

WEAK CONDITIONS FOR EXISTENCE OF RANDOM FIXED POINTS

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Abstract. In this article some results on existence of random fixed point for multivalued functions are extended. Such extensions involve weaker versions of some common concepts used on related studies.

Key Words and Phrases: Random fixed point, hemicompactness, multivalued random operators, condition (A).

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