A GENERAL SELECTION THEOREM
FOR MULTIVALUED FUNCTIONS SATISFYING
AN IMPLICIT RELATION

VALERIU POPA

Department of Mathematics, University of Bacău

Strada Spiru Haret Nr. 8, 600114 Bacău Romania

E-mail: vpopa@ub.ro

Abstract. J.R. Jachymski [**?**] initiated the study of Caristi selection. Some generalizations of J.R. Jachymski result are proved in [**?**], [**?**], [**?**]. In this paper a general selection theorem for multivalued functions satisfying an implicit relation which generalizes the results by [**?**], [**?**] and [**?**] is proved.

Key Words and Phrases: Multivalued function, selection, Caristi mapping, implicit relation.

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