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FIXED POINT THEOREMS VIA CONE-NORMS AND CONE-VALUED MEASURES OF NONCOMPACTNESS

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Abstract. In this paper, we obtain an extension of the Krasnoselskii fixed point theorem for sum of two operators to the case of cone normed spaces. We also prove a variant of the Darbo-Sadovskii theorem on fixed points for operators condensing with respect to a cone-valued measure of noncompactness and apply it to the Cauchy problem with deviating argument.
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