Fixed Point Theory, Volume 9, No. 1, 2008, 173-187 http://www.math.ubbcluj.ro/~nodeacj/sfptcj.html

TIME PERIODIC SOLUTIONS FOR A CLASS OF NONLINEAR BOUNDARY VALUE PROBLEMS

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Abstract. Using some results from the theory of monotone operators and a fixed point theorem due to F.E. Browder and W.V. Petryshyn, we prove the existence of time periodic solutions to a class of nonlinear hyperbolic problems, on positive semi-axis of spatial variable, which have applications in integrated circuits modelling.

Key Words and Phrases: Hyperbolic system, boundary condition, Cauchy problem, monotone operator, periodic solution.

2000 Mathematics Subject Classification: 35L50, 35B10, 47H10.

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This paper was presented at the International Conference on Nonlinear Operators, Differential Equations and Applications held in Cluj-Napoca (Romania) from July 4 to July 8, 2007.

¹⁷³

RODICA LUCA

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Received: July 7, 2007; Accepted: November 22, 2007.

174