A NEW FIXED POINT THEOREM AND ITS APPLICATIONS IN EQUILIBRIUM THEORY

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Abstract. We give a new fixed-point theorem for lower semicontinuous correspondences and introduce the notion of Q'-majorized correspondences. As applications we obtain some new equilibrium theorems which improve the results of X. Wu in [8], referred to abstract economies with lower semicontinuous correspondences, respectively X. Liu and H.Cai in [4], referred to abstract economies with Q-majorized correspondences.

Key Words and Phrases: Fixed point, Q-majorized correspondences, Q'-majorized correspondences, abstract economy, equilibrium.

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