

ITERATIONS AND FIXED POINTS FOR THE BERNSTEIN MAX-PRODUCT OPERATOR

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Abstract. In this paper we study the sequence of successive approximations, the fixed points and the Ishikawa iterates for the Bernstein max-product operator.

Key Words and Phrases: Bernstein max-product operator, nonexpansive operator, sequence of successive approximations, fixed points, Ishikawa iterations.

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