

CHARACTERIZATIONS OF COMMON FIXED POINTS OF ONE-PARAMETER NONEXPANSIVE SEMIGROUPS

YINGXIN GUO* AND MINGZHI XUE**

*School of Mathematical Sciences, Qufu Normal University
Qufu, Shandong 273165, P.R. China
E-mail: yxguo312@163.com

**Department of Mathematics, Shangqiu Normal University
Shangqiu 476000, Henan, P.R. China
E-mail: whl2762@163.com

Abstract. We prove characterizations of common fixed points of one-parameter nonexpansive semigroups. These results are sharper than some previous results.

Key Words and Phrases: Nonexpansive semigroup, common fixed point, convergence theorem.

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