

## FRACTIONAL ITERATIVE FUNCTIONAL DIFFERENTIAL EQUATIONS WITH IMPULSES

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**Abstract.** In this paper, a class of impulsive fractional iterative functional differential equations is studied. By applying the Schauder fixed point theorem, the first existence result of solutions is presented. By applying the Picard operators methods, the second existence, uniqueness and data dependence results are also established.

**Key Words and Phrases:** Impulses, iterative functional differential equations, existence, uniqueness, data dependence, fixed point.

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