

## GENERALIZED MEIR-KEELER TYPE CONTRACTIONS AND DISCONTINUITY AT FIXED POINT

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**Abstract.** In this paper, we show that generalized Meir-Keeler type contractive definitions are strong enough to generate a fixed point but do not force the mapping to be continuous at the fixed point. Thus we provide more answers to the open question posed by B.E. Rhoades in the paper *Contractive definitions and continuity*, Contemporary Mathematics 72(1988), 233-245.

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