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A MULTIPLICITY RESULT OF POSITIVE SOLUTIONS FOR THIRD-ORDER MULTI-POINT BOUNDARY VALUE PROBLEM

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Abstract. By using fixed point theorem, multiple positive solutions for third-order multi-point boundary value problem with nonlinearity depending on all order derivative are established. The associated Green's function is also given.
Key Words and Phrases: Multi-point boundary value problem, positive solution, cone, fixed point.
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