FIXED POINT THEOREMS FOR NONSELF OPERATORS IN *b*-METRIC SPACES

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Abstract. In this paper we prove some fixed point theorems for different type of contractions in the setting of a *b*-metric space. The starting point was a recent result of Rus and Şerban [16]. The presented theorems extend, generalize and unify several recent results in the literature.

Key Words and Phrases: Fixed point, *b*-metric space, nonself contraction, data dependence.

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