ON A BROAD CATEGORY OF MULTIVALUED WEAKLY PICARD OPERATORS

HATICE ASLAN HANÇER*, GÜLHAN MINAK** AND ISHAK ALTUN***

*Department of Mathematics, Faculty of Science and Arts
Kirikkale University, 71540 Yahsihan, Kirikkale, Turkey
E-mail: haslan@kku.edu.tr

**Department of Mathematics, Faculty of Science and Arts
Kirikkale University, 71540 Yahsihan, Kirikkale, Turkey
E-mail: g.minak.28@gmail.com

***Adress 1: King Saud University, College of Science,
Riyadh, Saudi Arabia
Adress 2: Department of Mathematics,
Faculty of Science and Arts,
Kirikkale University, 71450 Yahsihan, Kirikkale, Turkey,
E-mail: ishakaltun@yahoo.com.

Abstract. In the present paper, considering a recent technique which is used by Jleli and Samet [10] for fixed points of single-valued maps, we introduce a new concept of multivalued θ-contractions on metric spaces and prove that some of such mappings are multivalued weakly Picard operators on complete metric space. Finally, we give a nontrivial example to show that the class of multivalued θ-contractions is more general than multivalued contractions in the sense of Nadler [14] on complete metric spaces.
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