

APPROXIMATE FIXED POINTS AND BEST PROXIMITY PAIRS

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Abstract. In this paper we give existence theorems of ϵ -fixed points for multi-functions from a subset to another in a Banach space. Our result extends previous approximate fixed point theorems. As a consequence we obtain new theorems of existence of best proximity pairs.

Key Words and Phrases: Approximate fixed point, best proximity pairs, reflexive spaces.

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