

TWO ORDER THEORETIC PROOFS FOR A FIXED POINT THEOREM IN PARTIALLY ORDERED METRIC SPACES AND ITS APPLICATION TO TRACE CLASS OPERATOR EQUATIONS

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Abstract. In the present paper, we first give two order theoretic proofs for a known fixed point theorem in partially ordered metric spaces and then apply the results to find solutions of trace class operator equations.

Key Words and Phrases: Fixed points, posets, trace class operators.

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