**    **Sequential methods**
- 62L05    Sequential design
- 62L10    Sequential analysis
- 62L12    Sequential estimation
- 62L15    Optimal stopping [See also 60G40, 91A60]
- 62L20    Stochastic approximation
- 62L86    Fuzziness and sequential methods
- 62L99    None of the above, but in this section
- 62Mxx**    **Inference from stochastic processes**
- 62M02    Markov processes: hypothesis testing
- 62M05    Markov processes: estimation
- 62M07    Non-Markovian processes: hypothesis testing
- 62M09    Non-Markovian processes: estimation
- 62M10    Time series, auto-correlation, regression, etc. [See also 91B84]
- 62M15    Spectral analysis
- 62M20    Prediction [See also 60G25]; filtering [See also 60G35, 93E10, 93E11]
- 62M30    Spatial processes
- 62M40    Random fields; image analysis
- 62M45    Neural nets and related approaches
- 62M86    Inference from stochastic processes and fuzziness
- 62M99    None of the above, but in this section
- 62Nxx**    **Survival analysis and censored data**
- 62N01    Censored data models
- 62N02    Estimation
- 62N03    Testing
- 62N05    Reliability and life testing [See also 90B25]
- 62N86    Fuzziness, and survival analysis and censored data
- 62N99    None of the above, but in this section
- 62Pxx**    **Applications** [See also 90–XX, 91–XX, 92–XX]
- 62P05    Applications to actuarial sciences and financial mathematics
- 62P10    Applications to biology and medical sciences
- 62P12    Applications to environmental and related topics
- 62P15    Applications to psychology
- 62P20    Applications to economics [See also 91Bxx]
- 62P25    Applications to social sciences
- 62P30    Applications in engineering and industry
- 62P35    Applications to physics
- 62P99    None of the above, but in this section
- 62Qxx**    **Statistical tables**
- 62Q05    Statistical tables
- 62Q99    None of the above, but in this section

- 65–XX NUMERICAL ANALYSIS**
- 65–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
  - 65–01 Instructional exposition (textbooks, tutorial papers, etc.)
  - 65–02 Research exposition (monographs, survey articles)
  - 65–03 Historical (must also be assigned at least one classification number from Section 01)
  - 65–04 Explicit machine computation and programs (not the theory of computation or programming)
  - 65–05 Experimental papers
  - 65–06 Proceedings, conferences, collections, etc.
  - 65Axx Tables**
  - 65A05 Tables
  - 65A99 None of the above, but in this section
  - 65Bxx Acceleration of convergence**
  - 65B05 Extrapolation to the limit, deferred corrections
  - 65B10 Summation of series
  - 65B15 Euler-Maclaurin formula
  - 65B99 None of the above, but in this section
  - 65Cxx Probabilistic methods, simulation and stochastic differential equations** {{{}}For theoretical aspects, see 68U20 and 60H35
  - 65C05 Monte Carlo methods
  - 65C10 Random number generation
  - 65C20 Models, numerical methods [See also 68U20]
  - 65C30 Stochastic differential and integral equations
  - 65C35 Stochastic particle methods [See also 82C80]
  - 65C40 Computational Markov chains
  - 65C50 Other computational problems in probability
  - 65C60 Computational problems in statistics
  - 65C99 None of the above, but in this section
  - 65Dxx Numerical approximation and computational geometry (primarily algorithms)** {{{}}For theory, see 41–XX and 68Uxx
  - 65D05 Interpolation
  - 65D07 Splines
  - 65D10 Smoothing, curve fitting
  - 65D15 Algorithms for functional approximation
  - 65D17 Computer aided design (modeling of curves and surfaces) [See also 68U07]
  - 65D18 Computer graphics, image analysis, and computational geometry [See also 51N05, 68U05]
  - 65D19 Computational issues in computer and robotic vision
  - 65D20 Computation of special functions, construction of tables [See also 33F05]
  - 65D25 Numerical differentiation
  - 65D30 Numerical integration
  - 65D32 Quadrature and cubature formulas
  - 65D99 None of the above, but in this section
  - 65Exx Numerical methods in complex analysis (potential theory, etc.)** {{{}}For numerical methods in conformal mapping, see also 30C30
  - 65E05 Numerical methods in complex analysis (potential theory, etc.) {For numerical methods in conformal mapping, see \*also\* 30C30}
  - 65E99 None of the above, but in this section

- 65Fxx Numerical linear algebra**
- 65F05 Direct methods for linear systems and matrix inversion
- 65F08 Preconditioners for iterative methods
- 65F10 Iterative methods for linear systems [See also 65N22]
- 65F15 Eigenvalues, eigenvectors
- 65F18 Inverse eigenvalue problems
- 65F20 Overdetermined systems, pseudoinverses
- 65F22 Ill-posedness, regularization
- 65F25 Orthogonalization
- 65F30 Other matrix algorithms
- 65F35 Matrix norms, conditioning, scaling [See also 15A12, 15A60]
- 65F40 Determinants
- 65F50 Sparse matrices
- 65F60 Matrix exponential and similar matrix functions
- 65F99 None of the above, but in this section
- 65Gxx Error analysis and interval analysis**
- 65G20 Algorithms with automatic result verification
- 65G30 Interval and finite arithmetic
- 65G40 General methods in interval analysis
- 65G50 Roundoff error
- 65G99 None of the above, but in this section
- 65Hxx Nonlinear algebraic or transcendental equations**
- 65H04 Roots of polynomial equations
- 65H05 Single equations
- 65H10 Systems of equations
- 65H17 Eigenvalues, eigenvectors [See also 47Hxx, 47Jxx, 58C40, 58E07, 90C30]
- 65H20 Global methods, including homotopy approaches [See also 58C30, 90C30]
- 65H99 None of the above, but in this section
- 65Jxx Numerical analysis in abstract spaces**
- 65J05 General theory
- 65J08 Abstract evolution equations
- 65J10 Equations with linear operators (do not use 65Fxx)
- 65J15 Equations with nonlinear operators (do not use 65Hxx)
- 65J20 Improperly posed problems; regularization
- 65J22 Inverse problems
- 65J99 None of the above, but in this section
- 65Kxx Mathematical programming, optimization and variational techniques**
- 65K05 Mathematical programming methods [See also 90Cxx]
- 65K10 Optimization and variational techniques [See also 49Mxx, 93B40]
- 65K15 Numerical methods for variational inequalities and related problems
- 65K99 None of the above, but in this section
- 65Lxx Ordinary differential equations**
- 65L03 Functional-differential equations
- 65L04 Stiff equations
- 65L05 Initial value problems
- 65L06 Multistep, Runge-Kutta and extrapolation methods
- 65L07 Numerical investigation of stability of solutions
- 65L08 Improperly posed problems
- 65L09 Inverse problems

- 65L10 Boundary value problems
- 65L11 Singularly perturbed problems
- 65L12 Finite difference methods
- 65L15 Eigenvalue problems
- 65L20 Stability and convergence of numerical methods
- 65L50 Mesh generation and refinement
- 65L60 Finite elements, Rayleigh-Ritz, Galerkin and collocation methods
- 65L70 Error bounds
- 65L80 Methods for differential-algebraic equations
- 65L99 None of the above, but in this section
- 65Mxx Partial differential equations, initial value and time-dependent initial-boundary value problems**
- 65M06 Finite difference methods
- 65M08 Finite volume methods
- 65M12 Stability and convergence of numerical methods
- 65M15 Error bounds
- 65M20 Method of lines
- 65M22 Solution of discretized equations [See also 65Fxx, 65Hxx]
- 65M25 Method of characteristics
- 65M30 Improperly posed problems
- 65M32 Inverse problems
- 65M38 Boundary element methods
- 65M50 Mesh generation and refinement
- 65M55 Multigrid methods; domain decomposition
- 65M60 Finite elements, Rayleigh-Ritz and Galerkin methods, finite methods
- 65M70 Spectral, collocation and related methods
- 65M75 Probabilistic methods, particle methods, etc.
- 65M80 Fundamental solutions, Green's function methods, etc.
- 65M85 Fictitious domain methods
- 65M99 None of the above, but in this section
- 65Nxx Partial differential equations, boundary value problems**
- 65N06 Finite difference methods
- 65N08 Finite volume methods
- 65N12 Stability and convergence of numerical methods
- 65N15 Error bounds
- 65N20 Ill-posed problems
- 65N21 Inverse problems
- 65N22 Solution of discretized equations [See also 65Fxx, 65Hxx]
- 65N25 Eigenvalue problems
- 65N30 Finite elements, Rayleigh-Ritz and Galerkin methods, finite methods
- 65N35 Spectral, collocation and related methods
- 65N38 Boundary element methods
- 65N40 Method of lines
- 65N45 Method of contraction of the boundary
- 65N50 Mesh generation and refinement
- 65N55 Multigrid methods; domain decomposition
- 65N75 Probabilistic methods, particle methods, etc.
- 65N80 Fundamental solutions, Green's function methods, etc.
- 65N85 Fictitious domain methods
- 65N99 None of the above, but in this section

- 65Pxx Numerical problems in dynamical systems [See also 37Mxx]**
- 65P10 Hamiltonian systems including symplectic integrators
- 65P20 Numerical chaos
- 65P30 Bifurcation problems
- 65P40 Nonlinear stabilities
- 65P99 None of the above, but in this section
- 65Qxx Difference and functional equations, recurrence relations**
- 65Q05 Numerical methods in complex analysis (potential theory, etc.)
- 65Q99 None of the above, but in this section
- 65Rxx Integral equations, integral transforms**
- 65R10 Integral transforms
- 65R20 Integral equations
- 65R30 Improperly posed problems
- 65R32 Inverse problems
- 65R99 None of the above, but in this section
- 65Sxx Graphical methods**
- 65S05 Graphical methods
- 65S99 None of the above, but in this section
- 65Txx Numerical methods in Fourier analysis**
- 65T40 Trigonometric approximation and interpolation
- 65T50 Discrete and fast Fourier transforms
- 65T60 Wavelets
- 65T99 None of the above, but in this section
- 65Yxx Computer aspects of numerical algorithms**
- 65Y04 Algorithms for computer arithmetic, etc. [See also 68M07]
- 65Y05 Parallel computation
- 65Y10 Algorithms for specific classes of architectures
- 65Y15 Packaged methods
- 65Y20 Complexity and performance of numerical algorithms  
[See also 68Q25]
- 65Y99 None of the above, but in this section
- 65Zxx Applications to physics**
- 65Z05 Applications to physics
- 65Z99 None of the above, but in this section
- 68–XX COMPUTER SCIENCE FOR PAPERS INVOLVING MACHINE  
COMPUTATIONS AND PROGRAMS IN A SPECIFIC  
MATHEMATICAL AREA, SEE SECTION –04 IN THAT AREA { }**
- 68–00 General reference works (handbooks, dictionaries, bibliographies,  
etc.)
- 68–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 68–02 Research exposition (monographs, survey articles)
- 68–03 Historical (must also be assigned at least one classification number  
from Section 01)
- 68–04 Explicit machine computation and programs (not the theory of  
computation or programming)
- 68–06 Proceedings, conferences, collections, etc.
- 68Mxx Computer system organization**
- 68M01 General
- 68M07 Mathematical problems of computer architecture
- 68M10 Network design and communication [See also 68R10, 90B18]
- 68M11 Internet topics [See also 68U35]

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- 68M12 Network protocols
- 68M14 Distributed systems
- 68M15 Reliability, testing and fault tolerance [See also 94C12]
- 68M20 Performance evaluation; queueing; scheduling [See also 60K25, 90Bxx]
- 68M99 None of the above, but in this section
- 68Nxx Software**
- 68N01 General
- 68N15 Programming languages
- 68N17 Logic programming
- 68N18 Functional programming and lambda calculus [See also 03B40]
- 68N19 Other programming techniques (object-oriented, sequential, concurrent, automatic, etc.)
- 68N20 Compilers and interpreters
- 68N25 Operating systems
- 68N30 Mathematical aspects of software engineering (specification, verification, metrics, requirements, etc.)
- 68N99 None of the above, but in this section
- 68Pxx Theory of data**
- 68P01 General
- 68P05 Data structures
- 68P10 Searching and sorting
- 68P15 Database theory
- 68P20 Information storage and retrieval
- 68P25 Data encryption [See also 94A60, 81P94]
- 68P30 Coding and information theory (compaction, compression, models of communication, encoding schemes, etc.) [See also 94Axx]
- 68P99 None of the above, but in this section
- 68Qxx Theory of computing**
- 68Q01 General
- 68Q05 Models of computation (Turing machines, etc.) [See also 03D10, 68Q12, 81P68]
- 68Q10 Modes of computation (nondeterministic, parallel, interactive, probabilistic, etc.) [See also 68Q85]
- 68Q12 Quantum algorithms and complexity [See also 68Q05, 81P68]
- 68Q15 Complexity classes (hierarchies, relations among complexity classes, etc.) [See also 03D15, 68Q17, 68Q19]
- 68Q17 Computational difficulty of problems (lower bounds, completeness, difficulty of approximation, etc.) [See also 68Q15]
- 68Q19 Descriptive complexity and finite models [See also 03C13]
- 68Q25 Analysis of algorithms and problem complexity [See also 68W40]
- 68Q30 Algorithmic information theory (Kolmogorov complexity, etc.) [See also 03D32]
- 68Q32 Computational learning theory [See also 68T05]
- 68Q42 Grammars and rewriting systems
- 68Q45 Formal languages and automata [See also 03D05, 68Q70, 94A45]
- 68Q55 Semantics [See also 03B70, 06B35, 18C50]
- 68Q60 Specification and verification (program logics, model checking, etc.) [See also 03B70]
- 68Q65 Abstract data types; algebraic specification [See also 18C50]
- 68Q70 Algebraic theory of languages and automata [See also 18B20, 20M35]

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- 68Q80 Cellular automata [See also 37B15]
- 68Q85 Models and methods for concurrent and distributed computing (process algebras, bisimulation, transition nets, etc.)
- 68Q87 Probability in computer science (algorithm analysis, random structures, phase transitions, etc.) [See also 68W20, 68W40]
- 68Q99 None of the above, but in this section
- 68Rxx Discrete mathematics in relation to computer science**
- 68R01 General
- 68R05 Combinatorics
- 68R10 Graph theory (including graph drawing) [See also 05Cxx, 90B10, 90B35, 90C35]
- 68R15 Combinatorics on words
- 68R99 None of the above, but in this section
- 68Txx Artificial intelligence**
- 68T01 General
- 68T05 Learning and adaptive systems [See also 68Q32, 91E40]
- 68T10 Pattern recognition, speech recognition  $\{\{\}$ For cluster analysis, see 62H30
- 68T15 Theorem proving (deduction, resolution, etc.) [See also 03B35]
- 68T20 Problem solving (heuristics, search strategies, etc.)
- 68T27 Logic in artificial intelligence
- 68T30 Knowledge representation
- 68T35 Languages and software systems (knowledge-based systems, expert systems, etc.)
- 68T37 Reasoning under uncertainty
- 68T40 Robotics [See also 93C85]
- 68T42 Agent technology
- 68T45 Machine vision and scene understanding
- 68T50 Natural language processing [See also 03B65]
- 68T99 None of the above, but in this section
- 68Uxx Computing methodologies and applications**
- 68U01 General
- 68U05 Computer graphics; computational geometry [See also 65D18]
- 68U07 Computer-aided design [See also 65D17]
- 68U10 Image processing
- 68U15 Text processing; mathematical typography
- 68U20 Simulation [See also 65Cxx]
- 68U35 Information systems (hypertext navigation, interfaces, decision support, etc.) [See also 68M11]
- 68U99 None of the above, but in this section
- 68Wxx Algorithms  $\{\{\}$ For numerical algorithms, see 65–XX; for combinatorics and graph theory, see 05C85, 68Rxx**
- 68W01 General
- 68W05 Nonnumerical algorithms
- 68W10 Parallel algorithms
- 68W15 Distributed algorithms
- 68W20 Randomized algorithms
- 68W25 Approximation algorithms
- 68W27 Online algorithms
- 68W30 Symbolic computation and algebraic computation [See also 11Yxx, 12Y05, 13Pxx, 14Qxx, 16Z05, 17–08, 33F10]

- 68W32 Algorithms on strings
- 68W35 VLSI algorithms
- 68W40 Analysis of algorithms [See also 68Q25]
- 68W99 None of the above, but in this section
- 70–XX MECHANICS OF PARTICLES AND SYSTEMS FOR RELATIVISTIC MECHANICS, SEE 83A05 AND 83C10; FOR STATISTICAL MECHANICS, SEE 82–XX{}**
- 70–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 70–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 70–02 Research exposition (monographs, survey articles)
- 70–03 Historical (must also be assigned at least one classification number from Section 01)
- 70–04 Explicit machine computation and programs (not the theory of computation or programming)
- 70–05 Experimental work
- 70–06 Proceedings, conferences, collections, etc.
- 70–08 Computational methods
- 70Axx Axiomatics, foundations**
- 70A05 Axiomatics, foundations
- 70A99 None of the above, but in this section
- 70Bxx Kinematics [See also 53A17]**
- 70B05 Kinematics of a particle
- 70B10 Kinematics of a rigid body
- 70B15 Mechanisms, robots [See also 68T40, 70Q05, 93C85]
- 70B99 None of the above, but in this section
- 70Cxx Statics**
- 70C20 Statics
- 70C99 None of the above, but in this section
- 70Exx Dynamics of a rigid body and of multibody systems**
- 70E05 Motion of the gyroscope
- 70E15 Free motion of a rigid body [See also 70M20]
- 70E17 Motion of a rigid body with a fixed point
- 70E18 Motion of a rigid body in contact with a solid surface [See also 70F25]
- 70E20 Perturbation methods for rigid body dynamics
- 70E40 Integrable cases of motion
- 70E45 Higher-dimensional generalizations
- 70E50 Stability problems
- 70E55 Dynamics of multibody systems
- 70E60 Robot dynamics and control [See also 68T40, 70Q05, 93C85]
- 70E99 None of the above, but in this section
- 70Fxx Dynamics of a system of particles, including celestial mechanics**
- 70F05 Two-body problems
- 70F07 Three-body problems
- 70F10  $n$ -body problems
- 70F15 Celestial mechanics
- 70F16 Collisions in celestial mechanics, regularization
- 70F17 Inverse problems
- 70F20 Holonomic systems
- 70F25 Nonholonomic systems

- 70F35 Collision of rigid or pseudo-rigid bodies
- 70F40 Problems with friction
- 70F45 Infinite particle systems
- 70F99 None of the above, but in this section
- 70Gxx General models, approaches, and methods [See also 37–XX]**
- 70G10 Generalized coordinates; event, impulse-energy, configuration, state, or phase space
- 70G40 Topological and differential-topological methods
- 70G45 Differential-geometric methods (tensors, connections, symplectic, Poisson, contact, Riemannian, nonholonomic, etc.) [See also 53Cxx, 53Dxx, 58Axx]
- 70G55 Algebraic geometry methods
- 70G60 Dynamical systems methods
- 70G65 Symmetries, Lie-group and Lie-algebra methods
- 70G70 Functional-analytic methods
- 70G75 Variational methods
- 70G99 None of the above, but in this section
- 70Hxx Hamiltonian and Lagrangian mechanics [See also 37Jxx]**
- 70H03 Lagrange’s equations
- 70H05 Hamilton’s equations
- 70H06 Completely integrable systems and methods of integration
- 70H07 Nonintegrable systems
- 70H08 Nearly integrable Hamiltonian systems, KAM theory
- 70H09 Perturbation theories
- 70H11 Adiabatic invariants
- 70H12 Periodic and almost periodic solutions
- 70H14 Stability problems
- 70H15 Canonical and symplectic transformations
- 70H20 Hamilton-Jacobi equations
- 70H25 Hamilton’s principle
- 70H30 Other variational principles
- 70H33 Symmetries and conservation laws, reverse symmetries, invariant manifolds and their bifurcations, reduction
- 70H40 Relativistic dynamics
- 70H45 Constrained dynamics, Dirac’s theory of constraints [See also 70F20, 70F25, 70Gxx]
- 70H50 Higher-order theories
- 70H99 None of the above, but in this section
- 70Jxx Linear vibration theory**
- 70J10 Modal analysis
- 70J25 Stability
- 70J30 Free motions
- 70J35 Forced motions
- 70J40 Parametric resonances
- 70J50 Systems arising from the discretization of structural vibration problems
- 70J99 None of the above, but in this section
- 70Kxx Nonlinear dynamics [See also 34Cxx, 37–XX]**
- 70K05 Phase plane analysis, limit cycles
- 70K20 Stability
- 70K25 Free motions

- 70K28 Parametric resonances
- 70K30 Nonlinear resonances
- 70K40 Forced motions
- 70K42 Equilibria and periodic trajectories
- 70K43 Quasi-periodic motions and invariant tori
- 70K44 Homoclinic and heteroclinic trajectories
- 70K45 Normal forms
- 70K50 Bifurcations and instability
- 70K55 Transition to stochasticity (chaotic behavior) [See also 37D45]
- 70K60 General perturbation schemes
- 70K65 Averaging of perturbations
- 70K70 Systems with slow and fast motions
- 70K75 Nonlinear modes
- 70K99 None of the above, but in this section
- 70Lxx Random vibrations [See also 74H50]**
- 70L05 Random vibrations [See also 74H50]
- 70L99 None of the above, but in this section
- 70Mxx Orbital mechanics**
- 70M20 Orbital mechanics
- 70M99 None of the above, but in this section
- 70Pxx Variable mass, rockets**
- 70P05 Variable mass, rockets
- 70P99 None of the above, but in this section
- 70Qxx Control of mechanical systems [See also 60Gxx, 60Jxx]**
- 70Q05 Control of mechanical systems [See also 60Gxx, 60Jxx]
- 70Q99 None of the above, but in this section
- 70Sxx Classical field theories [See also 37Kxx, 37Lxx, 78–XX, 81Txx, 83–XX]**
- 70S05 Lagrangian formalism and Hamiltonian formalism
- 70S10 Symmetries and conservation laws
- 70S15 Yang-Mills and other gauge theories
- 70S20 More general nonquantum field theories
- 70S99 None of the above, but in this section
- 74–XX MECHANICS OF DEFORMABLE SOLIDS**
- 74–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 74–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 74–02 Research exposition (monographs, survey articles)
- 74–03 Historical (must also be assigned at least one classification number from Section 01)
- 74–04 Explicit machine computation and programs (not the theory of computation or programming)
- 74–05 Experimental work
- 74–06 Proceedings, conferences, collections, etc.
- 74Axx Generalities, axiomatics, foundations of continuum mechanics of solids**
- 74A05 Kinematics of deformation
- 74A10 Stress
- 74A15 Thermodynamics
- 74A20 Theory of constitutive functions
- 74A25 Molecular, statistical, and kinetic theories

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- 74A30 Nonsimple materials
- 74A35 Polar materials
- 74A40 Random materials and composite materials
- 74A45 Theories of fracture and damage
- 74A50 Structured surfaces and interfaces, coexistent phases
- 74A55 Theories of friction (tribology)
- 74A60 Micromechanical theories
- 74A65 Reactive materials
- 74A99 None of the above, but in this section
- 74Bxx Elastic materials**
- 74B05 Classical linear elasticity
- 74B10 Linear elasticity with initial stresses
- 74B15 Equations linearized about a deformed state (small deformations superposed on large)
- 74B20 Nonlinear elasticity
- 74B99 None of the above, but in this section
- 74Cxx Plastic materials, materials of stress-rate and internal-variable type**
- 74C05 Small-strain, rate-independent theories (including rigid-plastic and elasto-plastic materials)
- 74C10 Small-strain, rate-dependent theories (including theories of viscoplasticity)
- 74C15 Large-strain, rate-independent theories (including nonlinear plasticity)
- 74C20 Large-strain, rate-dependent theories
- 74C99 None of the above, but in this section
- 74Dxx Materials of strain-rate type and history type, other materials with memory (including elastic materials with viscous damping, various viscoelastic materials)**
- 74D05 Linear constitutive equations
- 74D10 Nonlinear constitutive equations
- 74D99 None of the above, but in this section
- 74Exx Material properties given special treatment**
- 74E05 Inhomogeneity
- 74E10 Anisotropy
- 74E15 Crystalline structure
- 74E20 Granularity
- 74E25 Texture
- 74E30 Composite and mixture properties
- 74E35 Random structure
- 74E40 Chemical structure
- 74E99 None of the above, but in this section
- 74Fxx Coupling of solid mechanics with other effects**
- 74F05 Thermal effects
- 74F10 Fluid-solid interactions (including aero- and hydro-elasticity, porosity, etc.)
- 74F15 Electromagnetic effects
- 74F20 Mixture effects
- 74F25 Chemical and reactive effects
- 74F99 None of the above, but in this section
- 74Gxx Equilibrium (steady-state) problems**
- 74G05 Explicit solutions

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- 74G10 Analytic approximation of solutions (perturbation methods, asymptotic methods, series, etc.)
- 74G15 Numerical approximation of solutions
- 74G20 Local existence of solutions (near a given solution)
- 74G25 Global existence of solutions
- 74G30 Uniqueness of solutions
- 74G35 Multiplicity of solutions
- 74G40 Regularity of solutions
- 74G45 Bounds for solutions
- 74G50 Saint-Venant's principle
- 74G55 Qualitative behavior of solutions
- 74G60 Bifurcation and buckling
- 74G65 Energy minimization
- 74G70 Stress concentrations, singularities
- 74G75 Inverse problems
- 74G99 None of the above, but in this section
- 74Hxx Dynamical problems**
- 74H05 Explicit solutions
- 74H10 Analytic approximation of solutions (perturbation methods, asymptotic methods, series, etc.)
- 74H15 Numerical approximation of solutions
- 74H20 Existence of solutions
- 74H25 Uniqueness of solutions
- 74H30 Regularity of solutions
- 74H35 Singularities, blowup, stress concentrations
- 74H40 Long-time behavior of solutions
- 74H45 Vibrations
- 74H50 Random vibrations
- 74H55 Stability
- 74H60 Dynamical bifurcation
- 74H65 Chaotic behavior
- 74H99 None of the above, but in this section
- 74Jxx Waves**
- 74J05 Linear waves
- 74J10 Bulk waves
- 74J15 Surface waves
- 74J20 Wave scattering
- 74J25 Inverse problems
- 74J30 Nonlinear waves
- 74J35 Solitary waves
- 74J40 Shocks and related discontinuities
- 74J99 None of the above, but in this section
- 74Kxx Thin bodies, structures**
- 74K05 Strings
- 74K10 Rods (beams, columns, shafts, arches, rings, etc.)
- 74K15 Membranes
- 74K20 Plates
- 74K25 Shells
- 74K30 Junctions
- 74K35 Thin films
- 74K99 None of the above, but in this section

- 74Lxx Special subfields of solid mechanics**
- 74L05 Geophysical solid mechanics [See also 86–XX]
- 74L10 Soil and rock mechanics
- 74L15 Biomechanical solid mechanics [See also 92C10]
- 74L99 None of the above, but in this section
- 74Mxx Special kinds of problems**
- 74M05 Control, switches and devices (“smart materials”) [See also 93Cxx]
- 74M10 Friction
- 74M15 Contact
- 74M20 Impact
- 74M25 Micromechanics
- 74M99 None of the above, but in this section
- 74Nxx Phase transformations in solids [See also 74A50, 80Axx, 82B26, 82C26]**
- 74N05 Crystals
- 74N10 Displacive transformations
- 74N15 Analysis of microstructure
- 74N20 Dynamics of phase boundaries
- 74N25 Transformations involving diffusion
- 74N30 Problems involving hysteresis
- 74N99 None of the above, but in this section
- 74Pxx Optimization [See also 49Qxx]**
- 74P05 Compliance or weight optimization
- 74P10 Optimization of other properties
- 74P15 Topological methods
- 74P20 Geometrical methods
- 74P99 None of the above, but in this section
- 74Qxx Homogenization, determination of effective properties**
- 74Q05 Homogenization in equilibrium problems
- 74Q10 Homogenization and oscillations in dynamical problems
- 74Q15 Effective constitutive equations
- 74Q20 Bounds on effective properties
- 74Q99 None of the above, but in this section
- 74Rxx Fracture and damage**
- 74R05 Brittle damage
- 74R10 Brittle fracture
- 74R15 High-velocity fracture
- 74R20 Anelastic fracture and damage
- 74R99 None of the above, but in this section
- 74Sxx Numerical methods [See also 65–XX, 74G15, 74H15]**
- 74S05 Finite element methods
- 74S10 Finite volume methods
- 74S15 Boundary element methods
- 74S20 Finite difference methods
- 74S25 Spectral and related methods
- 74S30 Other numerical methods
- 74S60 Stochastic methods
- 74S70 Complex variable methods
- 74S99 None of the above, but in this section

- 76–XX FLUID MECHANICS FOR GENERAL CONTINUUM MECHANICS, SEE 74AXX, OR OTHER PARTS OF 74–XX{}**
- 76–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
  - 76–01 Instructional exposition (textbooks, tutorial papers, etc.)
  - 76–02 Research exposition (monographs, survey articles)
  - 76–03 Historical (must also be assigned at least one classification number from Section 01)
  - 76–04 Explicit machine computation and programs (not the theory of computation or programming)
  - 76–05 Experimental work
  - 76–06 Proceedings, conferences, collections, etc.
  - 76Axx Foundations, constitutive equations, rheology**
  - 76A02 Foundations of fluid mechanics
  - 76A05 Non-Newtonian fluids
  - 76A10 Viscoelastic fluids
  - 76A15 Liquid crystals [See also 82D30]
  - 76A20 Thin fluid films
  - 76A25 Superfluids (classical aspects)
  - 76A99 None of the above, but in this section
  - 76Bxx Incompressible inviscid fluids**
  - 76B03 Existence, uniqueness, and regularity theory [See also 35Q35]
  - 76B07 Free-surface potential flows
  - 76B10 Jets and cavities, cavitation, free-streamline theory, water-entry problems, airfoil and hydrofoil theory, sloshing
  - 76B15 Water waves, gravity waves; dispersion and scattering, nonlinear interaction [See also 35Q30]
  - 76B20 Ship waves
  - 76B25 Solitary waves [See also 35C11]
  - 76B45 Capillarity (surface tension) [See also 76D45]
  - 76B47 Vortex flows
  - 76B55 Internal waves
  - 76B60 Atmospheric waves [See also 86A10]
  - 76B65 Rossby waves [See also 86A05, 86A10]
  - 76B70 Stratification effects in inviscid fluids
  - 76B75 Flow control and optimization [See also 49Q10, 93C20, 93C95]
  - 76B99 None of the above, but in this section
  - 76Dxx Incompressible viscous fluids**
  - 76D03 Existence, uniqueness, and regularity theory [See also 35Q30]
  - 76D05 Navier-Stokes equations [See also 35Q30]
  - 76D06 Statistical solutions of Navier-Stokes and related equations [See also 60H30, 76M35]
  - 76D07 Stokes and related (Oseen, etc.) flows
  - 76D08 Lubrication theory
  - 76D09 Viscous-inviscid interaction
  - 76D10 Boundary-layer theory, separation and reattachment, higher-order effects
  - 76D17 Viscous vortex flows
  - 76D25 Wakes and jets
  - 76D27 Other free-boundary flows; Hele-Shaw flows
  - 76D33 Waves

- 76D45 Capillarity (surface tension) [See also 76B45]
- 76D50 Stratification effects in viscous fluids
- 76D55 Flow control and optimization [See also 49Q10, 93C20, 93C95]
- 76D99 None of the above, but in this section
- 76Exx Hydrodynamic stability**
- 76E05 Parallel shear flows
- 76E06 Convection
- 76E07 Rotation
- 76E09 Stability and instability of nonparallel flows
- 76E15 Absolute and convective instability and stability
- 76E17 Interfacial stability and instability
- 76E19 Compressibility effects
- 76E20 Stability and instability of geophysical and astrophysical flows
- 76E25 Stability and instability of magnetohydrodynamic and electrohydrodynamic flows
- 76E30 Nonlinear effects
- 76E99 None of the above, but in this section
- 76Fxx Turbulence [See also 37–XX, 60Gxx, 60Jxx]**
- 76F02 Fundamentals
- 76F05 Isotropic turbulence; homogeneous turbulence
- 76F06 Transition to turbulence
- 76F10 Shear flows
- 76F20 Dynamical systems approach to turbulence [See also 37–XX]
- 76F25 Turbulent transport, mixing
- 76F30 Renormalization and other field-theoretical methods [See also 81T99]
- 76F35 Convective turbulence [See also 76E15, 76Rxx]
- 76F40 Turbulent boundary layers
- 76F45 Stratification effects
- 76F50 Compressibility effects
- 76F55 Statistical turbulence modeling [See also 76M35]
- 76F60  $k$ - $\varepsilon$  modeling
- 76F65 Direct numerical and large eddy simulation of turbulence
- 76F70 Control of turbulent flows
- 76F99 None of the above, but in this section
- 76Gxx General aerodynamics and subsonic flows**
- 76G25 General aerodynamics and subsonic flows
- 76G99 None of the above, but in this section
- 76Hxx Transonic flows**
- 76H05 Transonic flows
- 76H99 None of the above, but in this section
- 76Jxx Supersonic flows**
- 76J20 Supersonic flows
- 76J99 None of the above, but in this section
- 76Kxx Hypersonic flows**
- 76K05 Hypersonic flows
- 76K99 None of the above, but in this section
- 76Lxx Shock waves and blast waves [See also 35L67]**
- 76L05 Shock waves and blast waves [See also 35L67]
- 76L99 None of the above, but in this section

- 76Mxx Basic methods in fluid mechanics [See also 65–XX]**
- 76M10 Finite element methods
- 76M12 Finite volume methods
- 76M15 Boundary element methods
- 76M20 Finite difference methods
- 76M22 Spectral methods
- 76M23 Vortex methods
- 76M25 Other numerical methods
- 76M27 Visualization algorithms
- 76M28 Particle methods and lattice-gas methods
- 76M30 Variational methods
- 76M35 Stochastic analysis
- 76M40 Complex-variables methods
- 76M45 Asymptotic methods, singular perturbations
- 76M50 Homogenization
- 76M55 Dimensional analysis and similarity
- 76M60 Symmetry analysis, Lie group and algebra methods
- 76M99 None of the above, but in this section
- 76Nxx Compressible fluids and gas dynamics, general**
- 76N10 Existence, uniqueness, and regularity theory [See also 35L60, 35L65, 35Q30]
- 76N15 Gas dynamics, general
- 76N17 Viscous-inviscid interaction
- 76N20 Boundary-layer theory
- 76N25 Flow control and optimization
- 76N99 None of the above, but in this section
- 76Pxx Rarefied gas flows, Boltzmann equation [See also 82B40, 82C40, 82D05]**
- 76P05 Rarefied gas flows, Boltzmann equation [See also 82B40, 82C40, 82D05]
- 76P99 None of the above, but in this section
- 76Qxx Hydro- and aero-acoustics**
- 76Q05 Hydro- and aero-acoustics
- 76Q99 None of the above, but in this section
- 76Rxx Diffusion and convection**
- 76R05 Forced convection
- 76R10 Free convection
- 76R50 Diffusion [See also 60J60]
- 76R99 None of the above, but in this section
- 76Sxx Flows in porous media; filtration; seepage**
- 76S05 Flows in porous media; filtration; seepage
- 76S99 None of the above, but in this section
- 76Txx Two-phase and multiphase flows**
- 76T10 Liquid-gas two-phase flows, bubbly flows
- 76T15 Dusty-gas two-phase flows
- 76T20 Suspensions
- 76T25 Granular flows [See also 74C99, 74E20]
- 76T30 Three or more component flows
- 76T99 None of the above, but in this section
- 76Uxx Rotating fluids**
- 76U05 Rotating fluids
- 76U99 None of the above, but in this section

- 76Vxx**    **Reaction effects in flows [See also 80A32]**
- 76V05    Reaction effects in flows [See also 80A32]
- 76V99    None of the above, but in this section
- 76Wxx**    **Magnetohydrodynamics and electrohydrodynamics**
- 76W05    Magnetohydrodynamics and electrohydrodynamics
- 76W99    None of the above, but in this section
- 76Xxx**    **Ionized gas flow in electromagnetic fields; plasmic flow**  
[See also 82D10]
- 76X05    Ionized gas flow in electromagnetic fields; plasmic flow  
[See also 82D10]
- 76X99    None of the above, but in this section
- 76Yxx**    **Quantum hydrodynamics and relativistic hydrodynamics**  
[See also 82D50, 83C55, 85A30]
- 76Y05    Quantum hydrodynamics and relativistic hydrodynamics  
[See also 82D50, 83C55, 85A30]
- 76Y99    None of the above, but in this section
- 76Zxx**    **Biological fluid mechanics [See also 74F10, 74L15, 92Cxx]**
- 76Z05    Physiological flows [See also 92C35]
- 76Z10    Biopropulsion in water and in air
- 76Z99    None of the above, but in this section
  
- 78–XX**    **OPTICS, ELECTROMAGNETIC THEORY FOR QUANTUM**  
**OPTICS, SEE 81V80{}**
- 78–00    General reference works (handbooks, dictionaries, bibliographies,  
etc.)
- 78–01    Instructional exposition (textbooks, tutorial papers, etc.)
- 78–02    Research exposition (monographs, survey articles)
- 78–03    Historical (must also be assigned at least one classification number  
from Section 01)
- 78–04    Explicit machine computation and programs (not the theory of  
computation or programming)
- 78–05    Experimental work
- 78–06    Proceedings, conferences, collections, etc.
- 78Axx**    **General**
- 78A02    Foundations
- 78A05    Geometric optics
- 78A10    Physical optics
- 78A15    Electron optics
- 78A20    Space charge waves
- 78A25    Electromagnetic theory, general
- 78A30    Electro- and magnetostatics
- 78A35    Motion of charged particles
- 78A37    Ion traps
- 78A40    Waves and radiation
- 78A45    Diffraction, scattering [See also 34E20 for WKB methods]
- 78A46    Inverse scattering problems
- 78A48    Composite media; random media
- 78A50    Antennas, wave-guides
- 78A55    Technical applications
- 78A57    Electrochemistry
- 78A60    Lasers, masers, optical bistability, nonlinear optics [See also 81V80]
- 78A70    Biological applications [See also 91D30, 92C30]

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- 78A97 Mathematically heuristic optics and electromagnetic theory (must also be assigned at least one other classification number in this section)
- 78A99 Miscellaneous topics
- 78Mxx Basic methods**
- 78M05 Method of moments
- 78M10 Finite element methods
- 78M12 Finite volume methods, finite integration techniques
- 78M15 Boundary element methods
- 78M16 Multipole methods
- 78M20 Finite difference methods
- 78M22 Spectral methods
- 78M25 Other numerical methods
- 78M30 Variational methods
- 78M31 Monte Carlo methods
- 78M32 Neural and heuristic methods
- 78M34 Model reduction
- 78M35 Asymptotic analysis
- 78M40 Homogenization
- 78M50 Optimization
- 78M99 None of the above, but in this section
- 80-XX CLASSICAL THERMODYNAMICS, HEAT TRANSFER FOR THERMODYNAMICS OF SOLIDS, SEE 74A15{}**
- 80-00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 80-01 Instructional exposition (textbooks, tutorial papers, etc.)
- 80-02 Research exposition (monographs, survey articles)
- 80-03 Historical (must also be assigned at least one classification number from Section 01)
- 80-04 Explicit machine computation and programs (not the theory of computation or programming)
- 80-05 Experimental work
- 80-06 Proceedings, conferences, collections, etc.
- 80Axx Thermodynamics and heat transfer**
- 80A05 Foundations
- 80A10 Classical thermodynamics, including relativistic
- 80A17 Thermodynamics of continua [See also 74A15]
- 80A20 Heat and mass transfer, heat flow
- 80A22 Stefan problems, phase changes, etc. [See also 74Nxx]
- 80A23 Inverse problems
- 80A25 Combustion
- 80A30 Chemical kinetics [See also 76V05, 92C45, 92E20]
- 80A32 Chemically reacting flows [See also 92C45, 92E20]
- 80A50 Chemistry (general) [See mainly 92Exx]
- 80A99 None of the above, but in this section
- 80Mxx Basic methods**
- 80M10 Finite element methods
- 80M12 Finite volume methods
- 80M15 Boundary element methods
- 80M20 Finite difference methods
- 80M22 Spectral methods

- 80M25 Other numerical methods
- 80M30 Variational methods
- 80M31 Monte Carlo methods
- 80M35 Asymptotic analysis
- 80M40 Homogenization
- 80M50 Optimization
- 80M99 None of the above, but in this section
- 81–XX QUANTUM THEORY**
- 81–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 81–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 81–02 Research exposition (monographs, survey articles)
- 81–03 Historical (must also be assigned at least one classification number from Section 01)
- 81–04 Explicit machine computation and programs (not the theory of computation or programming)
- 81–05 Experimental papers
- 81–06 Proceedings, conferences, collections, etc.
- 81–08 Computational methods
- 81Pxx Axiomatics, foundations, philosophy**
- 81P05 General and philosophical
- 81P10 Logical foundations of quantum mechanics; quantum logic [See also 03G12, 06C15]
- 81P13 Contextuality
- 81P15 Quantum measurement theory
- 81P16 Quantum state spaces, operational and probabilistic concepts
- 81P20 Stochastic mechanics (including stochastic electrodynamics)
- 81P40 Quantum coherence, entanglement, quantum correlations
- 81P45 Quantum information, communication, networks [see also 94A15, 94A17]
- 81P50 Quantum state estimation, approximate cloning
- 81P68 Quantum computation [See also 68Q05, 68Q12]
- 81P70 Quantum coding (general)
- 81P94 Quantum quantum cryptography [See also 94A60]
- 81P99 None of the above, but in this section
- 81Qxx General mathematical topics and methods in quantum theory**
- 81Q05 Closed and approximate solutions to the Schrödinger, Dirac, Klein-Gordon and other equations of quantum mechanics
- 81Q10 Selfadjoint operator theory in quantum theory, including spectral analysis
- 81Q12 Non-selfadjoint operator theory in quantum theory
- 81Q15 Perturbation theories for operators and differential equations
- 81Q20 Semiclassical techniques, including WKB and Maslov methods
- 81Q30 Feynman integrals and graphs; applications of algebraic topology and algebraic geometry [See also 14D05, 32S40]
- 81Q35 Quantum mechanics on special spaces: manifolds, fractals, graphs, etc.
- 81Q37 Quantum dots, waveguides, ratchets, etc.
- 81Q40 Bethe-Salpeter and other integral equations
- 81Q50 Quantum chaos [See also 37Dxx]
- 81Q60 Supersymmetry and quantum mechanics

- 81Q65 Alternative quantum mechanics
- 81Q70 Differential-geometric methods, including holonomy, Berry and Hannay phases, etc.
- 81Q80 Special quantum systems, such as solvable systems
- 81Q93 Quantum control
- 81Q99 None of the above, but in this section
- 81Rxx Groups and algebras in quantum theory**
- 81R05 Finite-dimensional groups and algebras motivated by physics and their representations [See also 20C35, 22E70]
- 81R10 Infinite-dimensional groups and algebras motivated by physics, including Virasoro, Kac-Moody,  $W$ -algebras and other current algebras and their representations [See also 17B65, 17B67, 22E65, 22E67, 22E70]
- 81R12 Relations with integrable systems [See also 17Bxx, 37J35]
- 81R15 Operator algebra methods [See also 46Lxx, 81T05]
- 81R20 Covariant wave equations
- 81R25 Spinor and twistor methods [See also 32L25]
- 81R30 Coherent states [See also 22E45]; squeezed states [See also 81V80]
- 81R40 Symmetry breaking
- 81R50 Quantum groups and related algebraic methods [See also 16T20, 17B37]
- 81R60 Noncommutative geometry
- 81R99 None of the above, but in this section
- 81Sxx General quantum mechanics and problems of quantization**
- 81S05 Canonical quantization, commutation relations and statistics
- 81S10 Geometry and quantization, symplectic methods [See also 53D50]
- 81S20 Stochastic quantization
- 81S22 Open systems, reduced dynamics, master equations, decoherence [See also 82C31]
- 81S25 Quantum stochastic calculus
- 81S30 Phase-space methods including Wigner distributions, etc.
- 81S40 Path integrals [See also 58D30]
- 81S99 None of the above, but in this section
- 81Txx Quantum field theory; related classical field theories [See also 70Sxx]**
- 81T05 Axiomatic quantum field theory; operator algebras
- 81T08 Constructive quantum field theory
- 81T10 Model quantum field theories
- 81T13 Yang-Mills and other gauge theories [See also 53C07, 58E15]
- 81T15 Perturbative methods of renormalization
- 81T16 Nonperturbative methods of renormalization
- 81T17 Renormalization group methods
- 81T18 Feynman diagrams
- 81T20 Quantum field theory on curved space backgrounds
- 81T25 Quantum field theory on lattices
- 81T27 Continuum limits
- 81T28 Thermal quantum field theory [see also 82B30]
- 81T30 String and superstring theories; other extended objects (e.g., branes) [See also 83E30]
- 81T40 Two-dimensional field theories, conformal field theories, etc.
- 81T45 Topological field theories [See also 57R56, 58Dxx]
- 81T50 Anomalies

- 81T55 Casimir effect
- 81T60 Supersymmetric field theories
- 81T70 Quantization in field theory; cohomological methods [See also 58D29]
- 81T75 Noncommutative geometry methods [See also 46L85, 46L87, 58B34]
- 81T80 Simulation and numerical modeling
- 81T99 None of the above, but in this section
- 81Uxx Scattering theory [See also 34A55, 34L25, 34L40, 35P25, 47A40]**
- 81U05 2-body potential scattering theory [See also 34E20 for WKB methods]
- 81U10  $n$ -body potential scattering theory
- 81U15 Exactly and quasi-solvable systems
- 81U20  $S$ -matrix theory, etc.
- 81U30 Dispersion theory, dispersion relations
- 81U35 Inelastic and multichannel scattering
- 81U40 Inverse scattering problems
- 81U99 None of the above, but in this section
- 81Vxx Applications to specific physical systems**
- 81V05 Strong interaction, including quantum chromodynamics
- 81V10 Electromagnetic interaction; quantum electrodynamics
- 81V15 Weak interaction
- 81V17 Gravitational interaction [See also 83Cxx and 83Exx]
- 81V19 Other fundamental interactions
- 81V22 Unified theories
- 81V25 Other elementary particle theory
- 81V35 Nuclear physics
- 81V45 Atomic physics
- 81V55 Molecular physics [See also 92E10]
- 81V65 Quantum dots [See also 82D20]
- 81V70 Many-body theory; quantum Hall effect
- 81V80 Quantum optics
- 81V99 None of the above, but in this section
- 82–XX STATISTICAL MECHANICS, STRUCTURE OF MATTER**
- 82–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 82–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 82–02 Research exposition (monographs, survey articles)
- 82–03 Historical (must also be assigned at least one classification number from Section 01)
- 82–04 Explicit machine computation and programs (not the theory of computation or programming)
- 82–05 Experimental papers
- 82–06 Proceedings, conferences, collections, etc.
- 82–08 Computational methods
- 82Bxx Equilibrium statistical mechanics**
- 82B03 Foundations
- 82B05 Classical equilibrium statistical mechanics (general)
- 82B10 Quantum equilibrium statistical mechanics (general)
- 82B20 Lattice systems (Ising, dimer, Potts, etc.) and systems on graphs
- 82B21 Continuum models (systems of particles, etc.)
- 82B23 Exactly solvable models; Bethe ansatz
- 82B24 Interface problems; diffusion-limited aggregation

- 82B26 Phase transitions (general)
- 82B27 Critical phenomena
- 82B28 Renormalization group methods [See also 81T17]
- 82B30 Statistical thermodynamics [See also 80–XX]
- 82B31 Stochastic methods
- 82B35 Irreversible thermodynamics, including Onsager-Machlup theory  
[See also 92E20]
- 82B40 Kinetic theory of gases
- 82B41 Random walks, random surfaces, lattice animals, etc.  
[See also 60G50, 82C41]
- 82B43 Percolation [See also 60K35]
- 82B44 Disordered systems (random Ising models, random Schrödinger  
operators, etc.)
- 82B80 Numerical methods (Monte Carlo, series resummation, etc.)  
[See also 65–XX, 81T80]
- 82B99 None of the above, but in this section
- 82Cxx Time-dependent statistical mechanics (dynamic and nonequilibrium)**
- 82C03 Foundations
- 82C05 Classical dynamic and nonequilibrium statistical mechanics (general)
- 82C10 Quantum dynamics and nonequilibrium statistical mechanics  
(general)
- 82C20 Dynamic lattice systems (kinetic Ising, etc.) and systems on graphs
- 82C21 Dynamic continuum models (systems of particles, etc.)
- 82C22 Interacting particle systems [See also 60K35]
- 82C23 Exactly solvable dynamic models [See also 37K60]
- 82C24 Interface problems; diffusion-limited aggregation
- 82C26 Dynamic and nonequilibrium phase transitions (general)
- 82C27 Dynamic critical phenomena
- 82C28 Dynamic renormalization group methods [See also 81T17]
- 82C31 Stochastic methods (Fokker-Planck, Langevin, etc.) [See also 60H10]
- 82C32 Neural nets [See also 68T05, 91E40, 92B20]
- 82C35 Irreversible thermodynamics, including Onsager-Machlup theory
- 82C40 Kinetic theory of gases
- 82C41 Dynamics of random walks, random surfaces, lattice animals, etc.  
[See also 60G50]
- 82C43 Time-dependent percolation [See also 60K35]
- 82C44 Dynamics of disordered systems (random Ising systems, etc.)
- 82C70 Transport processes
- 82C80 Numerical methods (Monte Carlo, series resummation, etc.)
- 82C99 None of the above, but in this section
- 82Dxx Applications to specific types of physical systems**
- 82D05 Gases
- 82D10 Plasmas
- 82D15 Liquids
- 82D20 Solids
- 82D25 Crystals  $\{\{\}\}$ For crystallographic group theory, see 20H15
- 82D30 Random media, disordered materials (including liquid crystals and  
spin glasses)
- 82D35 Metals
- 82D37 Semiconductors
- 82D40 Magnetic materials

- 82D45 Ferroelectrics
- 82D50 Superfluids
- 82D55 Superconductors
- 82D60 Polymers
- 82D75 Nuclear reactor theory; neutron transport
- 82D77 Quantum wave guides, quantum wires [See also 78A50]
- 82D80 Nanostructures and nanoparticles
- 82D99 None of the above, but in this section
- 83–XX RELATIVITY AND GRAVITATIONAL THEORY**
- 83–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 83–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 83–02 Research exposition (monographs, survey articles)
- 83–03 Historical (must also be assigned at least one classification number from Section 01)
- 83–04 Explicit machine computation and programs (not the theory of computation or programming)
- 83–05 Experimental work
- 83–06 Proceedings, conferences, collections, etc.
- 83–08 Computational methods
- 83Axx Special relativity**
- 83A05 Special relativity
- 83A99 None of the above, but in this section
- 83Bxx Observational and experimental questions**
- 83B05 Observational and experimental questions
- 83B99 None of the above, but in this section
- 83Cxx General relativity**
- 83C05 Einstein's equations (general structure, canonical formalism, Cauchy problems)
- 83C10 Equations of motion
- 83C15 Exact solutions
- 83C20 Classes of solutions; algebraically special solutions, metrics with symmetries
- 83C22 Einstein-Maxwell equations
- 83C25 Approximation procedures, weak fields
- 83C27 Lattice gravity, Regge calculus and other discrete methods
- 83C30 Asymptotic procedures (radiation, news functions,  $H$ -spaces, etc.)
- 83C35 Gravitational waves
- 83C40 Gravitational energy and conservation laws; groups of motions
- 83C45 Quantization of the gravitational field
- 83C47 Methods of quantum field theory [See also 81T20]
- 83C50 Electromagnetic fields
- 83C55 Macroscopic interaction of the gravitational field with matter (hydrodynamics, etc.)
- 83C57 Black holes
- 83C60 Spinor and twistor methods; Newman-Penrose formalism
- 83C65 Methods of noncommutative geometry [See also 58B34]
- 83C75 Space-time singularities, cosmic censorship, etc.
- 83C80 Analogues in lower dimensions
- 83C99 None of the above, but in this section

- 83Dxx Relativistic gravitational theories other than Einstein's, including asymmetric field theories**
- 83D05 Relativistic gravitational theories other than Einstein's, including asymmetric field theories
- 83D99 None of the above, but in this section
- 83Exx Unified, higher-dimensional and super field theories**
- 83E05 Geometrodynamics
- 83E15 Kaluza-Klein and other higher-dimensional theories
- 83E30 String and superstring theories [See also 81T30]
- 83E50 Supergravity
- 83E99 None of the above, but in this section
- 83Fxx Cosmology**
- 83F05 Cosmology
- 83F99 None of the above, but in this section
- 85-XX ASTRONOMY AND ASTROPHYSICS FOR CELESTIAL MECHANICS, SEE 70F15{}**
- 85-00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 85-01 Instructional exposition (textbooks, tutorial papers, etc.)
- 85-02 Research exposition (monographs, survey articles)
- 85-03 Historical (must also be assigned at least one classification number from Section 01)
- 85-04 Explicit machine computation and programs (not the theory of computation or programming)
- 85-05 Experimental work
- 85-06 Proceedings, conferences, collections, etc.
- 85-08 Computational methods
- 85Axx Astronomy and astrophysics {{{}}For celestial mechanics, see 70F15**
- 85A04 General
- 85A05 Galactic and stellar dynamics
- 85A15 Galactic and stellar structure
- 85A20 Planetary atmospheres
- 85A25 Radiative transfer
- 85A30 Hydrodynamic and hydromagnetic problems [See also 76Y05]
- 85A35 Statistical astronomy
- 85A40 Cosmology {{{}}For relativistic cosmology, see 83F05
- 85A99 Miscellaneous topics
- 86-XX GEOPHYSICS [See also 76U05, 76V05]**
- 86-00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 86-01 Instructional exposition (textbooks, tutorial papers, etc.)
- 86-02 Research exposition (monographs, survey articles)
- 86-03 Historical (must also be assigned at least one classification number from Section 01)
- 86-04 Explicit machine computation and programs (not the theory of computation or programming)
- 86-05 Experimental work
- 86-06 Proceedings, conferences, collections, etc.
- 86-08 Computational methods

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- 86Axx**    **Geophysics [See also 76U05, 76V05]**
- 86A04    General
- 86A05    Hydrology, hydrography, oceanography [See also 76Bxx, 76E20, 76Q05, 76Rxx, 76U05]
- 86A10    Meteorology and atmospheric physics [See also 76Bxx, 76E20, 76N15, 76Q05, 76Rxx, 76U05]
- 86A15    Seismology
- 86A17    Global dynamics, earthquake problems
- 86A20    Potentials, prospecting
- 86A22    Inverse problems [See also 35R30]
- 86A25    Geo-electricity and geomagnetism [See also 76W05, 78A25]
- 86A30    Geodesy, mapping problems
- 86A32    Geostatistics
- 86A40    Glaciology
- 86A60    Geological problems
- 86A99    Miscellaneous topics
- 90–XX**    **OPERATIONS RESEARCH, MATHEMATICAL PROGRAMMING**
- 90–00    General reference works (handbooks, dictionaries, bibliographies, etc.)
- 90–01    Instructional exposition (textbooks, tutorial papers, etc.)
- 90–02    Research exposition (monographs, survey articles)
- 90–03    Historical (must also be assigned at least one classification number from Section 01)
- 90–04    Explicit machine computation and programs (not the theory of computation or programming)
- 90–06    Proceedings, conferences, collections, etc.
- 90–08    Computational methods
- 90Bxx**    **Operations research and management science**
- 90B05    Inventory, storage, reservoirs
- 90B06    Transportation, logistics
- 90B10    Network models, deterministic
- 90B15    Network models, stochastic
- 90B18    Communication networks [See also 68M10, 94A05]
- 90B20    Traffic problems
- 90B22    Queues and service [See also 60K25, 68M20]
- 90B25    Reliability, availability, maintenance, inspection [See also 60K10, 62N05]
- 90B30    Production models
- 90B35    Scheduling theory, deterministic [See also 68M20]
- 90B36    Scheduling theory, stochastic [See also 68M20]
- 90B40    Search theory
- 90B50    Management decision making, including multiple objectives [See also 90C31, 91A35, 91B06]
- 90B60    Marketing, advertising [See also 91B60]
- 90B70    Theory of organizations, manpower planning [See also 91D35]
- 90B80    Discrete location and assignment [See also 90C10]
- 90B85    Continuous location
- 90B90    Case-oriented studies
- 90B99    None of the above, but in this section

- 90Cxx Mathematical programming [See also 49Mxx, 65Kxx]**
- 90C05 Linear programming
- 90C06 Large-scale problems
- 90C08 Special problems of linear programming (transportation, multi-index, etc.)
- 90C09 Boolean programming
- 90C10 Integer programming
- 90C11 Mixed integer programming
- 90C15 Stochastic programming
- 90C20 Quadratic programming
- 90C22 Semidefinite programming
- 90C25 Convex programming
- 90C26 Nonconvex programming, global optimization
- 90C27 Combinatorial optimization
- 90C29 Multi-objective and goal programming
- 90C30 Nonlinear programming
- 90C31 Sensitivity, stability, parametric optimization
- 90C32 Fractional programming
- 90C33 Complementarity and equilibrium problems and variational inequalities (finite dimensions)
- 90C34 Semi-infinite programming
- 90C35 Programming involving graphs or networks [See also 90C27]
- 90C39 Dynamic programming [See also 49L20]
- 90C40 Markov and semi-Markov decision processes
- 90C46 Optimality conditions, duality [See also 49N15]
- 90C47 Minimax problems [See also 49K35]
- 90C48 Programming in abstract spaces
- 90C49 Extreme-point and pivoting methods
- 90C51 Interior-point methods
- 90C52 Methods of reduced gradient type
- 90C53 Methods of quasi-Newton type
- 90C55 Methods of successive quadratic programming type
- 90C56 Derivative-free methods and methods using generalized derivatives [See also 49J52]
- 90C57 Polyhedral combinatorics, branch-and-bound, branch-and-cut
- 90C59 Approximation methods and heuristics
- 90C60 Abstract computational complexity for mathematical programming problems [See also 68Q25]
- 90C70 Fuzzy programming
- 90C90 Applications of mathematical programming
- 90C99 None of the above, but in this section
- 91–XX GAME THEORY, ECONOMICS, SOCIAL AND BEHAVIORAL SCIENCES**
- 91–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 91–01 Instructional exposition (textbooks, tutorial papers, etc.)
- 91–02 Research exposition (monographs, survey articles)
- 91–03 Historical (must also be assigned at least one classification number from section 01)
- 91–04 Explicit machine computation and programs (not the theory of computation or programming)

- 91-06 Proceedings, conferences, collections, etc.
- 91-08 Computational methods
- 91Axx Game theory**
- 91A05 2-person games
- 91A06  $n$ -person games,  $n > 2$
- 91A10 Noncooperative games
- 91A12 Cooperative games
- 91A13 Games with infinitely many players
- 91A15 Stochastic games
- 91A18 Games in extensive form
- 91A20 Multistage and repeated games
- 91A22 Evolutionary games
- 91A23 Differential games [See also 49N70]
- 91A24 Positional games (pursuit and evasion, etc.) [See also 49N75]
- 91A25 Dynamic games
- 91A26 Rationality, learning
- 91A28 Signaling, communication
- 91A30 Utility theory for games [See also 91B16]
- 91A35 Decision theory for games [See also 62Cxx, 91B06, 90B50]
- 91A40 Game-theoretic models
- 91A43 Games involving graphs [See also 05C57]
- 91A44 Games involving topology or set theory
- 91A46 Combinatorial games
- 91A50 Discrete-time games
- 91A55 Games of timing
- 91A60 Probabilistic games; gambling [See also 60G40]
- 91A65 Hierarchical games
- 91A70 Spaces of games
- 91A80 Applications of game theory
- 91A90 Experimental studies
- 91A99 None of the above, but in this section
- 91Bxx Mathematical economics {}{} For econometrics, see 62P20**
- 91B02 Fundamental topics (basic mathematics, methodology; applicable to economics in general)
- 91B06 Decision theory [See also 62Cxx, 90B50, 91A35]
- 91B08 Individual preferences
- 91B10 Group preferences
- 91B12 Voting theory
- 91B14 Social choice
- 91B15 Welfare economics
- 91B16 Utility theory
- 91B18 Public goods
- 91B24 Price theory and market structure
- 91B25 Asset pricing models
- 91B26 Market models (auctions, bargaining, bidding, selling, etc.)
- 91B30 Risk theory, insurance
- 91B32 Resource and cost allocation
- 91B38 Production theory, theory of the firm
- 91B40 Labor market, contracts
- 91B42 Consumer behavior, demand theory
- 91B44 Informational economics

- 91B50 General equilibrium theory
- 91B51 Dynamic stochastic general equilibrium theory
- 91B52 Special types of equilibria
- 91B54 Special types of economies
- 91B55 Economic dynamics
- 91B60 Trade models
- 91B62 Growth models
- 91B64 Macro-economic models (monetary models, models of taxation)
- 91B66 Multisectoral models
- 91B68 Matching models
- 91B69 Heterogeneous agent models
- 91B70 Stochastic models
- 91B72 Spatial models
- 91B74 Models of real-world systems
- 91B76 Environmental economics (natural resource models, harvesting, pollution, etc.)
- 91B80 Applications of statistical and quantum mechanics to economics (econophysics)
- 91B82 Statistical methods; economic indices and measures
- 91B84 Economic time series analysis [See also 62M10]
- 91B99 None of the above, but in this section
- 91Cxx Social and behavioral sciences: general topics {{{}}}**For statistics, see **62-XX**
- 91C05 Measurement theory
- 91C15 One- and multidimensional scaling
- 91C20 Clustering [See also 62D05]
- 91C99 None of the above, but in this section
- 91Dxx Mathematical sociology (including anthropology)**
- 91D10 Models of societies, social and urban evolution
- 91D20 Mathematical geography and demography
- 91D25 Spatial models [See also 91B72]
- 91D30 Social networks
- 91D35 Manpower systems [See also 91B40, 90B70]
- 91D99 None of the above, but in this section
- 91Exx Mathematical psychology**
- 91E10 Cognitive psychology
- 91E30 Psychophysics and psychophysiology; perception
- 91E40 Memory and learning [See also 68T05]
- 91E45 Measurement and performance
- 91E99 None of the above, but in this section
- 91Fxx Other social and behavioral sciences (mathematical treatment)**
- 91F10 History, political science
- 91F20 Linguistics [See also 03B65, 68T50]
- 91F99 None of the above, but in this section
- 91Gxx Mathematical finance**
- 91G10 Portfolio theory
- 91G20 Derivative securities
- 91G30 Interest rates (stochastic models)
- 91G40 Credit risk
- 91G50 Corporate finance
- 91G60 Numerical methods (including Monte Carlo methods)

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- 91G70 Statistical methods, econometrics
- 91G80 Financial applications of other theories (stochastic control, calculus of variations, PDE, SPDE, dynamical systems)
- 91G99 None of the above, but in this section
- 92-XX BIOLOGY AND OTHER NATURAL SCIENCES**
- 92-00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 92-01 Instructional exposition (textbooks, tutorial papers, etc.)
- 92-02 Research exposition (monographs, survey articles)
- 92-03 Historical (must also be assigned at least one classification number from Section 01)
- 92-04 Explicit machine computation and programs (not the theory of computation or programming)
- 92-06 Proceedings, conferences, collections, etc.
- 92-08 Computational methods
- 92Bxx Mathematical biology in general**
- 92B05 General biology and biomathematics
- 92B10 Taxonomy, statistics
- 92B15 General biostatistics [See also 62P10]
- 92B20 Neural networks, artificial life and related topics [See also 68T05, 82C32, 94Cxx]
- 92B25 Biological rhythms and synchronization
- 92B99 None of the above, but in this section
- 92Cxx Physiological, cellular and medical topics**
- 92C05 Biophysics
- 92C10 Biomechanics [See also 74L15]
- 92C15 Developmental biology, pattern formation
- 92C17 Cell movement (chemotaxis, etc.)
- 92C20 Neural biology
- 92C30 Physiology (general)
- 92C35 Physiological flow [See also 76Z05]
- 92C37 Cell biology
- 92C40 Biochemistry, molecular biology
- 92C42 Systems biology, networks
- 92C45 Kinetics in biochemical problems (pharmacokinetics, enzyme kinetics, etc.) [See also 80A30]
- 92C50 Medical applications (general)
- 92C55 Biomedical imaging and signal processing [See also 44A12, 65R10]
- 92C60 Medical epidemiology
- 92C80 Plant biology
- 92C99 None of the above, but in this section
- 92Dxx Genetics and population dynamics**
- 92D10 Genetics  $\{\{\}\}$ For genetic algebras, see 17D92
- 92D15 Problems related to evolution
- 92D20 Protein sequences, DNA sequences
- 92D25 Population dynamics (general)
- 92D30 Epidemiology
- 92D40 Ecology
- 92D50 Animal behavior
- 92D99 None of the above, but in this section

- 92Exx**    **Chemistry**  $\{\{\}\}$  **For biochemistry, see 92C40**
- 92E10    Molecular structure (graph-theoretic methods, methods of differential topology, etc.)
- 92E20    Classical flows, reactions, etc. [See also 80A30, 80A32]
- 92E99    None of the above, but in this section
- 92Fxx**    **Other natural sciences (should also be assigned at least one other classification number in this section)**
- 92F05    Other natural sciences (should also be assigned at least one other classification number in section 92)
- 92F99    None of the above, but in this section
- 93–XX**    **SYSTEMS THEORY; CONTROL FOR OPTIMAL CONTROL, SEE 49–XX**
- 93–00    General reference works (handbooks, dictionaries, bibliographies, etc.)
- 93–01    Instructional exposition (textbooks, tutorial papers, etc.)
- 93–02    Research exposition (monographs, survey articles)
- 93–03    Historical (must also be assigned at least one classification number from Section 01)
- 93–04    Explicit machine computation and programs (not the theory of computation or programming)
- 93–06    Proceedings, conferences, collections, etc.
- 93Axx**    **General**
- 93A05    Axiomatic system theory
- 93A10    General systems
- 93A13    Hierarchical systems
- 93A14    Decentralized systems
- 93A15    Large scale systems
- 93A30    Mathematical modeling (models of systems, model-matching, etc.)
- 93A99    None of the above, but in this section
- 93Bxx**    **Controllability, observability, and system structure**
- 93B03    Attainable sets
- 93B05    Controllability
- 93B07    Observability
- 93B10    Canonical structure
- 93B11    System structure simplification
- 93B12    Variable structure systems
- 93B15    Realizations from input-output data
- 93B17    Transformations
- 93B18    Linearizations
- 93B20    Minimal systems representations
- 93B25    Algebraic methods
- 93B27    Geometric methods
- 93B28    Operator-theoretic methods [See also 47A48, 47A57, 47B35, 47N70]
- 93B30    System identification
- 93B35    Sensitivity (robustness)
- 93B36     $H^\infty$ -control
- 93B40    Computational methods
- 93B50    Synthesis problems
- 93B51    Design techniques (robust design, computer-aided design, etc.)
- 93B52    Feedback control
- 93B55    Pole and zero placement problems

- 93B60 Eigenvalue problems
- 93B99 None of the above, but in this section
- 93Cxx Control systems**
- 93C05 Linear systems
- 93C10 Nonlinear systems
- 93C15 Systems governed by ordinary differential equations [See also 34H05]
- 93C20 Systems governed by partial differential equations
- 93C23 Systems governed by functional-differential equations  
[See also 34K35]
- 93C25 Systems in abstract spaces
- 93C30 Systems governed by functional relations other than differential  
equations (such as hybrid and switching systems)
- 93C35 Multivariable systems
- 93C40 Adaptive control
- 93C41 Problems with incomplete information
- 93C42 Fuzzy control systems
- 93C55 Discrete-time systems
- 93C57 Sampled-data systems
- 93C62 Digital systems
- 93C65 Discrete event systems
- 93C70 Time-scale analysis and singular perturbations
- 93C73 Perturbations
- 93C80 Frequency-response methods
- 93C83 Control problems involving computers (process control, etc.)
- 93C85 Automated systems (robots, etc.) [See also 68T40, 70B15, 70Q05]
- 93C95 Applications
- 93C99 None of the above, but in this section
- 93Dxx Stability**
- 93D05 Lyapunov and other classical stabilities (Lagrange, Poisson,  $L^p$ ,  $l^p$ ,  
etc.)
- 93D09 Robust stability
- 93D10 Popov-type stability of feedback systems
- 93D15 Stabilization of systems by feedback
- 93D20 Asymptotic stability
- 93D21 Adaptive or robust stabilization
- 93D25 Input-output approaches
- 93D30 Scalar and vector Lyapunov functions
- 93D99 None of the above, but in this section
- 93Exx Stochastic systems and control**
- 93E03 Stochastic systems, general
- 93E10 Estimation and detection [See also 60G35]
- 93E11 Filtering [See also 60G35]
- 93E12 System identification
- 93E14 Data smoothing
- 93E15 Stochastic stability
- 93E20 Optimal stochastic control
- 93E24 Least squares and related methods
- 93E25 Other computational methods
- 93E35 Stochastic learning and adaptive control
- 93E99 None of the above, but in this section

- 94–XX INFORMATION AND COMMUNICATION, CIRCUITS**
- 94–00 General reference works (handbooks, dictionaries, bibliographies, etc.)
  - 94–01 Instructional exposition (textbooks, tutorial papers, etc.)
  - 94–02 Research exposition (monographs, survey articles)
  - 94–03 Historical (must also be assigned at least one classification number from Section 01)
  - 94–04 Explicit machine computation and programs (not the theory of computation or programming)
  - 94–06 Proceedings, conferences, collections, etc.
  - 94Axx Communication, information**
  - 94A05 Communication theory [See also 60G35, 90B18]
  - 94A08 Image processing (compression, reconstruction, etc.) [See also 68U10]
  - 94A11 Application of orthogonal and other special functions
  - 94A12 Signal theory (characterization, reconstruction, filtering, etc.)
  - 94A13 Detection theory
  - 94A14 Modulation and demodulation
  - 94A15 Information theory, general [See also 62B10, 81P94]
  - 94A17 Measures of information, entropy
  - 94A20 Sampling theory
  - 94A24 Coding theorems (Shannon theory)
  - 94A29 Source coding [See also 68P30]
  - 94A34 Rate-distortion theory
  - 94A40 Channel models (including quantum)
  - 94A45 Prefix, length-variable, comma-free codes [See also 20M35, 68Q45]
  - 94A50 Theory of questionnaires
  - 94A55 Shift register sequences and sequences over finite alphabets
  - 94A60 Cryptography [See also 11T71, 14G50, 68P25, 81P94]
  - 94A62 Authentication and secret sharing [See also 81P94]
  - 94A99 None of the above, but in this section
  - 94Bxx Theory of error-correcting codes and error-detecting codes**
  - 94B05 Linear codes, general
  - 94B10 Convolutional codes
  - 94B12 Combined modulation schemes (including trellis codes)
  - 94B15 Cyclic codes
  - 94B20 Burst-correcting codes
  - 94B25 Combinatorial codes
  - 94B27 Geometric methods (including applications of algebraic geometry) [See also 11T71, 14G50]
  - 94B30 Majority codes
  - 94B35 Decoding
  - 94B40 Arithmetic codes [See also 11T71, 14G50]
  - 94B50 Synchronization error-correcting codes
  - 94B60 Other types of codes
  - 94B65 Bounds on codes
  - 94B70 Error probability
  - 94B75 Applications of the theory of convex sets and geometry of numbers (covering radius, etc.) [See also 11H31]
  - 94B99 None of the above, but in this section
  - 94Cxx Circuits, networks**
  - 94C05 Analytic circuit theory

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- 94C10 Switching theory, application of Boolean algebra; Boolean functions  
[See also 06E30]
- 94C12 Fault detection; testing
- 94C15 Applications of graph theory [See also 05Cxx, 68R10]
- 94C30 Applications of design theory [See also 05Bxx]
- 94C99 None of the above, but in this section
- 94Dxx Fuzzy sets and logic (in connection with questions of Section 94)**  
**[See also 03B52, 03E72, 28E10]**
- 94D05 Fuzzy sets and logic (in connection with questions of Section 94)  
[See also 03B52, 03E72, 28E10]
- 94D99 None of the above, but in this section
- 97-XX MATHEMATICS EDUCATION**
- 97-00 General reference works (handbooks, dictionaries, bibliographies,  
etc.)
- 97-01 Instructional exposition (textbooks, tutorial papers, etc.)
- 97-02 Research exposition (monographs, survey articles)
- 97-03 Historical (must also be assigned at least one classification number  
from Section 01)
- 97-04 Explicit machine computation and programs (not the theory of  
computation or programming)
- 97-06 Proceedings, conferences, collections, etc.
- 97Axx General, mathematics and education**
- 97A10 Comprehensive works. Reference books
- 97A20 Recreational mathematics Games [See also 00A08]
- 97A30 History of mathematics and mathematics education [See also 01-XX]
- 97A40 Mathematics and society
- 97A50 Bibliographies [See also 01-00]
- 97A70 Theses and postdoctoral theses
- 97A80 Popularization of mathematics
- 97A99 None of the above, but in this section
- 97Bxx Educational policy and systems**
- 97B10 Educational research and planning
- 97B20 General education
- 97B30 Vocational education
- 97B40 Higher education
- 97B50 Teacher education  $\{\{\}\}$ For research aspects, see 97C70
- 97B60 Adult and further education
- 97B70 Syllabuses. Educational Standards
- 97B99 None of the above, but in this section
- 97Cxx Psychology of mathematics education. Research in mathematics  
education**
- 97C10 Comprehensive works
- 97C20 Affective behavior
- 97C30 Cognitive processes. Learning theories
- 97C40 Intelligence and aptitudes
- 97C50 Language and verbal communities
- 97C60 Sociological aspects of learning
- 97C70 Teaching-learning processes
- 97C99 None of the above, but in this section

- 97Dxx Education and instruction in mathematics**
- 97D10 Comprehensive works. Comparative studies
- 97D20 Philosophical and theoretical contributions (maths didactics)
- 97D30 Objectives and goals
- 97D40 Teaching methods and classroom techniques
- 97D50 Teaching problem solving and heuristic strategies  $\{\{\}\}$ For research aspects, see 97Cxx
- 97D60 Student assessment, achievement control and rating
- 97D70 Learning difficulties and student errors
- 97D80 Teaching units and draft lessons
- 97D99 None of the above, but in this section
- 97Exx Foundations of mathematics**
- 97E10 Comprehensive works
- 97E20 Philosophy and mathematics
- 97E30 Logic
- 97E40 Language of mathematics
- 97E50 Reasoning and proving in the mathematics classroom
- 97E60 Sets. Relations. Set theory
- 97E99 None of the above, but in this section
- 97Fxx Arithmetic. Number theory**
- 97F10 Comprehensive works
- 97F20 Pre-numerical stage. Concept of numbers
- 97F30 Natural numbers
- 97F40 Integers. Rational numbers
- 97F50 Real numbers. Complex numbers
- 97F60 Number theory
- 97F70 Measures and units
- 97F80 Ratio and proportion. Percentages
- 97F90 Real life mathematics. Practical arithmetic
- 97E99 None of the above, but in this section
- 97Gxx Geometry**
- 97G10 Comprehensive works
- 97G20 Informal geometry
- 97G30 Areas and volumes
- 97G40 Plane and solid geometry
- 97G50 Transformation geometry
- 97G60 Plane and spherical trigonometry
- 97G70 Analytic geometry. Vector algebra
- 97G80 Descriptive geometry
- 97G99 None of the above, but in this section
- 97Hxx Algebra**
- 97H10 Comprehensive works
- 97H20 Elementary algebra
- 97H30 Equations and inequalities
- 97H40 Groups, rings, fields
- 97H50 Ordered algebraic structures
- 97H60 Linear algebra
- 97H99 None of the above, but in this section
- 97Ixx Analysis**
- 97I10 Comprehensive works
- 97I20 Mappings and functions

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97I30	Sequences and series
97I40	Differential calculus
97I50	Integral calculus
97I60	Functions of several variables
97I70	Functional equations
97I80	Complex analysis
97I99	None of the above, but in this section
<b>97Kxx</b>	<b>Combinatorics. Graph theory. Probability. Statistics</b>
97K10	Comprehensive works
97K20	Combinatorics
97K30	Graph theory
97K40	Descriptive statistics
97K50	Probability theory
97K60	Distributions and stochastic processes
97K70	Foundations and methodology of statistics
97K80	Applied statistics
97K99	None of the above, but in this section
<b>97Mxx</b>	<b>Mathematical modeling. Applications of mathematics</b>
97M10	Modeling and interdisciplinarity
97M20	Mathematics in vocational training and career education
97M30	Financial and insurance mathematics
97M40	Operations research, economics
97M50	Physics. Astronomy. Technology. Engineering
97M60	Biology. Chemistry. Medicine
97M70	Behavioral and social sciences
97M80	Arts. Music. Language. Architecture
97M99	None of the above, but in this section
<b>97Nxx</b>	<b>Numerical mathematics</b>
97N10	Comprehensive works
97N20	Rounding, estimation. Theory of errors
97N30	Numerical algebra
97N40	Numerical analysis
97N50	Interpolation and approximation
97N60	Mathematical programming
97N70	Discrete mathematics
97N80	Mathematical software, computer programs
97N99	None of the above, but in this section
<b>97Pxx</b>	<b>Computer science</b>
97P10	Comprehensive works
97P20	Theory of computer science
97P30	System software
97P40	Programming languages
97P50	Programming techniques
97P60	Hardware
97P70	Computer science and society
97P99	None of the above, but in this section
<b>97Qxx</b>	<b>Computer science education</b>
97Q10	Comprehensive works
97Q20	Affective aspects in teaching computer science
97Q30	Cognitive processes
97Q40	Sociological aspects

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97Q50	Objectives
97Q60	Teaching methods and classroom techniques
97Q70	Student assessment
97Q80	Teaching units
97Q99	None of the above, but in this section
<b>97Rxx</b>	<b>Computer science applications</b>
97R10	Comprehensive works. Collections of programs
97R20	Applications in mathematics
97R30	Applications in sciences
97R40	Artificial intelligence
97R50	Data bases. Information systems
97R60	Computer graphics
97R70	User programs. Administrative applications
97R80	Recreational computing
97R99	None of the above, but in this section
<b>97Uxx</b>	<b>Educational material and media. Educational technology</b>
97U10	Comprehensive works
97U20	Textbooks. Textbook research
97U30	Teachers' manuals and planning aids
97U40	Problem books. Competitions. Examinations
97U50	Computer assisted instruction; e-learning
97U60	Manipulative materials
97U70	Technological tools. Calculators
97U80	Audiovisual media
97U99	None of the above, but in this section