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PICARD OPERATORS ON ORDERED METRIC SPACES

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Abstract. In this paper, we shall give some results about Picard operators on ordered metric spaces. In fact, we shall prove that some contractive-like mappings satisfying some conditions on ordered metric spaces are Picard operators. We shall also present an application of our results.
Key Words and Phrases: Fixed point, Picard operator, orbitally continuous.
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