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CARISTI'S AND DOWNING-KIRK'S FIXED POINT THEOREMS ON BIPOLAR METRIC SPACES

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Abstract. In this paper, we give some new fixed point results over bipolar metric spaces, that extend Caristi's and Downing-Kirk's fixed point theorems.
Key Words and Phrases: Bipolar metric space, fixed point, Caristi map, completeness.
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