

ON THE PROPERTIES OF APPROXIMATION OF A SEQUENCES OF MODIFIED SZÁSZ-MIRAKJAN OPERATORS

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2000 Mathematics Subject Classification. 41A36, 41A35, 41A25

Keywords and phrases. Modified Szász-Mirakjan operators, order of approximation, simultaneous approximation.

We studies futher properties of approximation of the following sequence of operators, introduced in [1]

$$L_{\alpha}^{\rho}(f, x) = e^{-\alpha x} \left(f(0) + \sum_{k=1}^{\infty} \frac{(\alpha x)^k}{k!} \int_0^{\infty} \frac{\alpha \rho^{k\rho}}{\Gamma(k\rho)} \cdot e^{-\alpha \rho t} (\alpha t)^{k\rho-1} f(t) dt \right),$$

where $\alpha > 0$, $\rho > 0$ and $f : [0, \infty) \rightarrow \mathbf{R}$ is an integrable function, for which the series above converges for all $x \geq 0$. Varying the parameter ρ , these operators make a link between the Philips operators, obtained for $\rho = 1$ and the usual Szász-Mirakjan operators, obtained by passing to the limit $\rho \rightarrow \infty$.

REFERENCES

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