THE FIXED POINT PROPERTY OF THE CARTESIAN PRODUCT OF ROBERTS SPACES

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Abstract. We know all Roberts spaces have the fixed point property (see [6]) and it is not certain that the Cartesian product of fixed point spaces is a fixed point space. The aim of this paper is to show that the product of Roberts spaces has the fixed point property. This is an extension of the result in [6].

Key Words and Phrases: Linear metric spaces, convex sets, Roberts spaces, the fixed point property.

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