

## AN ITERATIVE METHOD FOR GENERALIZED VARIATIONAL INEQUALITIES WITH APPLICATIONS

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**Abstract.** In this paper, we introduce a composite iterative process for an inverse-strongly accretive mapping and a nonexpansive mapping. We study the convergence analysis of the iterative algorithm. Strong convergence theorems are established in a real Banach space.

**Key Words and Phrases:** Sunny nonexpansive retraction, fixed point, nonexpansive mapping, variational inequality.

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