

COMMON FIXED POINTS OF BANACH OPERATOR PAIR ON FUZZY NORMED SPACES

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Abstract. We prove the existence of common fixed points of noncommuting mappings on fuzzy normed spaces.

Key Words and Phrases: Fixed point, fuzzy normed space, fuzzy nonexpansive mapping, R -subweakly commuting mappings, Banach operator pair.

2010 Mathematics Subject Classification: 47H10, 47H09, 54H25, 46S40.

Acknowledgements. The present version of the paper owes much to the precise and kind remarks of the learned referee. We also acknowledge with thanks Higher Education Commission of Pakistan research grant: 20-918/R&D/07.

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Received: December 10, 2008; Accepted: June 4, 2009.