A HYBRID PROJECTION ALGORITHM FOR FINDING FIXED POINTS OF BREGMAN QUASI-STRICT PSEUDO-CONTRACTIONS

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Abstract. In this paper, a hybrid projection algorithm is investigated for finding fixed points of Bregman quasi-strict pseudo-contractions. Strong convergence theorems are established in the framework of reflexive Banach spaces.

Key Words and Phrases: Bregman projection, monotone operator, Banach space, strong convergence, fixed point.

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