BEST PROXIMITY THEOREMS OF PROXIMAL MULTIFUNCTIONS

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Abstract. Best proximity point theorems for self multifunctions have been proved with different conditions on the space and the considered mappings. In this paper, we prove some best proximity point theorems for a class of generalized multifunctions, namely proximal multifunctions.
Key Words and Phrases: Best proximity point, proximal multifunctions of first kind, proximal multifunctions of second kind, approximatively compact, cyclically Cauchy sequence, fairly Cauchy sequence, fairly complete space, uniform approximation, $T-$approximation, quasi-continuous.
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