ESSENTIAL WEAKLY MÖNCH TYPE MAPS AND CONTINUATION THEORY

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Abstract. In this paper we present a variety of Leray–Schauder type continuation theorems for general classes of weakly Mönch type maps.

Key Words and Phrases: Essential maps, fixed points, nonlinear alternatives, Mönch type maps.

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