ON GREGUS-ĆIRIĆ MAPPINGS ON WEIGHTED GRAPHS

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Abstract. In this paper, we introduce the concept of monotone Gregus-Ćirić-contraction mappings in weighted digraphs. Then we establish a fixed point theorem for monotone Gregus-Ćirić-contraction mappings defined in convex weighted digraphs.

Key Words and Phrases: Fixed point, Gregus-Ćirić-contraction, monotone mappings, weighted graph.

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