SOME RESULTS ON ASYMPTOTICALLY HEMI-PSEUDOCONTRACTIVE MAPPINGS IN THE INTERMEDIATE SENSE

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Abstract. In this paper, a mapping which is asymptotically hemi-pseudocontractive in the intermediate sense is introduced. Hybrid projection methods are considered for the class of mappings. Strong convergence theorems for common fixed points are established in the framework of Hilbert spaces.
Key Words and Phrases: Asymptotically hemi-pseudocontractive mapping, asymptotically quasi-pseudocontractive mapping in the intermediate sense, fixed point, hybrid projection method.
2010 Mathematics Subject Classification: 47H09, 47H10, 47J25.

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