

FIXED POINT THEOREMS FOR OCCASIONALLY WEAKLY COMPATIBLE MAPPINGS, ERRATUM

G. JUNGCK* AND B. E. RHOADES**

*Department of Mathematics, Bradley University
Peoria, Illinois 62625
E-mail: gj@hilltop.bradley.edu

**Department of Mathematics, Indiana University, Bloomington
Indiana 47405-5701, USA
E-mail: rhoades@indiana.edu

Abstract. We correct the errors that appeared in [1].

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We correct the errors that appeared in [1].

291⁴, (X, d) should read (X, r) .

291⁵ Delete *such that* $f(X) \subset S(X)$,

291⁸ s, y should read x, y

291₉ – 291₈ Insert a new line which reads:

Define $\psi : \mathbb{R}^+ \rightarrow \mathbb{R}^+$ which is upper semicontinuous, nondecreasing, and satisfying $\psi(t) < t$ for each $t > 0$.

Because important items were left out of inequality (6) in the statement of Theorem 3 in [1], we shall state the correct Theorem 3 and include a proof.

Theorem 3. *Let X be a symmetric space with symmetric r, f, g, S , and T selfmaps of X satisfying*

$$\begin{aligned} (r(fx, gy))^p &\leq \psi(a(r(fx, Ty))^p + \\ &\quad + (1-a)\max\{\alpha(r(fx, Sx))^p, \beta(r(gy, Ty))^p\}, \\ &\quad (r(fx, Sx))^{p/2}(r(fx, Ty))^{p/2}, \\ &\quad (r(Ty, fx))^{p/2}(r(Sx, gy))^{p/2} \frac{1}{2}[r^p(Sx, fx) + r^p(Ty, gy)]) \end{aligned} \quad (1)$$

for all $x, y \in X$, where $0 < a, \alpha, \beta \leq 1$, and $p \geq 1$. If $\{f, S\}$ and $\{g, T\}$ are owc, then f, g, S , and T have a unique common fixed point.

Proof. By hypothesis there exist points x and y such that $fx = Sx$ and $gy = Ty$. Suppose that $fx \neq gy$. Then, from (6),

$$\begin{aligned} (r(fx, gy))^p &\leq \psi(a(r(fx, gy))^p + (1-a)\max\{0, 0, 0, (r(fx, gy))^p, 0\}) \\ &= \psi(r(fx, gy))^p < r(fx, gy)^p, \end{aligned}$$

a contradiction. Therefore $r(fx, gy) = 0$, which implies that $fx = gy$. Suppose that there exists another point z such that $fz = Sz$. Then, using (6) one obtains $fz = Sz = gy = Ty = fx = Sx$ and hence $w = fx = fz$ is the unique point of coincidence of f and S . By symmetry there exists a unique point $v \in X$ such that $v = gz = Tv$. It then follows that $w = v$, w is a common fixed point of f, g, S , and T , and w is unique. \square 293₃ – 293₂ Delete "satisfying $f(X) \subset T(X), g(X) \subset S(X)$, and"

294₃ Replace the period at the end of the line with a comma.

294₂ If should read for each $x, y \in X$ such that $Tx \neq Ty$. If

295¹ – 295₂ implies should read , along with SX or TX complete and (10) imply

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REFERENCES

- [1] G. Jungck and B. E. Rhoades, *Fixed point theorems for occasionally weakly compatible mappings*, Fixed Point Theory, **7**(2006), 287-296.

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