

## PREŠIĆ-KANNAN-RUS FIXED POINT THEOREM ON PARTIALLY ORDER METRIC SPACES

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**Abstract.** The purpose of this paper is to present some fixed point theorems for operators  $f : X^k \rightarrow X$  satisfying a general Prešić-type contractivity condition on a partially order complete metric space  $X$ . Moreover, we give an application of our main theorem to the study of nonlinear differential equations.

**Key Words and Phrases:** Prešić-type contractive mapping, partially ordered set, fixed point.

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