

COMPARISON OF SOME TYPES OF LOCALLY COVERING MAPPINGS

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Abstract. Definitions of covering property that frequently appear in publications are discussed and compared. Several examples related to these definitions and coincidence points theorems of covering and Lipschitz mappings are constructed.

Key Words and Phrases: locally covering mappings; coincidence points.

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