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# FIXED POINT THEOREMS FOR CONDENSING MULTIVALUED MAPPINGS UNDER WEAK TOPOLOGY FEATURES

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**Abstract.** We present new fixed point theorems for weakly condensing multivalued maps with weakly sequentially closed graph. Our fixed point results are obtained under Sadovskii's, Leray-Schauder's and Furi-Pera's type conditions.
**Key Words and Phrases**: Sadovskii's fixed point theorem, Krasnosel'skii's fixed point theorem, Leray-Schauder's fixed point theorem, measure of weak noncompactness, weakly condensing, multivalued maps.
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