

BEST PROXIMITY POINTS THEOREM IN b -METRIC SPACES ENDOWED WITH A GRAPH

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Abstract. In this paper the existence and uniqueness of best proximity point for Reich-type contraction on b -metric spaces endowed with a graph is established. These results are significant, since we replace the condition of continuity of mapping with the condition of G -continuity of mapping and we consider b -metric spaces endowed with a graph instead of metric spaces, under which can be unified some theorems of the existing literature.

Key Words and Phrases: b -metric space, best proximity point, P -property, G -proximal.

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