

MULTIPLE POSITIVE SOLUTIONS FOR A HIGHER ORDER BOUNDARY VALUE PROBLEM ON TIME SCALES

İSMAİL YASLAN

Pamukkale University
Department of Mathematics
20070 Denizli, Turkey
E-mail: iyaslan@pau.edu.tr

Abstract. In this paper, we consider a nonlinear higher order three-point boundary value problem on time scales. We establish the criteria for the existence of one or two positive solutions for a higher order boundary value problem on time scales by using a result from the theory of fixed point index. Later, Leggett-Williams fixed-point theorem is used to investigate the existence of at least three positive solutions for a higher order boundary value problem on time scales. As an application, to demonstrate our results we also give an example.

Key Words and Phrases: Boundary value problems, cone, fixed point theorems, positive solutions, time scales.

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REFERENCES

- [1] R.P. Agarwal, D. O'Regan, *Nonlinear boundary value problems on time scales*, *Nonlinear Anal.*, **44**(2001), 527–535.
- [2] R.P. Agarwal, D. O'Regan, B. Yan, *Positive solutions for singular three-point boundary value problems*, *Electron. J. Diff. Equations*, **2008**(2008), 1–20.
- [3] D.R. Anderson, *Solutions to second order three-point problems on time scales*, *J. Difference Eq. Appl.*, **8**(2002), 673–688.
- [4] D.R. Anderson, R.I. Avery, *An even-order three-point boundary value problem on time scales*, *J. Math. Anal. Appl.*, **291**(2004), 514–525.
- [5] D.R. Anderson, *Nonlinear triple-point problems on time scales*, *Electron. J. Diff. Equations*, **47**(2004), 1–12.
- [6] D.R. Anderson, I.Y. Karaca, *Higher-order three-point boundary value problem on time scales*, *Comput. Math. Appl.*, **56**(2008), 2429–2443.
- [7] M. Bohner, A. Peterson, *Dynamic Equations on Time Scales: An Introduction with Applications*, Birkhäuser, Boston, 2001.
- [8] M. Bohner, A. Peterson (Eds.), *Advances in Dynamic Equations on Time Scales*, Birkhäuser, Boston, 2003.
- [9] J.J. DaCunha, J.M. Davis, P.K. Singh, *Existence results for singular three point boundary value problems on time scales*, *J. Math. Anal. Appl.*, **295**(2004), 378–391.

- [10] P.W. Eloe, J. McKelvey, *Positive solutions of three point boundary value problems*, Comm. Appl. Nonlinear Anal., **4**(1997), 45–54.
- [11] D. Guo, V. Lakshmikantham, *Nonlinear Problems in Abstract Cones*, Academic Press, San Diego, 1988.
- [12] S. Hilger, *Analysis on measure chains-A unified approach to continuous and discrete calculus*, Results Math., **18**(1990), 18–56.
- [13] S. Hong, *Triple positive solutions of three-point boundary value problems for p -Laplacian dynamic equations on time scales*, J. Comput. Appl. Math., **206**(2007), 967–976.
- [14] I.Y. Karaca, *Positive solutions of an n th order three-point boundary value problem*, Rocky Mountain J. Math., **43**(2013), 205–224.
- [15] K.Q. Lan, *Multiple positive solutions of semilinear differential equations with singularities*, J. London Math. Soc., **63**(2001), 690–704.
- [16] R.W. Leggett, L.R. Williams, *Multiple positive fixed points of nonlinear operators on ordered Banach spaces*, Indiana University Math. J., **28**(1979), 673–688.
- [17] R. Ma, D. O'Regan, *Positive solutions of singular sublinear second-order three-point boundary value problems*, Fixed Point Theory, **7**(2006), 65–81.
- [18] J.W. Neuberger, *The lack of self-adjointness in three point boundary value problems*, Pacific J. Math., **18**(1966), 165–168.
- [19] A.C. Peterson, Y.N. Raffoul, C.C. Tisdell, *Three point boundary value problems on time scales*, J. Differ. Equations Appl., **10**(2004), 843–849.
- [20] Y. Sang, H. Su, *Several sufficient conditions of solvability for a nonlinear higher order three point boundary value problem on time scales*, Appl. Math. Comput., **190**(2007), 566–575.
- [21] H.R. Sun, W.T. Li, *Positive solutions for nonlinear three-point boundary value problems on time scales*, J. Math. Anal. Appl., **299**(2004), 508–524.
- [22] D. Wang, *Three positive solutions of three-point boundary value problems for p -Laplacian dynamic equations on time scales*, Nonlinear Anal., **68**(2008), 2172–2180.
- [23] X. Xian, D. O'Regan, Z. Ruifang, *Existence and location results for sign-changing solutions for three-point boundary value problems using Leray-Schauder degree*, Monatsh. Math., **158**(2009), 413–439.
- [24] İ. Yaslan, *Existence results for an even-order boundary value problem on time scales*, Nonlinear Anal., **70**(2009), 483–491.

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